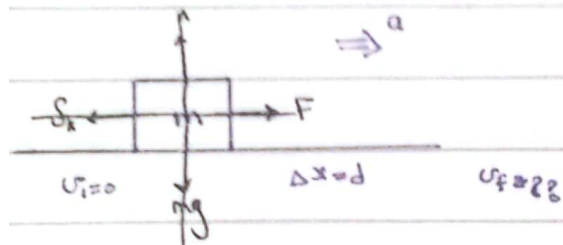


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Ex: 8.4 } Solve by Newton's law



$$\sum F_y = 0 \Rightarrow n = mg$$

$$\sum F_x = ma$$

$$F - f_k = ma$$

$$F - \mu_k n = ma$$

$$a = \frac{F - \mu_k n}{m} \Rightarrow a = \frac{F - \mu_k mg}{m}$$

$$\rightarrow v_f^2 = v_i^2 + 2a\Delta x$$

$$v_f^2 = 2 \left(\frac{F - \mu_k mg}{m} \right) d$$

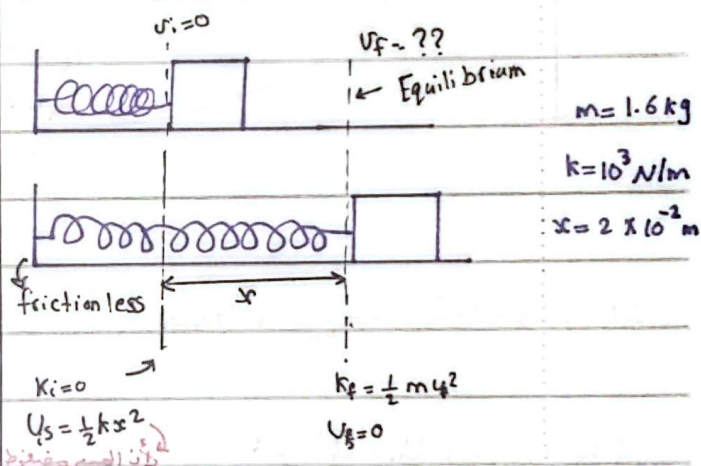
$$v_f = \sqrt{\frac{2(Fd - \mu_k mgd)}{m}}$$

نفس القبل
بالمثل (أ) بس الطريقة
التي

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Ex 8.6: A block of mass 1.6 kg is attached to a horizontal spring that has a force constant of 1000 N/m as shown in Figure (2). The spring is compressed 2 cm and is released from rest as in Figure (1).

(A) calculate the speed of block as it passes through the equilibrium position $x=0$ if the surface is frictionless.



$$\Delta K + \Delta U_g + \Delta U_s = -f_k d + W_{\text{app}}$$

$$(K_f - K_i) + (U_{gf} - U_{gi}) = 0$$

$$\frac{1}{2} m v_f^2 - \frac{1}{2} k x^2 = 0$$

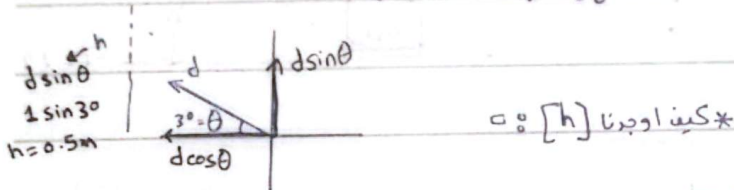
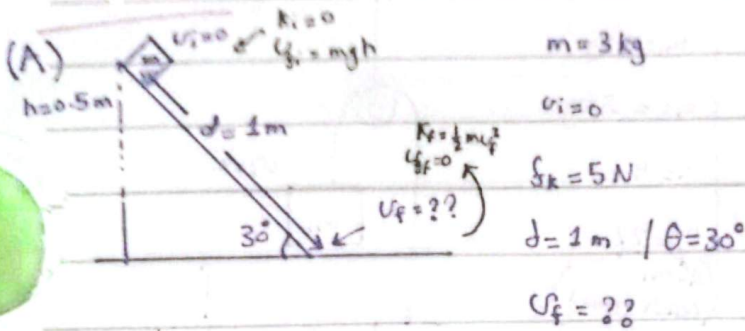
$$\frac{1}{2} m v_f^2 = \frac{1}{2} k x^2 \Rightarrow v_f^2 = \frac{k x^2}{m}$$

$$v_f = \sqrt{\frac{k x^2}{m}}$$

$$v_f = 0.5 \text{ m/s}$$

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Ex 8.7.



$$\Delta K + \Delta U_g + \Delta U_s = -f_k d + W_{app}$$

$$(K_f - K_i) + (U_{gf} - U_{gi}) = -f_k d$$

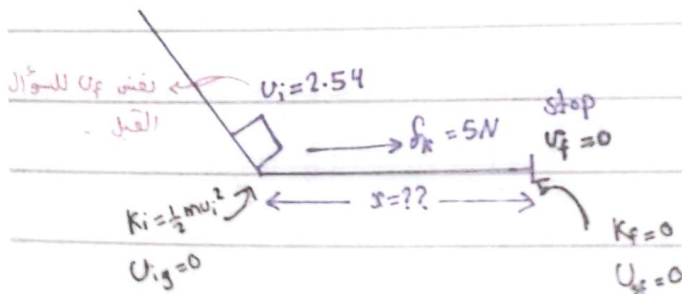
$$\frac{1}{2} m v_f^2 - mgh = -f_k d$$

$$\frac{1}{2} m v_f^2 = mgh - f_k d$$

$$v_f = \sqrt{\frac{2(mgh - f_k d)}{m}}$$

$$v_f = 2.54 \text{ m/s}$$

(B) if the object moves horizontally until stop.



$$\Delta K + \Delta U_g + \Delta U_s = -f_k d + W_{app}$$

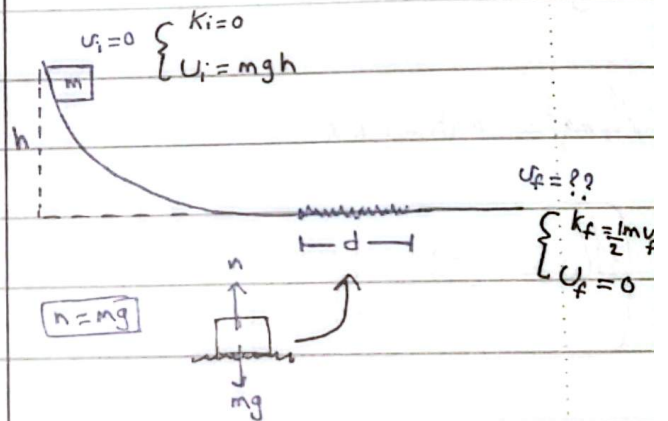
$$(K_f - K_i) + (U_{gf} - U_{gi}) = -f_k d$$

$$-\frac{1}{2} m v_i^2 = -f_k d$$

$$d = \frac{m v_i^2}{2 f_k}$$

$$d = 1.93 \text{ m}$$

Ex:



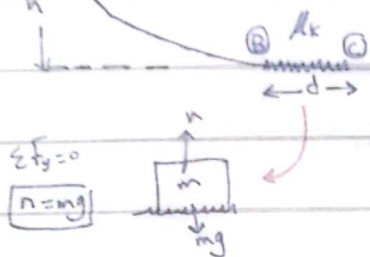
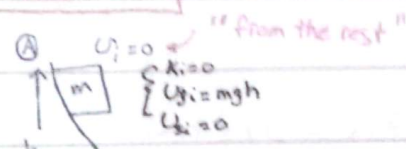
$$\Delta K + \Delta U_g + \Delta U_s = -f_k d + W_{app}$$

$$(K_f - K_i) + (U_{gf} - U_{gi}) = -\mu_k m g d$$

$$\frac{1}{2} m v_f^2 - mgh = -\mu_k m g d$$

$$\frac{1}{2} m v_f^2 = mgh - \mu_k m g d$$

$$v_f = \sqrt{2(g h - \mu_k g d)}$$



$h = 3\text{ m}$
 $m = 10\text{ kg}$
 $d = 6\text{ m}$
 $k = 2250\text{ N/m}$
 $x = 0.3\text{ m}$
 $k_k = ??$

"from the rest"
 "before coming to rest momentarily"
 "at the top of the spring"

$$\Delta K + \Delta U_g + \Delta U_s = -f_k d + W_{app}$$

$$(\cancel{K_f} - \cancel{K_i}) + (\cancel{U_{f,g}} - U_i)_g + (U_f - \cancel{U_i})_s = -\mu_k m g d$$

$$-mgh + \frac{1}{2} k x^2 = -\mu_k m g d$$

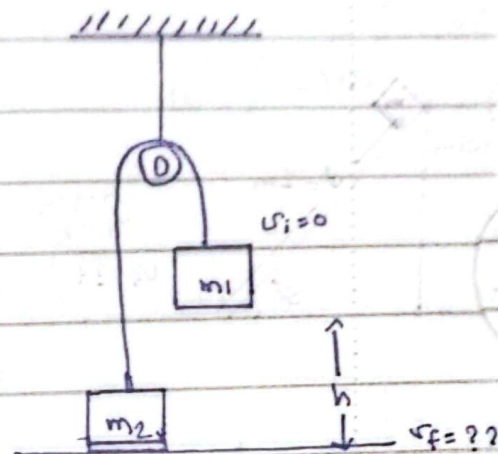
$$\mu_k m g d = mgh - \frac{1}{2} k x^2$$

$$\mu_k = \frac{mgh - \frac{1}{2} k x^2}{m g d}$$

$$\mu_k = 0.48$$

$m_1 = 5\text{ kg}$
 $m_2 = 3\text{ kg}$
 $h = 4\text{ m}$

$v_i = ??$
 (at m_1 reach ground)



الطريقة الأولى

1 (Newton's)

$$a = \frac{m_1 g - m_2 g}{m_1 + m_2}$$

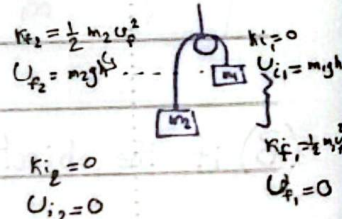
$$v_f^2 = v_i^2 + 2 a \Delta y$$

$$v_f^2 = (2) \frac{(m_1 - m_2) g h}{m_1 + m_2}$$

$$v_f = \sqrt{\frac{(2) g h (m_1 - m_2)}{(m_1 + m_2)}}$$

الطريقة الثانية

2 (Energy)



$$\Delta K_1 + \Delta K_2 + \Delta U_{1g} + \Delta U_{2g} + \Delta U_{s1} + \Delta U_{s2} = -f_k d_1 - f_k d_2$$

$$(\cancel{K_{f1}} - \cancel{K_{i1}}) + (\cancel{K_{f2}} - \cancel{K_{i2}}) + (\cancel{U_{f1,g}} - U_{i1})_g + (U_{f2} - \cancel{U_{i2}})_g = 0$$

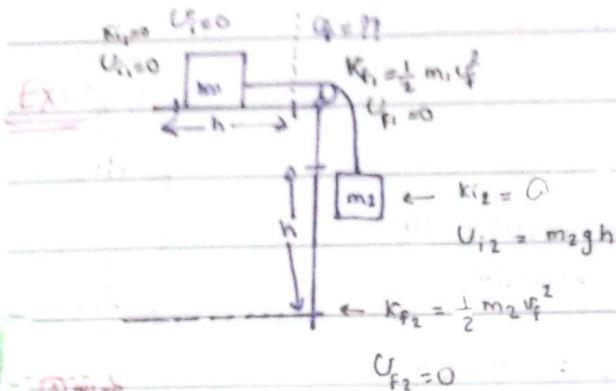
$$\frac{1}{2} m_1 v_f^2 + \frac{1}{2} m_2 v_f^2 - m_1 g h + m_2 g h = 0$$

$$\frac{1}{2} v_f^2 (m_1 + m_2) - g h (m_1 - m_2) = 0$$

$$\frac{1}{2} v_f^2 (m_1 + m_2) = g h (m_1 - m_2)$$

$$v_f = \sqrt{\frac{2 g h (m_1 - m_2)}{(m_1 + m_2)}}$$

Subject Monday 15/12/2025



1 (Newton's)

$$a = \frac{m_2 g}{m_1 + m_2}$$

$$u_f^2 = u_i^2 + 2a \Delta x$$

$$u_f^2 = 2 \left(\frac{m_2 g}{m_1 + m_2} \right) h$$

$$u_f = \sqrt{\frac{2h(m_2 g)}{m_1 + m_2}}$$

الطريقة الثانية

2 (Energy)

$$\Delta K_1 + \Delta K_2 + \Delta U_1 + \Delta U_2 = 0$$

$$(K_{f1} - K_{i1}) + (K_{f2} - K_{i2}) + (U_{f1} - U_{i1}) + (U_{f2} - U_{i2}) = 0$$

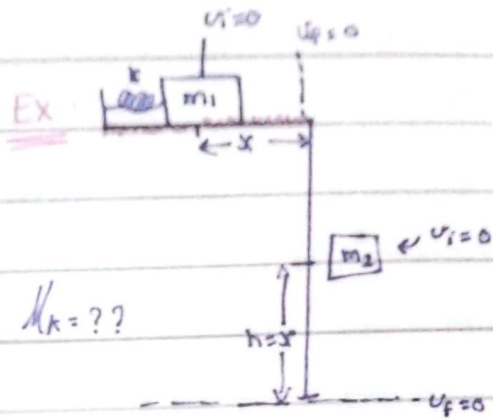
$$\frac{1}{2} m_1 u_f^2 + \frac{1}{2} m_2 u_f^2 - m_2 g h = 0$$

$$\frac{1}{2} u_f^2 (m_1 + m_2) = m_2 g h$$

$$u_f = \sqrt{\frac{2m_2 g h}{m_1 + m_2}}$$

Date

No



$\mu_k = ??$

$$\Delta K_1 + \Delta K_2 + \Delta U_{g1} + \Delta U_{g2} + \Delta U_{s1} + \Delta U_{s2} = -f_k \Delta x$$

$$(U_{sf1} - U_{ei1}) + (U_{sf2} - U_{ei2}) = -\mu_k m_1 g x$$

$$-m_2 g x + \frac{1}{2} k x^2 = -\mu_k m_1 g x$$

$$\mu_k = \frac{m_2 g - \frac{1}{2} k x}{m_1 g}$$

NOTEBOOK

* Power (P)

$$P = \frac{W}{t}$$

$$P = \frac{dW}{dt}$$

$$P = \frac{W}{t} = \frac{Fd \cos \theta}{t}$$

$$P = \vec{F} \cdot \vec{v}$$

$$P = Fv \cos \theta$$

$$P = \frac{W}{t} = Fv \cos \theta$$

$$[P] = \frac{[W]}{[t]} = \frac{J}{s}$$

$$[P] = J/s / \text{watt}$$

$$\text{or } [P] = Nm/s \quad \leftarrow \frac{Nm}{s}$$

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Ex: 8.11

$$m_e = 1600 \text{ kg}$$

↳ elevator

$$m_p = 200 \text{ kg}$$

↳ passengers

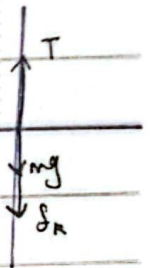
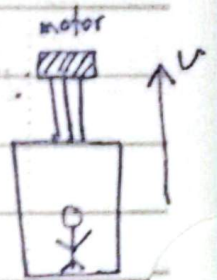
$$m_{\text{total}} = 1800 \text{ kg}$$

$$F_K = 4000 \text{ N}$$

$$v = 3 \text{ m/s}$$

$$P = ??$$

$$\Rightarrow a = 0 \Rightarrow \sum F = 0$$



* القوة المؤثرة على رافعة قوة السحب.

$$T = mg + F_K$$

$$P = Fv \cos \theta$$

$$= T v \cos \theta$$

$$= (mg + F_K) v$$

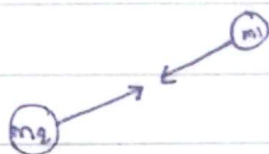
$$= ((1800)(9.8) + 4000)(3)$$

$$P = 6.49 \times 10^4 \text{ W}$$

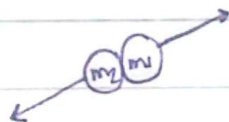
chapter 9

Momentum & Collision ...

before



after



$$\vec{F}_{12} = -\vec{F}_{21}$$

$$\vec{F}_{12} + \vec{F}_{21} = 0$$

$$m_1 \vec{a}_1 + m_2 \vec{a}_2 = 0$$

$$m_1 \frac{d\vec{v}_1}{dt} + m_2 \frac{d\vec{v}_2}{dt} = 0$$

$$\int m_1 \frac{d\vec{v}_1}{dt} + \int m_2 \frac{d\vec{v}_2}{dt} = \int 0 dt$$

$$m_1 \vec{v}_1 + m_2 \vec{v}_2 = \text{const}$$

$$\boxed{\vec{P} = m\vec{v}} \quad \text{linear momentum}$$

$$\vec{P}_1 + \vec{P}_2 = \text{const}$$

$$\underbrace{\vec{P}_{1i} + \vec{P}_{2i}}_{\text{before}} = \underbrace{\vec{P}_{1f} + \vec{P}_{2f}}_{\text{after}}$$

$$\boxed{\sum \vec{P}_i = \sum \vec{P}_f}$$

$$\sum \vec{P}_i - \sum \vec{P}_f = 0$$

$$\Delta \vec{P} = 0$$

systems

isolated system

non-isolated

$$\boxed{\Delta \vec{P} = 0}$$

$$\vec{I} = 0$$

$$\boxed{\Delta \vec{P} = \int_{t_i}^{t_f} \vec{F} dt}$$

$$\vec{I} = \Delta \vec{P}$$

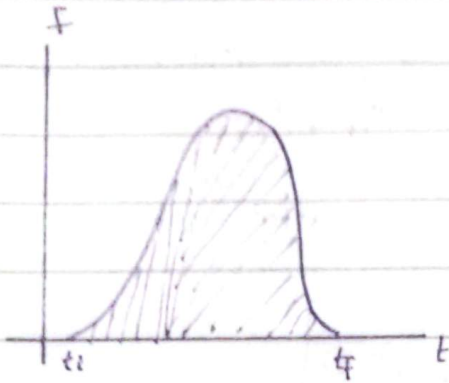
 $\vec{I}$ = impulse

$$\Delta \vec{P} = \vec{I}$$

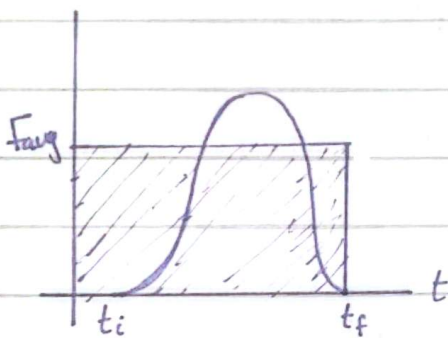
↳ isolated

$$\Delta \vec{P} = 0$$

$$\boxed{I = \int_{t_i}^{t_f} \vec{F} dt}$$

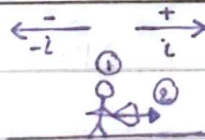


$I = \text{Area under curve.}$



$$I = F_{avg} \Delta t$$

Ex: 9.1



$$m_1 = 60 \text{ kg}$$

$$v_{1i} = 0$$

$$v_{1i} = 0$$

$$v_{2i} = 85 \text{ m/s}$$

$$m_2 = 0.03 \text{ kg}$$

$$v_{2f} = ??$$

$$\sum P_i = \sum P_f$$

$$m_1 v_{1i} + m_2 v_{2i} = m_1 v_{1f} + m_2 v_{2f}$$

$$0 = 60 v_{1f} + 0.03(85)$$

$$-2.55 = 60 v_{1f}$$

$$v_{1f} = -0.042 \text{ m/s}$$

$$v_{1f} = -0.042 \hat{i}$$