



اللجنة الأكاديمية للهندسة المدنية

دفتر

فيزياء 1

رهف هماش

Contact us :



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	S.I	unit	Dim
of	Time	s	T
#	Mass	Kg	M
#	Length	m	L

$\text{nano: } n = 10^{-9}$
 $\text{Micro: } \mu = 10^{-6}$
 $\text{milli: } m = 10^{-3}$
 $\text{Kilo: } K = 10^3$
 $\text{giga: } G = 10^9$

Ex, $7 \text{ nm} = 7 \times 10^{-9} \text{ m}$
 $7 \mu \text{ m} = 7 \times 10^{-6} \text{ m}$
 $7 \text{ mm} = 7 \times 10^{-3} \text{ m}$
 $7 \text{ Km} = 7 \times 10^3 \text{ m}$
 $7 \text{ Gm} = 7 \times 10^9 \text{ m}$

v = velocity

$$v = \frac{x}{t} = \frac{\text{unit}}{[ms]} = \frac{\text{dim}}{[L/T]}$$

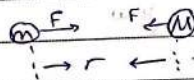
Ex $F = G \frac{mM}{r^2}$ ← $\frac{\text{force}}{a_1}$

find the unit of G ?

$$G = \frac{m^3}{s^2} \cdot \frac{1}{Kg}$$

Dim?

$$G = \frac{1^3}{T^2} \cdot \frac{1}{M}$$



$$F_{\text{force}} = ma \text{ [Kg} \cdot \text{m/s}^2]$$

$$Kg \cdot \frac{m}{s^2} = [G] \cdot \frac{Kg \cdot Kg}{m^2}$$

$$G = \frac{m^3}{s^2} \cdot \frac{1}{Kg} \leftarrow \text{unit}$$

$$r_2 = \frac{1}{2} = R \cdot a^n \cdot t^0 \rightarrow m = \left(\frac{m}{s^2}\right)^n (s)^0$$

If $\frac{1}{2}$: distance [m]

R : Constant $[F]$

a : acceleration $[m/s^2]$

t : time [s]

find the n

of n and a ?

$$m' = m^0 \cdot s^{-2n} \cdot s^0$$

$$m' = m^n \cdot s^{0-2n}$$

$$s^0 \cdot m' = m^n \cdot s^{0-2n}$$

$$m' = m^n \rightarrow n=1$$

$$2 = s^{0-2n}$$

$$2 = 0-2n = 2(1)$$

$$n = +2$$

$$R = \frac{G}{a}$$

$$s^0 = 1$$

$$s^1 = s$$

$$(s^2)^3 = s^6$$

$$s^2 \cdot s^3 = s^5$$

$$s^{-4} = \frac{1}{s^4}$$

$$S = R \cdot a^n \cdot t^o + V^w \cdot t^K$$

← قابل ہے

Find the values of $n, o, w, K?$

$R \leftarrow$ constant

$$\dot{S} = R \cdot a^n \cdot t^{o-1}$$

1 derivative

$$\dot{S} = V^w \cdot t^{K-1}$$

Ques 11 part 13/131

$$n=1, o=2$$

$$[\Delta x = v \cdot t + \frac{1}{2} a t^2] \text{ dimensional analysis}$$

$$h.w \left\{ \begin{array}{l} w=1 \\ K=1 \end{array} \right.$$

$$S = R \cdot a^n \cdot t^o + V^w \cdot t^K$$

$$S = R \cdot a^n \cdot t^o$$

$$S = V^w \cdot t^K$$

$$m = \left(\frac{m}{s}\right)^w \cdot (s)^K$$

$$m = m^w \cdot s^{-w} \cdot s^K$$

$$m = m^w \cdot s^{K-w}$$

$$s^0 \cdot m = m^w \cdot s^{K-w}$$

$$m^1 = m^w$$

$$\boxed{w=1}$$

$$s^0 = s^{K-w}$$

$$0 = K - w$$

$$0 = K - 1$$

$$\boxed{K=1}$$

$$S = R \cdot a^1 \cdot t^2 + V^1 \cdot t^1$$

1 - position

2 - velocity

3 - acceleration

1 - position

Distance ← المسافة

displacement ← $\Delta x = x_f - x_i / \Delta t = t_f - t_i$

2 - velocity

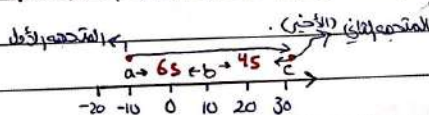
Average speed = $\frac{\text{distance}}{\text{time}}$

$$u = m/s$$

Average velocity = $\frac{\text{displacement}}{\text{time}}$

$$\frac{\Delta x}{\Delta t}$$

* Ex. find the distance, displacement, average speed and average velocity



* distance → $ab + bc$

$$20 + 20 = 40 \text{ m}$$

* displacement → $\Delta x = x_f - x_i$

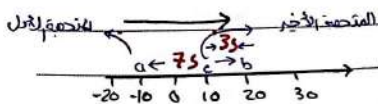
$$30 - (-10) = +40 \text{ m} \leftarrow \text{in } x\text{-axis positive}$$

* Average speed → $\frac{\text{distance}}{\text{time}} = \frac{40}{10} = 4 \text{ m/s}$

Average velocity → $\frac{\text{displacement}}{\text{time}}$

$$\frac{\Delta x}{\Delta t} = \frac{40}{10} = +4 \text{ m/s} \leftarrow \text{in } x\text{-axis positive}$$

Ex - Find the distance, displacement, average speed and average velocity.



• Distance = $ab + bc$

$30 + 10 = 40 \text{ m}$

• Displacement = $\Delta x = x_f - x_i$

$= 10 - (-10) = +20 \text{ m}$ in x -axis positive

• Average speed = $\frac{\text{distance}}{\text{time}}$

$\frac{40}{10} = 4 \text{ m/s}$

$7+3=10$

• Average velocity = $\frac{\text{displacement}}{\text{time}}$

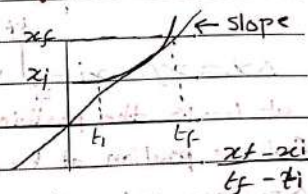
$\frac{\Delta x}{\Delta t} = \frac{20}{10} = +2 \text{ m/s}$ in x -axis positive

position $\nearrow$ Distance
 $\searrow$ Displacement = $\Delta x = x_f - x_i$

velocity $\nearrow$ Ave. speed = $\frac{\text{distance}}{\text{time}}$
 $\searrow$ Ave. velocity = $\frac{\Delta x}{\Delta t}$
 $\searrow$ Instantaneous velocity = $\vec{v}$

$$\vec{v} = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t}$$

$$\vec{v} = \frac{dx}{dt} = \text{slope}$$



* Ex, $x = 3t^2 - t + 4$

Find the ave. velocity from $t = 1s$ to $t = 3s$

$$v = \frac{x_f - x_i}{t_f - t_i} = \frac{28 - 6}{3 - 1} = \underline{\underline{+11 \text{ m/s}}}$$

ave. speed = ave. velocity

$$x(1) = 3 - 1 + 4 = 6m$$

$$x(3) = 27 - 3 + 4 = 28m$$

* Find the velocity at $t = 2s$ (instantaneous)

$$x = 3t^2 - t + 4 \rightarrow 6t - 1$$

$$v = 6 \times 2 - 1 = 12 - 1 = \underline{\underline{11 \text{ m/s}}}$$

7/15, $x = 3t^2 - 2t + 3$

position $t = (2-3)s$ h.m

velocity $t = 2s$

$$x_i = 3(2)^2 - 2(2) + 3 = 12 - 4 + 3 = 11m$$

$$x_f = 3(3)^2 - 2(3) + 3 = 27 - 6 + 3 = 24m$$

$$v = \frac{x_f - x_i}{t_f - t_i} = \frac{24 - 11}{3 - 2} = 13 \text{ m/s}$$

$$t = 2s$$

$$= 6t - 2$$

$$= 6(2) - 2$$

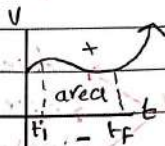
$$= 12 - 2$$

$$= 10 \text{ m/s}$$

$$v = \frac{dx}{dt}$$

$$dx = v \cdot dt$$

$$\int_{x_i}^{x_f} dx = \Delta x = \int_{t_i}^{t_f} v \cdot dt$$



$$\Delta x = x_f - x_i = \int_{t_i}^{t_f} v \cdot dt = \text{area}$$

at $t = 15$ the position = equal 2m

find the position at $t = 65$?

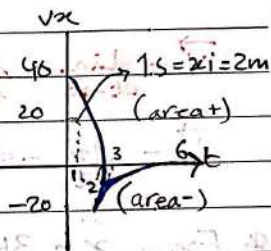
$$\Delta x = x_f - x_i = \text{area}$$

$$x_f - x_i = x_f - 2 = \text{area}_1 + -\text{area}_2$$

$$x_f - 2 = \frac{1}{2}(15)(20) - \frac{1}{2}(4)(20)$$

$$= 10 - 40 = -30$$

$$x_f = -30 + 2 = -28 \text{ m}$$



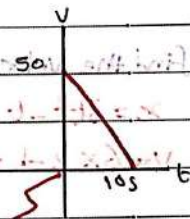
* At $t = 20$, the position = equal 5m

find the position at $t = 105$

$$x_f - x_i = \text{area}$$

$$x_f - 5 = \frac{1}{2}(10)(50)$$

$$x_f = 25 + 250 = \boxed{255 \text{ m}}$$



* find the displacement from $t=0$ to $t=105$

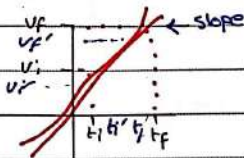
$$\Delta x = \text{area} = 250 \text{ m} \checkmark$$

or

$$x_f - x_i = 255 - 5 = 250 \text{ m} \checkmark$$

Acceleration $\rightarrow$ Ave. accel = $\bar{a} = \frac{\Delta v}{\Delta t} = \frac{v_f - v_i}{t_f - t_i}$

Instant. accel = $\vec{a} = \lim_{\Delta t \rightarrow 0} \frac{\Delta v}{\Delta t}$



$$\vec{a} = \frac{dv}{dt} = \frac{dx}{dt^2}$$

$$\text{slope} = \frac{v_f - v_i}{t_f - t_i}$$

Q15 $x = 3t^2 - 2t + 3$

A) Find the acceleration from $t = 2$ sec $t_f - t_i = 3$ s?

$$\bar{a} = \frac{v_f - v_i}{t_f - t_i} = \frac{16 - 10}{3 - 2} = 6 \text{ m/s}^2$$

$$v = \frac{dx}{dt} = 6t - 2$$

$$t_i = 2 \text{ s} \rightarrow 6 \times 2 - 2 = 10 \text{ m/s}$$

$$t_f = 3 \text{ s} \rightarrow 6 \times 3 - 2 = 16 \text{ m/s}$$

B) Find the acceleration at $t = 5$ s?

$$\vec{a} = \frac{dv}{dt} = 6$$

$$\vec{a}(t = 5 \text{ s}) = 6 \text{ m/s}^2$$

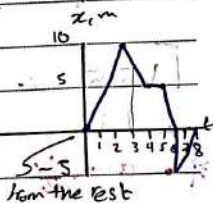
Q1) Find the average velocity

[1] 0 - 2 s

$$\bar{v} = \frac{x_f - x_i}{t_f - t_i} = \frac{10 - 0}{2 - 0} = +5 \text{ m/s}$$

[2] 2 s $\rightarrow$ 4 s

$$\bar{v} = \frac{5 - 10}{4 - 2} = -2.5 \text{ m/s}$$



3) $4s \rightarrow 5s?$

$$\bar{v} = \frac{5-5}{5-4} = \text{Zero}$$

4) $0 \rightarrow 7$

$$\bar{v} = \frac{-5-0}{7-0} = \frac{-5}{7} \text{ m/s}$$

Q.B) Find the average speed? متوسط السرعة

1) $0 \rightarrow 2s?$

$$\frac{\text{distance}}{\text{time}} = \frac{10}{2} = 5 \text{ m/s}$$

2) $2s \rightarrow 4s?$

$$\frac{5}{2} = 2.5 \text{ m/s}$$

3) $4s \rightarrow 5s?$

$$\frac{0}{1} = 0 \text{ m/s}$$

4) $0s \rightarrow 7s?$

$$\frac{10+5+0+5+5}{7} = \frac{25}{7} \text{ m/s}$$

Q.C) find the velocity at $t=1s?$ at 0, 2, 4, 5, 7, 8s?

$$\bar{v} = \text{slope} = \frac{x_f - x_i}{t_f - t_i} = \frac{10-2}{2-0} = 5 \text{ m/s}$$

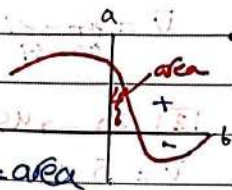
$$\bar{v} = 0 \text{ (Zero)}$$

$$[\text{W.m} \rightarrow \text{ie } \begin{matrix} \uparrow & \uparrow & \uparrow & \uparrow & \uparrow \\ 0.7s & 1.5s & 3s & 4.5s & 6s \end{matrix}]$$

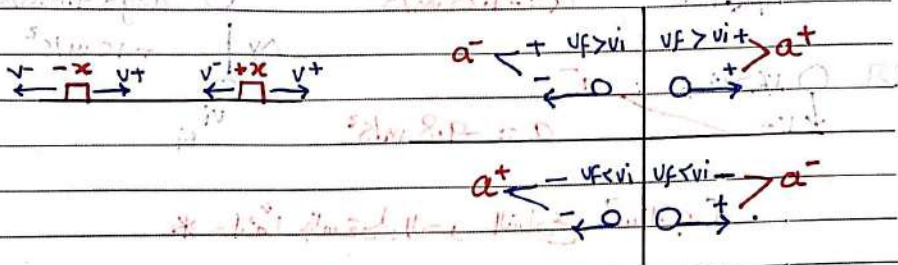
$$* a = \frac{dv}{dt} = \int_{t_i}^{t_f} dv = \int_{t_i}^{t_f} a \cdot dt$$

$$v_f - v_i = \Delta v = \int_{t_i}^{t_f} a \cdot dt$$

$$\Delta v = \text{area}$$



Motion in one dimension with constant acceleration.



Equations of motion for constant acceleration:

- $v_f = v_i + a \Delta t$
- $v_f^2 = v_i^2 + 2a \Delta x$
- $\Delta x = v_i \Delta t + \frac{1}{2} a \Delta t^2$

Q19 → 7 A jet plane

$v_i = 100 \text{ m/s}$, $a = -5 \text{ m/s}^2$, $v_f = 0$

1) $v_f = v_i + a \Delta t$

$0 = 100 - 5 \Delta t$

$+5 \Delta t = \frac{100}{5}$

$\Delta t = 20$

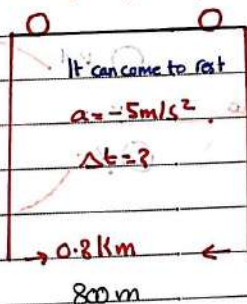
2) $v_f^2 = v_i^2 + 2a \Delta x$

$0^2 = (100)^2 + 2(-5 \Delta x)$

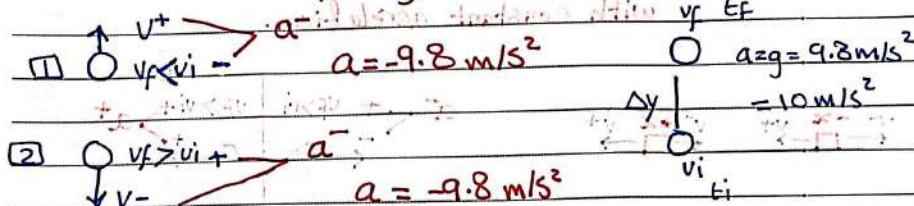
$= 10000 - 10 \Delta x$

$\frac{10 \Delta x}{10} = \frac{10000}{10}$

$\Delta x = 1000 > 800 \text{ m}$



free falling objects

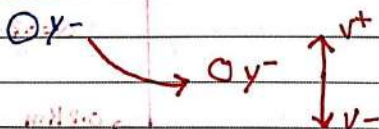


* دائماً بالسقوط الحر التسارع [سالبي]

$$\begin{aligned} [1] \quad v_f &= v_i - g \Delta t \\ [2] \quad v_f^2 &= v_i^2 - 2g \Delta y \\ [3] \quad \Delta y &= v_i \Delta t - \frac{1}{2} g \Delta t^2 \end{aligned}$$

$$\Delta y = y_f - y_i = 0$$

مرجعية



Confidential - Not for Release

$$g = -9.8 \approx 10$$
$$g = -10 \text{ m/s}^2$$

$\uparrow$ $a/g = -9.8 \text{ m/s}^2$
 $v_f < v_i$

$\uparrow$ $\downarrow$ $v_i = 8 \text{ m/s}^2$
 30m $\Delta T = ?$
 $\downarrow$ $\uparrow$ $v_f = ?$

$$v_i = -8 \text{ m/s}$$

② Find ΔT_2

$$\Delta y = v_i t - \frac{1}{2} g T^2$$

$$-30 = -8T - \frac{1}{2}(10)T^2$$

$$-30 = -8T - 5T^2$$

$$5T^2 + 8T - 30 = 0 \leftarrow \text{Mod } 5, 3$$

$$[t_1 = 1.77 \approx 1.8 \checkmark]$$

$$t_2 = -3.37 \text{ s}$$

* الزمن $\rightarrow ax^2 + bx + c = 0$

الزمن خالقنا العام .

$$= 5T^2 + 8T - 30 = 0$$

$t = 1.8$ ✓

$$t = \frac{-8 \pm \sqrt{(8)^2 - 4(5)(-30)}}{2(5)}$$

$$t = -3.4 \text{ s}$$

$$\underline{-30 = -8T - 5T^2}$$

1] find the velocity?

$$v_f = -20 \text{ m/s}$$

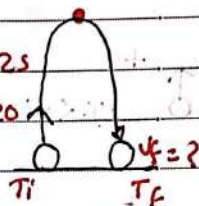
$$t_i = 2 \text{ s}$$

$$v_i = 20$$

2] find the velocity at the top point?

$$v_f = \text{Zero}$$

$$g = -9.8 \text{ m/s}^2$$



3] $\Delta T = ?$ 2x $\Delta x / v_i$

or

$$v_f = v_i - g \Delta T$$

$$-20 = 20 - 10T$$

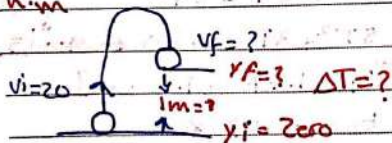
$$-20 - 20 = -10T$$

$$\frac{-40}{-10} = \frac{-10T}{-10}$$

$$T = 4 \text{ s}$$

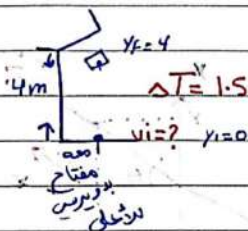
الشائع في هذه الحالة
لما الجسم يكون في شكل
O → مستقيم
Constant speed

h.m



$$\uparrow 19.5 \text{ m/s}^2 \quad \downarrow -19.5 \text{ m/s}^2$$

$$T =$$



1- find v_i ?

$$dy = v_i t + \frac{1}{2} g t^2$$

$$4 = v_i(1.5) - \frac{1}{2}(10)(1.5)^2$$

$$4 = 1.5 v_i - 11.25$$

$$1.5 v_i = 11.25 + 4$$

$$\frac{1.5 v_i}{1.5} = \frac{15.25}{1.5}$$

$$v_i = 10$$

2- find the velocity after 1.5s?

$$v_f = v_i - g \Delta t$$

$$v_f = 10 - (10)(1.5)$$

$$v_f = 10 - 15$$

$$v_f = -5 \text{ m/s}$$

$$v_f = -5 \text{ m/s} \quad (\text{تأخر})$$

3- Find the velocity at $y = 4 \text{ m}$?

* At $y = 4 \text{ m}$

after 1.5 s $\rightarrow -5 \text{ m/s}$

* At $y = 4 \text{ m}$

$\rightarrow +5 \text{ m/s}$ / -5 m/s تأخر

* وهو صاعد لأن
 أقل من 1.5s

CH3 → Vectors .

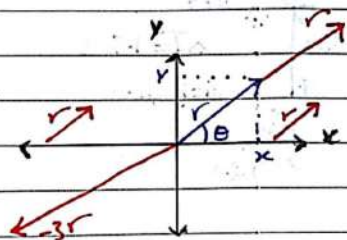
$$(x, y) = (r, \theta)$$

① إذا بضرب الـ r بـ 2 .

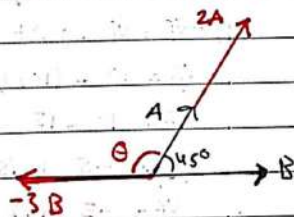
يصير الضعف بس زاوية ثلثها

② إذا بضرب الـ r بـ -3 .

نحسب الاتجاه وتصير 3 أمثاله



- If the angle between A and B 45°
Find the angle between $2A$ and $-3B$



$$180 = 45 + \theta$$

$$180 - 45 = \theta$$

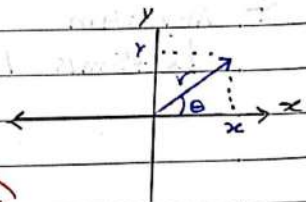
$$\theta = 135^\circ$$

$$* \sin \theta = \frac{y}{r}$$

$$y = r \sin \theta$$

$$* \cos \theta = \frac{x}{r}$$

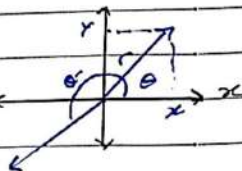
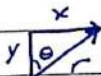
$$x = r \cos \theta$$



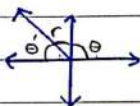
* الزاوية القريبة من المحاور
مهم جداً أخذ $\cos$

$$x = r \sin \theta$$

$$y = r \cos \theta$$



الربع الثاني



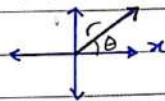
$$r = \sqrt{x^2 + y^2}$$

$$\theta' = \tan^{-1}\left(\left|\frac{y}{x}\right|\right)$$

above $-x$ -axis

$$\theta = 180 - \theta'$$

الربع الأول

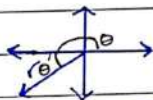


$$r = \sqrt{x^2 + y^2}$$

$$\tan \theta = \frac{y}{x} \rightarrow \theta \rightarrow \tan^{-1}\left(\left|\frac{y}{x}\right|\right)$$

$$\theta = \theta'$$

الربع الثالث



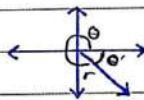
$$r = \sqrt{x^2 + y^2}$$

$$\theta' = \tan^{-1}\left(\left|\frac{y}{x}\right|\right)$$

below $-x$ -axis

$$\theta = 180 + \theta'$$

الربع الرابع



$$r = \sqrt{x^2 + y^2}$$

$$\theta' = \tan^{-1}\left(\left|\frac{y}{x}\right|\right) \text{ or } \theta' = \tan^{-1}\left(\frac{y}{x}\right)$$

below $+x$ -axis (أعطيني جوابا بالبال)

$$\theta = 360 - \theta'$$

$$Q_1: r = 5.5 \text{ m}, \theta = 240^\circ \quad x = ?, y = ?$$

$$[1] \quad x = r \cos 240 = 5.5 \cdot \cos 240$$

$$x = -2.75 \text{ m}$$

$$[2] \quad y = r \sin 240 = 5.5 \cdot \sin 240$$

$$y = -4.8 \text{ m}$$

$$(5.5 \text{ m}, 240^\circ) = (-2.75 \text{ m}, -4.8 \text{ m})$$

$$E_x = (x, y)$$

Find the magnitude and direction of the vector?

$$r = \sqrt{(2)^2 + (-4)^2} = r = \sqrt{20}$$

$$r = 2\sqrt{5}$$

* direction?

$$\theta' = \tan^{-1}\left(\frac{-4}{-2}\right)$$

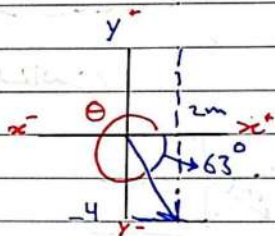
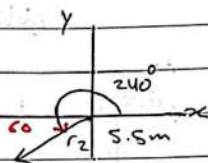
$$= \tan^{-1}(2)$$

$$= 63.4^\circ \checkmark$$

$$\theta = 360 - 63.4 = 296.6^\circ \checkmark$$

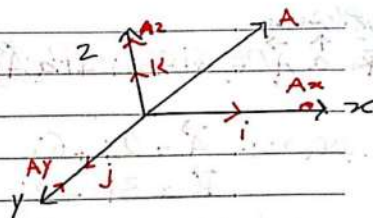
$$\theta = \tan^{-1}\left(\frac{-4}{-2}\right) = \tan^{-1}(2)$$

$$= -63.4^\circ \checkmark$$



* $|\mathbf{i}| = |\mathbf{j}| = |\mathbf{k}| = 1$ unit.

$\vec{A} = A_x \mathbf{i} + A_y \mathbf{j} + A_z \mathbf{k}$



Components of the vectors

* $A_x = A \cos \theta$

* $A_y = A \sin \theta$

* $\vec{A} = A_x \mathbf{i} + A_y \mathbf{j}$

$(A, \theta) = (A_x, A_y)$

* Find the components of vectors A?

$A_x??$, $A_y??$

* $A_x = A \cos 37^\circ = 10 \cos 37^\circ$
 $= A_x = 8 \text{ N}$

* $A_y = A \sin 37^\circ = 10 \sin 37^\circ$
 $= A_y = 6 \text{ N}$

$\vec{A} = 8\mathbf{i} + 6\mathbf{j}$

$\vec{A} = A_x \mathbf{i} + A_y \mathbf{j} + A_z \mathbf{k}$

$\vec{B} = B_x \mathbf{i} + B_y \mathbf{j} + B_z \mathbf{k}$

* $\vec{A} + \vec{B} = (A_x + B_x)\mathbf{i} + (A_y + B_y)\mathbf{j} + (A_z + B_z)\mathbf{k}$

* $\vec{A} - \vec{B} = (A_x - B_x)\mathbf{i} + (A_y - B_y)\mathbf{j} + (A_z - B_z)\mathbf{k}$

* $a\vec{A} = aA_x \mathbf{i} + aA_y \mathbf{j} + aA_z \mathbf{k}$

عدد عشري

"physics - CH3"

Q 20: $\vec{A} = 2\mathbf{i} + 6\mathbf{j}$

$\vec{B} = 3\mathbf{i} - 2\mathbf{j}$

find the mag, and dir.

(1) $\vec{A} + \vec{B}$?

$\vec{A} + \vec{B} = (2+3)\mathbf{i} + (6+(-2))\mathbf{j}$

$\vec{A} + \vec{B} = 5\mathbf{i} + 4\mathbf{j}$

* Mag = $|\vec{A} + \vec{B}| = \sqrt{5^2 + 4^2} = \sqrt{41} \text{ m}$

Dir:

* $\theta' = \tan^{-1}\left(\frac{4}{5}\right) = 38.6^\circ$

(2) $\vec{A} - \vec{B}$?

$\vec{A} - \vec{B} = (2-3)\mathbf{i} + (6-(-2))\mathbf{j}$

$\vec{A} - \vec{B} = -1\mathbf{i} + 8\mathbf{j}$

Mag = $\sqrt{(-1)^2 + (8)^2} = \sqrt{65}$

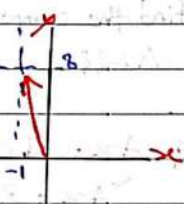
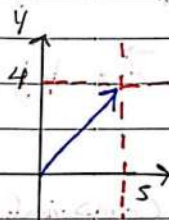
Dir:

* $\theta' = \tan^{-1}\left(\frac{8}{-1}\right) = 82.8^\circ$
above $\vec{x}$

$\theta = 180 - \theta'$

$180 - 82.8$

$= 97.2^\circ$



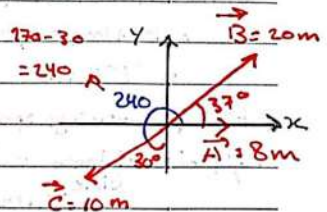
Ex, find the resultant vectors?

$$* \vec{A} = (8\mathbf{i} + 0\mathbf{j}) \text{ m}$$

$$* \vec{B} = (16\mathbf{i} + 12\mathbf{j}) \text{ m}$$

$$* \vec{C} = (-5\mathbf{j} + (-8.7)\mathbf{j}) \text{ m}$$

↓ $\vec{C}$ و $\vec{B}$ إلى $\vec{A}$ ↓



$$* B_x = B \cos 37 = 20 \cos 37 = 16 \text{ m}$$

$$B_y = B \sin 37 = 20 \sin 37 = 12 \text{ m}$$

$$* C_x = C \cos 240 = 10 \cos 240 = -5$$

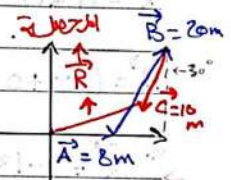
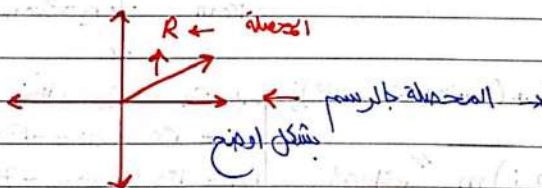
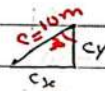
$$C_y = C \sin 240 = 10 \sin 240 = -8.7$$

∴ لإيجاد المحصلة $\vec{R}$

$$\vec{R} = \vec{A} + \vec{B} + \vec{C}$$

$$\vec{R} = (8 + 16 - 5)\mathbf{i} + (0 + 12 - 8.7)\mathbf{j}$$

$$= 19\mathbf{i} + 3.3\mathbf{j} \text{ m}$$

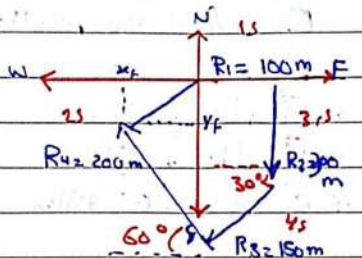


1) Find the distance?

$$\begin{aligned} \text{distance} &= r_1 + r_2 + r_3 + r_4 \\ &= 100 + 300 + 150 + 200 \\ &= 750 \text{ m} \end{aligned}$$

2) Find the average speed?

$$\begin{aligned} \text{Avg. speed} &= \frac{\text{distance}}{\text{time}} = \frac{750}{(1+3+4+2)} \\ &= 75 \text{ m/s} \end{aligned}$$



3) Find the displacement / Find the resultant vectors?

$$\text{displacement} : \Delta x i + \Delta y j = (x_f - x_i) i + (y_f - y_i) j$$

$$\vec{r}_1 = 100 i + 0 j$$

$$\vec{r}_2 = 0 j - 300 j$$

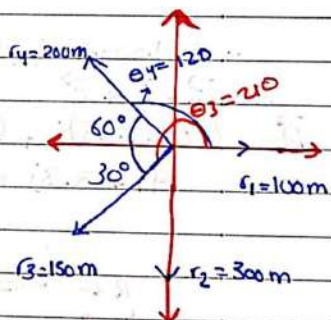
$$\vec{r}_3 = -130 i - 75 j$$

$$\vec{r}_4 = -100 i + 173 j$$

$$\vec{R} = \vec{r}_1 + \vec{r}_2 + \vec{r}_3 + \vec{r}_4$$

$$\vec{R} = (100 + 0 - 130 - 100) i + (0 - 300 - 75 + 173) j$$

$$\Rightarrow \vec{R} = (-130 i - 202 j) \text{ m}$$



4) Find the average velocity? / Find the magnitude

$$\vec{V} = \frac{\Delta \vec{R}}{\Delta t} = \frac{-130 i}{10} - \frac{202 j}{10}$$

$$= (-13 i - 20.2 j) \text{ m/s}$$

Q38, $\vec{A} = 6\mathbf{i} - 8\mathbf{j}$

$\vec{B} = -8\mathbf{i} + 3\mathbf{j}$

$\vec{C} = 26\mathbf{i} + 19\mathbf{j}$

* $a\vec{A} + b\vec{B} + \vec{C} = 0$

* find the value a and b?

$a\vec{A} = 6a\mathbf{i} - 8a\mathbf{j}$

$b\vec{B} = -8b\mathbf{i} + 3b\mathbf{j}$

$\vec{C} = 26\mathbf{i} + 19\mathbf{j}$

$(6a - 8b + 26)\mathbf{i} + (-8a + 3b + 19)\mathbf{j} = 0 = 0\mathbf{i} + 0\mathbf{j}$

$(6a - 8b + 26 = 0) \times 8 = 48a - 64b + 208 = 0$

$(-8a + 3b + 19 = 0) \times 6 = -48a + 18b + 114 = 0$

$$\begin{array}{r} -48a \\ -48a \end{array} = \begin{array}{r} -322 \\ -46 \end{array}$$

$$\boxed{b = 7}$$

* $6a - 8(7) + 26 =$

$6a - 56 + 26 = \frac{6a}{6} = \frac{+30}{6}$

$$\boxed{a = 5}$$

$a\vec{A} + b\vec{B} + \vec{C} = 5\mathbf{i} + 0\mathbf{j}$

$a\vec{A} + b\vec{B} + \vec{C} = 5\mathbf{i} + 3\mathbf{j}$

وإجابة

Q24 $\vec{A} = -8.7\mathbf{i} + 15\mathbf{j}$
 $\vec{B} = 13.2\mathbf{i} - 6.6\mathbf{j}$

* IF:

$$\vec{A} - \vec{B} + 3\vec{C} = 0$$

Find the vector $\vec{C} = ?$

$$3\vec{C} = \vec{B} - \vec{A}$$

$$\vec{C} = \frac{1}{3}(\vec{B} - \vec{A})$$

$$\vec{B} - \vec{A} = (13.2 - (-8.7))\mathbf{i} + (-6.6 - 15)\mathbf{j}$$

$$= 21.9\mathbf{i} - 21.6\mathbf{j}$$

$$\vec{C} = \frac{1}{3}(\vec{B} - \vec{A}) = \frac{1}{3}(21.9\mathbf{i} - 21.6\mathbf{j})$$

$$\boxed{\vec{C} = (7.3\mathbf{i} - 7.2\mathbf{j}) \text{ cm}}$$

* $\vec{A} = A_x\mathbf{i} + A_y\mathbf{j} + A_z\mathbf{k}$

find the magnitude of the vectors?

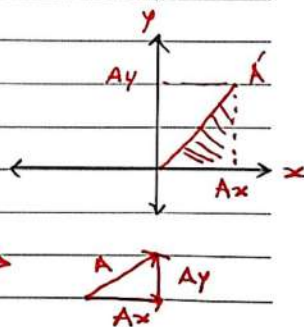
$$A = \sqrt{A_x^2 + A_y^2 + A_z^2}$$

* $\vec{A} = A_x\mathbf{i} + A_y\mathbf{j}$

$$\text{Mag} = 21$$

$$A = \sqrt{A_x^2 + A_y^2}$$

$$\text{dir} = \theta = \tan^{-1}\left(\left|\frac{A_y}{A_x}\right|\right)$$



physics

CH4 19000

5.nov.2020

$$\vec{V} = V_x \hat{i} + V_y \hat{j} + V_z \hat{k}$$

Magnitude -

$$V = \sqrt{V_x^2 + V_y^2 + V_z^2}$$

= Speed

$$\vec{V} = -5 \text{ m/s} = -5\hat{j} + 0\hat{k}$$

$$-5\hat{j} + 0\hat{k} + 0\hat{k}$$

speed = 5 m/s ← مغیر اشارہ

$$\text{speed} = \sqrt{(-5)^2 + (0)^2 + (0)^2}$$
$$= \sqrt{25} = 5 \text{ m/s}$$

Motion in 2 Dimension

	1D	2D
Position:		
Distance	Distance	Distance
Displacement	Δx	$\Delta x_i + \Delta y_j = \Delta R$
velocity		
1- Average speed	$\frac{\text{distance}}{\text{time}}$	$\frac{\text{distance}}{\text{time}}$
2- Average velocity	$\vec{v} = \frac{\Delta x}{\Delta t}$	$\vec{v} = \frac{\Delta x_i}{\Delta t} + \frac{\Delta y_j}{\Delta t}$
3- Instantaneous velocity	$\vec{v} = \frac{dx}{dt}$	$\vec{v} = \frac{dx}{dt}i + \frac{dy}{dt}j$
acceleration		
1- average acceleration	$\vec{a} = \frac{\Delta v}{\Delta t}$	$\vec{a} = \frac{\Delta v_x}{\Delta t}i + \frac{\Delta v_y}{\Delta t}j$
2- Instantaneous acceleration	$\frac{dv}{dt} \text{ or } \frac{d^2x}{dt^2}$	$\frac{dv_x}{dt}i + \frac{dv_y}{dt}j$ or $\frac{d^2x}{dt^2}i + \frac{d^2y}{dt^2}j$

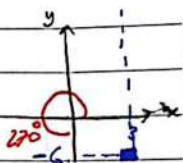
"physics"

8. nov. 2020

Q6, $\vec{r} = (3i - 6t^2j) \text{ m}$

* $t = 1\text{s}$, find the position?

$$\begin{aligned}\vec{r}(t=1\text{s}) &= 3i - 6(1)^2j \\ &= (3i - 6j) \text{ m}\end{aligned}$$



* find the velocity?

$$\vec{v} = \frac{d\vec{r}}{dt} = \frac{dx}{dt}i + \frac{dy}{dt}j$$

$$= 0j - 12tj$$

$$\vec{v}(t=1\text{s}) = -12 \text{ m/s}$$

* find the speed?

$$\text{speed} = 12 \text{ m/s}$$

* find the acceleration?

$$\vec{a} = \frac{dv_x}{dt}i + \frac{dv_y}{dt}j$$

$$0j - 12j$$

$$\vec{a}(t=1\text{s}) = -12j \text{ m/s}^2$$

* find the magnitude?

$$a = \sqrt{0^2 + 12^2 + 0^2}$$

$$= 12 \text{ m/s}^2$$

* find the average velocity from $t=1\text{s}$ to $t=3\text{s}$?

$$\vec{v} = \frac{\Delta x}{\Delta t}i + \frac{\Delta y}{\Delta t}j$$

$$= \frac{3-3}{2}i + \frac{-54-(-6)}{2}j = 0i - 24j \text{ m/s}$$

$$x_i = 3\text{m}, x_f = 3\text{m}$$

$$y_i = -6\text{m}, y_f = -54\text{m}$$

$$\vec{v} = 0j - 24j \text{ m/s}$$

$$t_i = 1\text{s} \rightarrow x_i = 3\text{m} \rightarrow x_f = 3\text{m}$$

$$t_f = 3\text{s} \rightarrow x_f = 3\text{m} \rightarrow y_f = -6 \cdot 3^2 = -54\text{m}$$

$$r = 3tj + (8t - 16t^2)j$$

* Find the position when the object change direction at y-axis?

$$v_y = \frac{dy}{dt} = \text{zero}$$

$$8 - 32t = 0$$

$$t = \frac{8}{32} = 0.25s$$

$$\vec{r}(t=0.25s) = 3(0.25)j + (8(0.25) - 16(0.25)^2)j$$

$$\vec{r} = (0.75j + 1j)m \leftarrow \text{بالربع الأول}$$

2D motion with constant

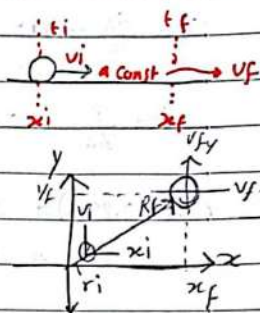
$$v_f = v_i + a \Delta t$$

$$v_f^2 = v_i^2 + 2a\Delta x$$

$$\Delta y = v_i \Delta t + \frac{1}{2} a \Delta t^2$$

$$\vec{v} = v_x \hat{i} + v_y \hat{j}$$

$$\text{Speed} = \sqrt{v_x^2 + v_y^2}$$



Q8 at the

$$x_i = y_i = \text{zero}$$

$$\vec{a} = 3 \hat{j} \text{ m/s}^2$$

$$\vec{a} = (0\hat{i} + 3\hat{j}) \text{ m/s}^2$$

$$\vec{v}_i = (5\hat{i} + 0\hat{j}) \text{ m/s} = 5 \hat{i} \text{ m/s}$$

Find the coordinate and speed

at the particle at $t=2\text{s}$?

x-axis -

$$x_i = \text{zero} / a_x = 0 \text{ m/s}^2 / v_i = 5 \text{ m/s} / \Delta t = 2\text{s}$$

$$\Delta x = x_f - x_i = v_{ix} \Delta t + \frac{1}{2} a_x \Delta t^2$$

$$x_f - 0 = 5(2) + \frac{1}{2}(0)(2)^2$$

$$x_f = 10 \text{ m}$$

y-axis -

$$y_i = \text{zero} / v_i = \text{zero} / a_y = 3 \text{ m/s}^2 / \Delta t = 2\text{s}$$

$$\Delta y = y_f - y_i = v_{iy} \Delta t + \frac{1}{2} a_y \Delta t^2$$

$$y_f - 0 = 0(2) + \frac{1}{2}(3)(2)^2$$

$$y_f = 6 \text{ m}$$

$$\vec{r} = (10\hat{i} + 6\hat{j}) \text{ m}$$

$$\begin{aligned} \textcircled{1} \quad & \begin{cases} v_{fx} = v_{ix} + a_x \Delta t \\ v_{fy} = v_{iy} + a_y \Delta t \end{cases} \\ \textcircled{2} \quad & \begin{cases} v_{fx}^2 = v_{ix}^2 + 2a_x \Delta x \\ v_{fy}^2 = v_{iy}^2 + 2a_y \Delta y \end{cases} \\ \textcircled{3} \quad & \begin{cases} \Delta x = v_{ix} \Delta t + \frac{1}{2} a_x \Delta t^2 \\ \Delta y = v_{iy} \Delta t + \frac{1}{2} a_y \Delta t^2 \end{cases} \end{aligned}$$

1* Magnitude =

$$r = \sqrt{(10)^2 + (6)^2}$$

$$r = \sqrt{136} \text{ m}$$

2. final velocity.

• x-axis

$$v_f x = v_i x + a_x \Delta t$$

$$v_f x = 5 + 0(2)$$

$$v_f x = 5 \text{ m/s}$$

• y-axis

$$v_f y = v_i y + a_y \Delta t$$

$$v_f y = 0 + 3(2)$$

$$v_f y = 6 \text{ m/s}$$

$$\vec{v}_f = (5\hat{i} + 6\hat{j}) \text{ m/s}$$

3. Speed =

$$= \sqrt{(5)^2 + (6)^2}$$

$$= \sqrt{61} \text{ m/s}$$

Q5: $\vec{v}_i = (4\hat{i} + 1\hat{j}) \text{ m/s}$ / $\vec{r}_i = (10\hat{i} - 4\hat{j}) \text{ m}$

$\Delta t = 20 \text{ s}$ / $\vec{v}_f = (20\hat{i} - 5\hat{j}) \text{ m/s}$

① What are the components of the acceleration? $\Delta x = ?$ $\Delta y = ?$

x-axis

$\vec{v}_i x = 4 \text{ m/s}$ / $x_i = 10 \text{ m}$ / $\Delta t = 20 \text{ s}$ / $\vec{v}_f x = 20 \text{ m/s}$ / $a_x = ?$

$$v_f x = v_i x + a_x \Delta t$$

$$20 = 4 + a_x \cdot 20$$

$$20 = 4 + 20 a_x$$

$$\frac{16}{20} = 20 a_x$$

$$a_x = 0.8 \text{ m/s}^2$$



y-axis

$$\vec{v}_y = 1 \text{ m/s} / y_i = -4 \text{ m} / \Delta t = 20 \text{ s} / v_{fy} = -5 \text{ m/s} / a_y$$

$$v_{fy} = v_{iy} + a_y \Delta t$$

$$-5 = 1 + a_y \cdot 20$$

$$-5 = 1 + 20 a_y$$

$$\frac{-6}{20} = \frac{20 a_y}{20}$$

$$a_y = -0.3 \text{ m/s}^2$$

[2] find the acceleration?

$$\vec{a} = a_x \hat{i} + a_y \hat{j}$$

$$\vec{a} = (0.8 \hat{i} - 0.3 \hat{j}) \text{ m/s}^2$$

[3] find the magnitude of the acceleration?

$$a = \sqrt{(0.8)^2 + (-0.3)^2}$$

$$= 0.85 \text{ m/s}^2$$

[4] find the direction of the acceleration?

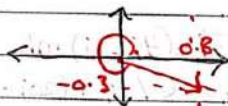
$$\theta = \tan^{-1}\left(\frac{0.3}{0.8}\right) = 20.5$$

↻ below x-axis +

$$\text{or} = 360 - 20.5$$

$$= 339.5$$

$$\tan^{-1}\left(\frac{a_y}{a_x}\right) = \tan^{-1}\left(\frac{-0.3}{0.8}\right) = -20.5$$



projectile motion.

$$v_{ix} = v_i \cos \theta$$

$$v_{iy} = v_i \sin \theta$$

* y-axis = free falling object.

$$v_{fy} = v_{iy} - g \Delta t$$

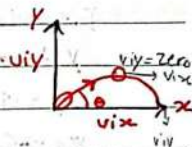
$$v_{fy}^2 = v_{iy}^2 - 2g \Delta y$$

$$\Delta y = v_{iy} \Delta t - \frac{1}{2} g \Delta t^2$$

* x-axis = constant speed

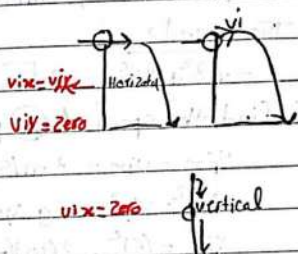
$$v_{fx} = v_{ix}$$

$$\Delta x = v_{ix} \Delta t$$



$$\Delta t =$$

x & y solutions



Ex 1 Find the speed of the following cases?

(i) at the top point?

$$v_{ix} = v_i \cos 37^\circ = 10 \cos 37^\circ = 8 \text{ m/s}$$

$$v_{iy} = v_i \sin 37^\circ = 10 \sin 37^\circ = 6 \text{ m/s}$$

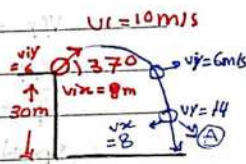
$$v_{fx} = v_{ix} = 8 \text{ m/s}$$

$$v_{fy} = 0$$

$$\vec{v}_f = (8\hat{i} + 0\hat{j}) \text{ m/s}$$

$$\vec{v}_f = 8\hat{i} \text{ m/s}$$

$$\text{Speed} = 8 \text{ m/s}$$



② find the speed after 2s?

$$v_{fx} = v_{ix} = 8 \text{ m/s} \quad \leftarrow \text{راجع للنقطة الاولى}$$

y-axis

$$v_{fy} = v_{iy} - g \Delta t$$

$$v_{fy} = +6 - 10(2)$$

$$v_{fy} = -14 \text{ m/s}$$

The velocity?

$$\vec{v}_f = (8\mathbf{i} - 14\mathbf{j}) \text{ m/s}$$

The Speed?

$$= \sqrt{8^2 + (-14)^2} = 2\sqrt{65} = 16 \text{ m/s}$$

③ find the speed at (A) point?

$$v_{fx} = v_{ix} = 8 \text{ m/s}$$

$$v_{fy}^2 = v_{iy}^2 - 2g\Delta y$$

$$v_{fy}^2 = (6)^2 - 2(10)(-36-0)$$

$$v_{fy}^2 = 36 + 600$$

$$v_{fy} = \sqrt{636}$$

$$v_{fy} = -25.2$$

$$\vec{v}_f = (8\mathbf{i} - 25.2\mathbf{j}) \text{ m/s}$$

$$\text{Speed} = \sqrt{(8)^2 + (-25.2)^2}$$

$$= 26.4 \text{ m/s}$$

Q₁ Find the initial velocity?

$$* v_{ix} = v_i, \quad v_{iy} = \text{zero}$$

$$* \Delta x = v_{ix} \cdot \Delta t$$

$$\Delta y = y_f - y_i = v_{iy} \Delta t - \frac{1}{2} g \Delta t^2$$

$$0.86 - 0 = 0 - \frac{1}{2} (10) \Delta t^2$$

$$\Delta t = \sqrt{0.86}$$

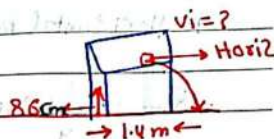
$$\boxed{\Delta t = 0.41 \text{ s}}$$

$$\Delta x = v_{ix} \cdot \Delta t$$

$$\frac{1.4}{0.41} = \frac{v_{ix} \cdot 0.41}{0.41}$$

$$v_{ix} = 3.4 \text{ m/s}$$

$$v_{ix} = \boxed{v_i = 3.4 \text{ m/s}}$$



Q₂ Find the final velocity?

$$v_{fy} = v_{iy} - g \Delta t$$

$$= 0 - 10(0.41)$$

$$\boxed{v_{fy} = -4.1 \text{ m/s}}$$

$$\text{" } \vec{v_f} = (3.4\hat{i} - 4.1\hat{j}) \text{ m/s. "}$$

Q₁ Find the initial velocity?

$$v_i = v_{ix}, \quad v_{iy} = \text{zero}$$

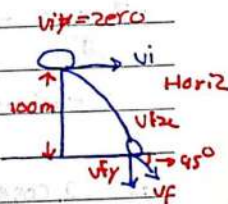
y-axis

$$v_{fy}^2 = v_{iy}^2 - 2g(y_f - y_i)$$

$$= 0 - 2(10)(-100 - 0)$$

$$v_{fy} = \sqrt{2000} = 44.7 \text{ m/s} = v_{fx}$$

$$\text{" } v_{ix} = v_{fx} = 44.7 \text{ m/s "}$$



$$\tan 45 = 1$$

$$v_{fx} \cdot \left(\frac{v_{fy}}{v_{fx}} \right) = 1(v_{fx})$$

$$v_{fy} = v_{fx}$$

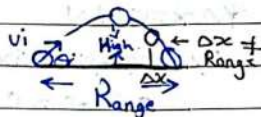
$$\text{" } v_{fx} = v_{fy} \text{"}$$

$$v_{ix} = v_{fx}$$

* Horizontal range and maximum height of projectile

$$R = \frac{v_i^2 \cdot \sin 2\theta_i}{g}$$

$$H = \frac{v_i^2 \cdot \sin^2 \theta_i}{2g}$$



$$* \sin(2\theta) = 2 \sin \theta \cos \theta$$

$$* \theta_i = \frac{\pi}{4} \rightarrow R = \frac{v_i^2}{g} \rightarrow \sin 2\left(\frac{\pi}{4}\right) = 1$$

$$\rightarrow H = \frac{v_i^2 \cdot \left(\frac{1}{\sqrt{2}}\right)^2}{2g} = \frac{v_i^2}{4g}$$

$$* \theta_i = 90^\circ = \frac{\pi}{2} \rightarrow R = \text{Zero} \quad \text{if } \theta_i = 90^\circ \Rightarrow \sin 2\theta_i = 0$$

$$\rightarrow H = \frac{v_i^2}{2g} \rightarrow \sin^2(90^\circ) = 1$$

$$Q: R = 3H$$

Find θ_i ?

$$R = 3H$$

$$\frac{v_i^2 \cdot \sin 2\theta}{g} = 3 \left(\frac{v_i^2 \cdot \sin^2 \theta_i}{2g} \right)$$

$$2 \sin \theta \cos \theta = \frac{3 \cdot \sin^2 \theta_i}{2}$$

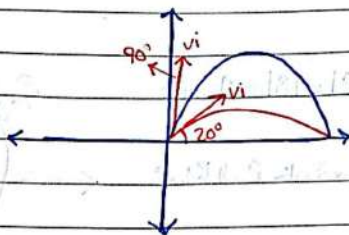
$$= 2 \cos \theta_i = \frac{3 \sin \theta_i}{2}$$

$$= \frac{\sin \theta_i}{\cos \theta_i} = \frac{3}{2}$$

$$= \tan \theta_i = \frac{3}{2}$$

$$\tan^{-1}\left(\frac{3}{2}\right) = 53.1$$

$$" \theta_i = 53.1^\circ "$$



* الزاوية ومتممة الزاوية الـ $Range$ اهم واحد

$$Range\ 20^\circ = Range\ 70^\circ$$

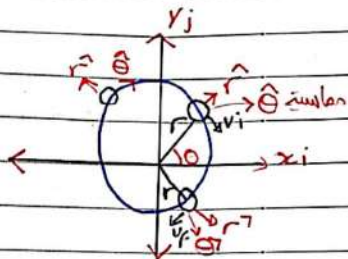
الزاوية $\nearrow$

متتممة الزاوية $\nearrow$

Circle motion, (acceleration).

$$|\hat{i}| = |\hat{j}| = |\hat{k}| = |\hat{r}| = |\hat{\theta}| = 1 \text{ unit}$$

"انما الـ $\hat{r}$ خارجة عن الدائرة طارئة على الدائرة"

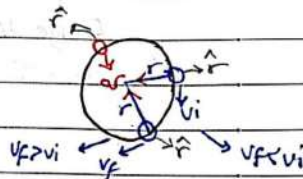


$$|v_i| = |v_f|, \text{ Constant speed}$$

Change direction = a_r

a_r : radial acceleration

$$[a_r = \frac{v^2}{r}] \Rightarrow [a_r = -\frac{v^2}{r} \hat{r}]$$



الحركة الدائرية:

Constant speed $\neq$ zero

السرعة المتغيرة

Constant speed = zero

a_r $\leftarrow$ داخل الدائرة

$\hat{r}$ $\leftarrow$ خارج الدائرة

a_r و $\hat{r}$ متضادان

$$* v = \frac{\text{dis}}{\text{time}}$$

$$\vec{v} = \frac{2\pi r}{T}, T: \text{period}$$

$$\vec{v} = \frac{(2\pi r)}{T} \hat{\theta}, T: \text{total time}$$

$$② v_i \neq v_f$$

$$a_r = \frac{v^2}{r}$$

$$a_t = \frac{dv}{dt}$$

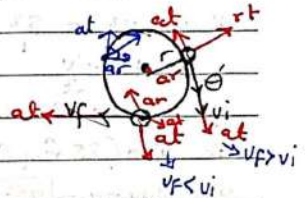
Tangential acceleration.

[1] $|v_i| = |v_f|$

$a_r = \frac{v^2}{r}$

$\vec{a} = -\frac{v^2}{r} \hat{r}$

$v = 2\pi r / T$ (الدورات)
 $\frac{v}{T} = \frac{2\pi r}{T^2}$



[2] $|v_f| \neq |v_i|$

$a_r = \frac{v^2}{r} \rightarrow \vec{a}_r = -\frac{v^2}{r} \hat{r}$

$a_t = \text{tangential acceleration} = \frac{dv}{dt} \hat{\theta}$

$\frac{dv}{dt} = \frac{v_f - v_i}{t} \rightarrow \frac{v_f - v_i}{t}$

* Total acceleration $\vec{a} = \vec{a}_r + \vec{a}_t$

$\vec{a} = \frac{v^2}{r} \hat{r} + \frac{dv}{dt} \hat{\theta}$

* $\vec{a} = -\frac{v^2}{r} \hat{r} + \frac{dv}{dt} \hat{\theta}$

Magn $= \sqrt{a_r^2 + a_t^2}$

Dir $= \theta = \tan^{-1} \left(\frac{a_t}{a_r} \right)$

size $\phi = \tan^{-1} \left(\frac{a_t}{a_r} \right)$

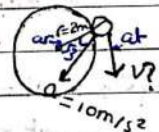


* Ex, Find the radial and tangential acceleration and the velocity at this moment?

$a_r = \frac{v^2}{r}$

$G = \frac{v^2}{r}$

$v = \sqrt{6.2} = \sqrt{12} \text{ m/s}$



$\cos 53 = \frac{a_r}{a} \rightarrow \frac{0.6}{10} = \frac{a_r}{a}$
 $\sin 53 = \frac{a_t}{a} \rightarrow \frac{0.8}{10} = \frac{a_t}{a}$
 $a_r = 6 \text{ m/s}^2$
 $a_t = 8 \text{ m/s}^2$

Total acceleration $= a$

11 $ar = ?? / at = ??, a = ??$

* $ar = \frac{v^2}{r} = \frac{5^2}{1} = 25 \text{ m/s}^2$

* $at = \frac{dv}{dt}$

* $at = g = 9.8 \text{ m/s}^2$

* $\vec{a} = (25\hat{r} + 9.8\hat{\theta}) \text{ m/s}^2$

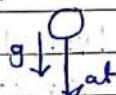
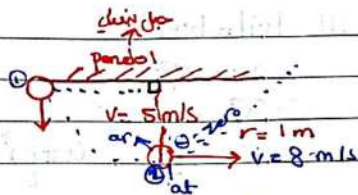
* $\text{Mag} = a = \sqrt{(25)^2 + (9.8)^2} = 26.8 \text{ m/s}^2$

$\text{Dir} = \theta \text{ s } \frac{at}{ar}$

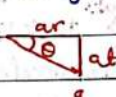
$\theta = \tan^{-1}\left(\frac{at}{ar}\right)$

$= \tan^{-1}\left(\frac{9.8}{25}\right)$

$= 21.4^\circ$



$at = g = 9.8 \text{ m/s}^2$



10

12 $ar = \frac{v^2}{r} = \frac{8^2}{1} = 64 \text{ m/s}^2$

$\vec{ar} = -64\hat{r} \text{ m/s}^2$

$at = \text{Zero}$ ← $\text{ميراثان كمالا تقيس (الفرق) ... لكن في بين السرعة والتسارع بالتزاوية}$

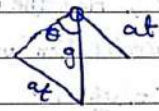
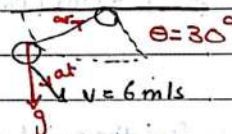
$\vec{a} = -64\hat{r} \text{ m/s}^2, +64\hat{j} \text{ m/s}^2$

$ar = \frac{v^2}{r} = \frac{6^2}{1} = 36 \text{ m/s}^2$

$\vec{ar} = -36\hat{r} \text{ m/s}^2$

$at = 4.9 \text{ m/s}^2$

$\vec{a} = -36\hat{r} + 4.9\hat{\theta} \text{ m/s}^2$



$at = 9.8 \sin 90^\circ = 9.8 \text{ m/s}^2$

$at \text{ s } 9.8 \sin 0 = \text{Zero}$

$\sin \theta = \frac{at}{g}$

$at = \sin \theta \cdot g$

السرعة والتسارع بالتزاوية

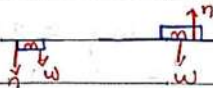
$at = 9.8 \cdot \sin 30$

$at = 4.9 \text{ m/s}^2$

The laws of motion

* W: weight ← $\vec{W}$

$$W = m \cdot g$$



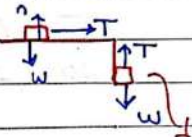
* N: normal force ← $\vec{N}$

N: normal force

* T: tension



T: tension



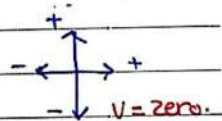
□ Equilibrium ← حالة التوازن ← $\vec{F} = 0$

□ V = zero



* $\vec{F} = 0$ ← حالة التوازن ← $\vec{F} = 0$

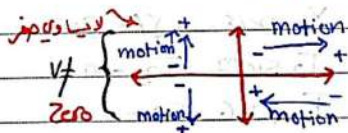
$$\vec{F} = 0 \rightarrow \sum F_x = 0 \rightarrow \sum F_y = 0$$



[2] $v_i = v_f$ (constant speed).

$$\sum F = 0$$

$$\sum F_x = 0 \rightarrow \sum F_y = 0$$



[3] $v_i \neq v_f$ (constant acceleration).

$$\sum \vec{F} = m \vec{a} \rightarrow \sum F_x = m a_x \rightarrow \sum F_y = m a_y$$

$$F_{12} = F_{21}$$

المotion ← $\vec{a}$

المotion ← $\vec{a}$

المotion ← $\vec{a}$

المotion ← $\vec{a}$

* Find the tension?

$$W = mg = 2 \times 10$$

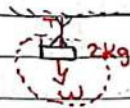
$$W = 20 \text{ N}$$

$$* Y\text{-axis} = \sum F_y = \text{Zero}$$

$$T - W = \text{Zero}$$

$$T = 20$$

$$20 = 20 \text{ N}$$

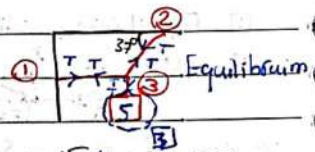


١- T الصاعد (الشد) جاذب الكتلة ويصير
٢- اما T الهازل وجاذب عاكف، ما بهن

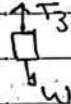
$$W = mg = 5 \times 10 = 50 \text{ N}$$

$$Y\text{-axis} = \sum F_y = \text{Zero}$$

$$T - W = 0 \Rightarrow T_3 = W = 50$$



* كل جسم متوازن
في حالة متزنة



$$Y\text{-axis} \rightarrow \sum F = \text{Zero}$$

$$T_2 \sin 37 - T_3 = 0$$

$$T_2 \cdot 0.6 - 50 = 0$$

$$T_2 = \frac{50}{0.6}$$

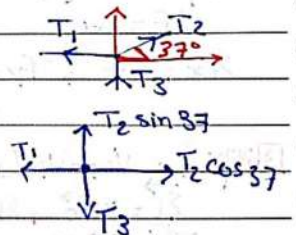
$$T_2 = 83.3 \text{ N}$$

$$X\text{-axis} \rightarrow \sum F_x = \text{Zero}$$

$$T_2 \cos 37 - T_1 = 0$$

$$83.3 \times 0.8 - T_1 = 0$$

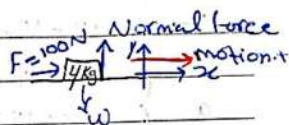
$$T_1 = 66.7 \text{ N}$$



* Find the weight and normal force tension and acceleration?

$$\square W = mg = 4 \times 10$$

$$W = 40 \text{ N}$$



y-axis $\rightarrow \Sigma F = 0$

$$N - W = 0$$

$$N = W = 40$$

x-axis $\rightarrow m \cdot a_x$ $a = a_x = \overset{\text{total}}{T} \cdot a$ $a_x = 0$ $a_y = 0$

$$+F = ma$$

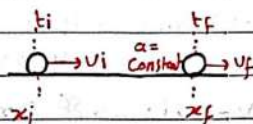
$$100 = 4a$$

$$a = +25 \text{ m/s}^2$$

✓ yes motion is not just a guess

The laws of motion.

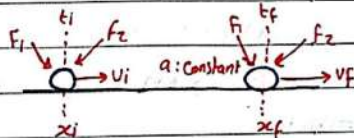
$$\left. \begin{array}{l} \Delta x \\ v \\ a \\ \Delta t \end{array} \right\} \begin{array}{l} v_f = v_i + at \\ v_f^2 = v_i^2 + 2a\Delta t \\ \Delta x = v_i \Delta t + \left(\frac{1}{2}\right)a\Delta t^2 \end{array}$$



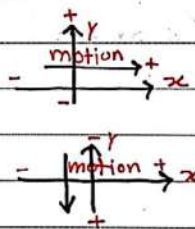
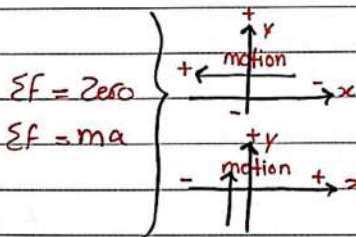
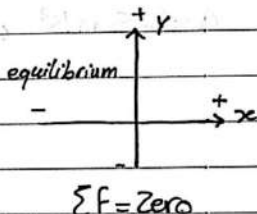
$v = 0 \rightarrow \text{Equilibrium} \rightarrow \Sigma F = \text{Zero}$

$v_f = v_i \rightarrow \text{Constant speed} \rightarrow \Sigma F = \text{Zero}$

$v_f \neq v_i \rightarrow \text{Constant accel} \rightarrow \Sigma F = ma$



إذا كان الجسم متزن فهو للأعلى فهو موجب ،
وإذا كان الجسم متزن فهو للأسفل فهو سالب ،
وإذا كان (جسم متزن) فهو لليمين فهو موجب ،
وإذا كان (جسم متزن) فهو لليسار فهو سالب .



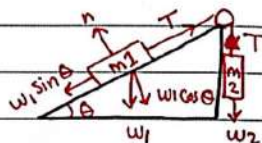
$\Sigma F = \text{Zero} , \Sigma F = ma \quad \vec{F}_{12} = -\vec{F}_{21}$

• weight : w

$w = mg$

• Normal force : n

• Tension : T



Ex, Find the weight, the normal force, tension and acceleration in the following cases? (Frictionless)

1) $w = mg = 10 \times 10 = 100 \text{ N}$

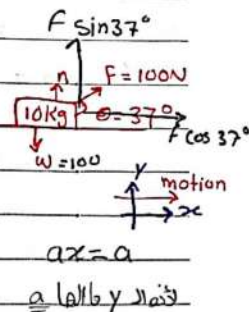
* y -axis $\Rightarrow \Sigma F_y = \text{zero}$

$n + F \sin 37^\circ - w = 0$

$n + 100(\sin 37^\circ) - 100 = 0$

$n + 60 - 100 = 0$

$n = 40 \text{ N}$



$ax = a$

a along y axis

* x -axis $\Rightarrow \Sigma F_x = ma$

$F \cos 37^\circ = ma$

$100(\cos 37^\circ) = 10a$

$80 = 10a$

$a = 8 \text{ m/s}^2$ ✓ *olzi motion 11 qoljöl*

2) $w = mg = 5 \times 10 = 50 \text{ N}$

* y -axis $\Rightarrow \Sigma F_y = \text{zero}$

$n - w \cos 37^\circ = 0$

$n = 50 \cdot 0.8 = 40 \text{ N}$

5 yiliclar 100 N qoljöl w

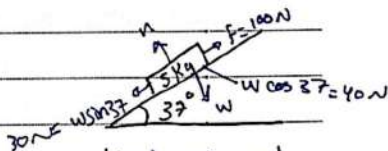
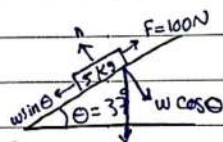
* x -axis $\Rightarrow \Sigma F_x = ma$

$F - w \sin 37^\circ = ma$

$100 - 50 \cdot 0.6 = 5a$

$\frac{70}{5} = 5a$

$a = 14 \text{ m/s}^2$



$40 \text{ N} = y$ 11, *uzerde*

$30 \text{ N} = x$ 11, *uzerde*

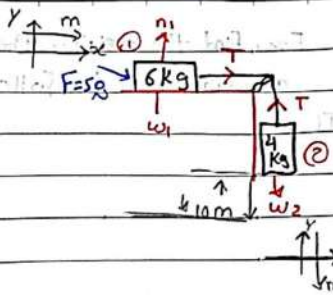
x -axis $\rightarrow 50 \sin 37^\circ = 30 \text{ N}$

y -axis $\rightarrow 50 \cos 37^\circ = 40 \text{ N}$

$$* w_1 = m_1 g_1$$

$$* = 6 \times 10 = 60 \text{ N}$$

$$* w_2 = 4 \times 10 = 40 \text{ N}$$



for mass 1 ① y -axis $\Rightarrow \Sigma F_y = \text{zero}$

$$n_1 - w_1 = 0$$

$$n_1 = w_1 = 60 \text{ N}$$

$$x\text{-axis} \Rightarrow \Sigma F_x = m_1 a$$

$$T = 6a$$

$$T = 6 \times 4$$

$$T = 24 \text{ N}$$

for mass 2 ② y -axis $\Rightarrow \Sigma F_y = m_2 a$

$$w_2 - T = m_2 a$$

$$40 - T = 4a$$

$$T = 6a$$

$$40 - T = 4a +$$

$$= 40 - 10a \Rightarrow \boxed{a = +4 \text{ m/s}^2}$$

* Find the final velocity?

$$v_f^2 = v_i^2 + 2a \Delta y$$

$$v_f^2 = 0 + 2(4)(10)$$

$$v_f = \sqrt{80} \text{ m/s}$$

$$v_f = 4\sqrt{5} \text{ m/s}$$

$$* v_f^2 = v_i^2 + 2a \Delta y$$

$$0 + 2(-4)(-10-0)$$

$$v_f = \sqrt{80} = 4\sqrt{5} \text{ m/s} \leftarrow y\text{-axis with } \downarrow$$

$$v_i = 20 \text{ m/s} \leftarrow 1.1 \uparrow$$

$$\vec{a} = 4 \text{ m/s}^2 \quad 10 \text{ m}$$

$$\downarrow$$

* Find the acceleration ?, N_{12} ?

$$\textcircled{1} \Sigma F = M_{\text{total}} \cdot a$$

$$\Sigma F = (M_1 + M_2) a$$

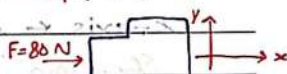
$$80 = (6+4) a$$

$$80 = 10 a$$

$$a = 8 \text{ m/s}^2$$



↓ الخيط حسب واحد



$$\rightarrow \Sigma F = M_{\text{total}} \cdot a$$

$$\textcircled{2} \Sigma F_x = m_1 a \leftarrow \text{الحجم الأول}$$

$$F - N_{21} = m_1 a$$

$$80 - N_{21} = 4(8)$$

$$80 - N_{21} = 32$$

$$80 - 32 = N_{21}$$

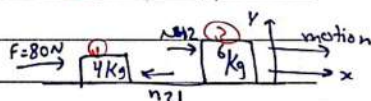
$$N_{21} = 48 \text{ N} \leftarrow N_{21} = N_{12}$$

$$\rightarrow \Sigma F = (M_1 + M_2) a$$

$$a \text{ حسب واحد} \rightarrow 80 = (6+4) a$$

$$80 = 10 a$$

$$a = 8 \text{ m/s}^2 \leftarrow \text{قيمة الـ } a$$



③ x-axis

$$\Sigma F_x = m_2 a \leftarrow \text{الحجم الثاني}$$

$$N_{12} = m_2 a$$

$$N_{12} = 6 \times 8$$

$$N_{12} = 48 \text{ N} \leftarrow N_{12} = N_{21} \leftarrow \text{الشئ على انوار نفس القيمة}$$

قوة دفع جسم إلى اليمين N_{12}

قوة دفع جسم إلى اليمين N_{21}

* y-axis $\leftarrow$ Normal force + عليم الوزن

* x-axis

$$\Sigma F_x = m_{total} \cdot a$$

$$f \cos 53 - w \sin 53 = 10 + (2+8)a$$

$$100 \cos 53 - 100 \sin 53 = 10a$$

$$60 - 80 = 10a$$

$$-20 = 10a$$

↓ motion ↓ $a = -2 \text{ m/s}^2$ ← direction ↓

x-axis ← direction ↓

$$\Sigma F_x = m_1 a$$

$$+f \cos 53 - w_1 \sin 53 - N_{21} = M_1 a$$

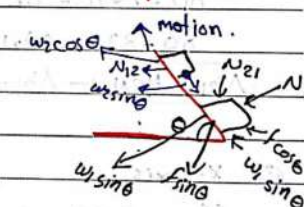
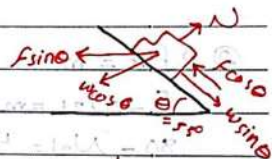
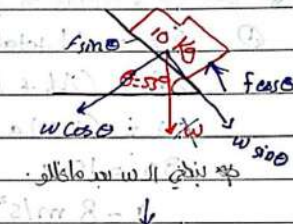
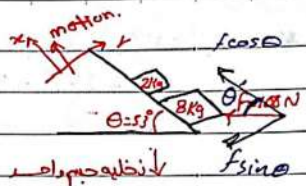
$$(100 \cdot 0.6) - (80 \cdot 0.8) - N_{21} = 8(-2)$$

$$60 - 64 - N_{21} = -16$$

$$-4 - N_{21} = -16$$

$$-4 + 16 = N_{21}$$

$$\downarrow N_{21} = +12 \text{ N} = N_{12} \checkmark$$



Find the Normal force, accel, and N_{12} , N_{23} ? h.w

① $x = a$ axis

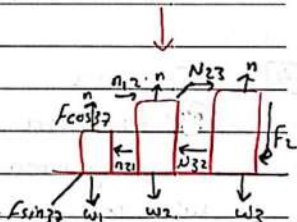
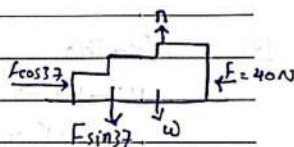
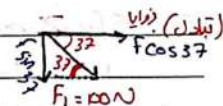
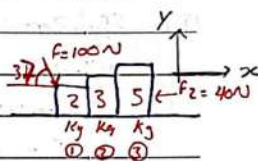
$$F_x = m_{\text{total}} \cdot a$$

$$+F_1 \cos 37^\circ - F_2 = (M_1 + M_2 + M_3) \cdot a$$

$$(100 \cdot 0.8) - 40 = 10a$$

$$40 = 10a$$

$$a = 4 \text{ m/s}^2$$



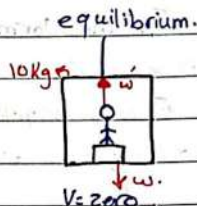
Elevator

[1] $\Sigma F_y = \text{Zero}$

$w' - w = 0$

$w' = w = m \cdot g$

$w' = w = 10 \cdot 10 = \boxed{100 \text{ N}}$

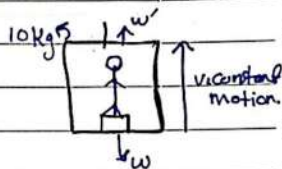


[2] $\Sigma F_y = \text{Zero}$

$w' - w = 0$

$w' = w = m \cdot g$

$w' = w = 10 \cdot 10 = \boxed{100 \text{ N}}$

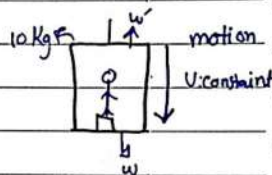


[3] $\Sigma F_y = \text{Zero}$

$w' - w = 0$

$w' = w = m \cdot g$

$w' - w = 10 \cdot 10 = \boxed{100 \text{ N}}$

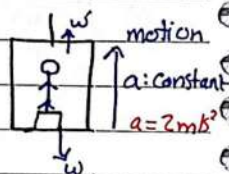


[4] $\Sigma F_y = ma$

$w' - w = ma$

$w' = mg + ma$

$w' = 10 \cdot 10 + 10 \cdot 2 = \boxed{120 \text{ N}}$

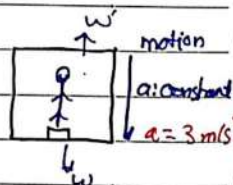


[5] $\Sigma F_y = ma$

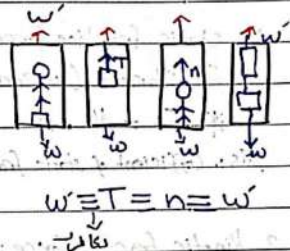
$w - w' = ma$

$w' = w - ma = mg - ma$

$= 100 - 30 = 70 \text{ N}$



* مقدار T يساوي الوزن الحقيقي w ؟
 إذا كان الجسم يسكن ويحرك بسرعة ثابتة للأعلى والأسفل
 من سرعة الزلا إذا حرك الجسم تسارع للأعلى
 وتقل عن w إذا حرك الجسم تسارع للأسفل



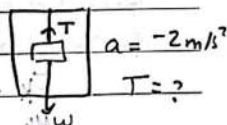
$$\sum F_y = ma$$

$$w - T = ma$$

$$5 \cdot 10 - T = -10$$

$$50 - T = -10$$

$$T = 50 + 10 = 60 \text{ N}$$



- حقيقي
 ① $v = \text{zero}$ $= w' = w$
 ② $v_i = v_f \uparrow$ $= w' = w$
 ③ $v_i = v_f \downarrow$ $= w' = w$
 ④ $v_i \neq v_f \rightarrow v_f > v_i \leftarrow +a \leftarrow \uparrow \leftarrow w' > w$
 ⑤ $v_i \neq v_f \rightarrow v_f < v_i \leftarrow +a \leftarrow \downarrow \leftarrow w' < w$
 ⑥ $v_i \neq v_f \rightarrow v_f < v_i \leftarrow -a \leftarrow \uparrow \leftarrow w' < w$
 ⑦ $v_i \neq v_f \rightarrow v_f < v_i \leftarrow -a \leftarrow \downarrow \leftarrow w' > w$

الحالات
 المسموعة
 Elevator

* $v = \text{zero} \rightarrow T = w$

* $v = \text{constant} \downarrow \rightarrow T = w$

* $a = \text{constant} \downarrow \rightarrow T < w$

* $a = g \downarrow \rightarrow T = \text{zero}$

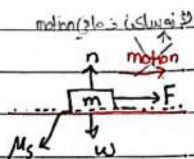
* $a > g \downarrow \rightarrow T = \text{zero}$ (لا يوجد تension) لا يوجد تension



Friction forces

1. static friction force: f_s Equilibrium ($v=0$) $\rightarrow \Sigma F = 0$

$$* f_s = \mu_s \cdot n$$

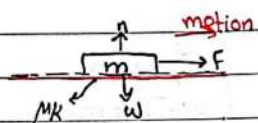
 μ_s : Coefficient of static friction2. kinetic friction force: f_k * Constant speed ($v_i = v_f$) $\rightarrow \Sigma F = 0$ * Constant accel ($v_i \neq v_f$) $\rightarrow \Sigma F = ma$

$$f_k = \mu_k \cdot n$$

 μ_k : Coefficient of kinetic friction

mostly always

$$1 > \mu_s > \mu_k > 0$$



* Find the tension and the acceleration in the following cases?

① y-axis $\rightarrow \Sigma F_y = 0$

$$n - w = 0$$

$$n = w = 100 \text{ N}$$

② $f_k = \mu_k \cdot n$

$$f_k = 0.5 \times 100 = 50 \text{ N}$$

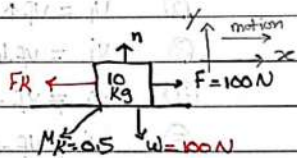
③ x-axis $\rightarrow \Sigma F_x = ma$

$$F - f_k = ma$$

$$100 - 50 = 10a$$

$$50 = 10a$$

$$\checkmark a = 5 \text{ m/s}^2$$



* Find the tension and the acceleration?

$$W_1 = m_1 g = 60 \text{ N}$$

$$W_2 = m_2 g = 40 \text{ N}$$

① y-axis $\Rightarrow \Sigma F_y = \text{zero}$

$$n_1 - W_1 = 0$$

$$n_1 = W_1 = \boxed{60 \text{ N}}$$

$$F_k = \mu_k \cdot n_1$$

$$F_k = 0.2 \times 60 = \boxed{12 \text{ N}}$$

② x-axis $\Rightarrow \Sigma F_x = m_1 a$

$$T - F_k = m_1 a$$

$$T - 12 = 6a$$

$$T = 6(2.8) + 12$$

$$\boxed{T = 28.8 \text{ N}}$$

③ y-axis $\Rightarrow \Sigma F_y = m_2 a$

$$W_2 - T = m_2 a$$

$$40 - T = 4a$$

$$T = 40 - (4(2.8))$$

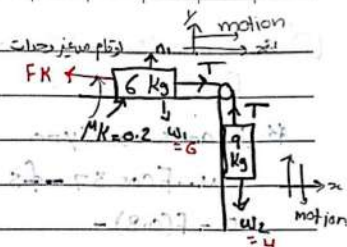
$$\boxed{T = 28.8 \text{ N}}$$

$$T - 12 = 6a$$

$$40 - T = 4a \quad +$$

$$28 = 10a$$

$$\boxed{a = 2.8 \text{ m/s}^2}$$



Find the min. force?

* $F_s = \mu_s \cdot n = 0.2 \cdot n$

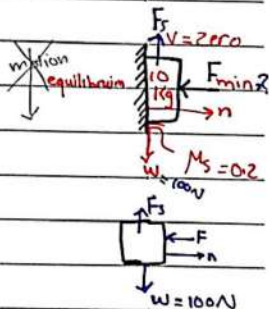
$$100 = 0.2 n \Rightarrow \boxed{n = 500 \text{ N}}$$

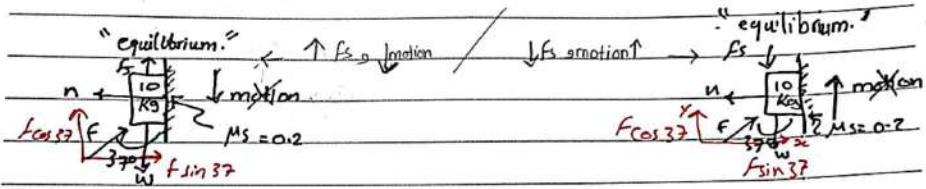
* x-axis $\Rightarrow \Sigma F_x = 0$

$$n - F_{min} = 0 \Rightarrow n = F_{min} = \boxed{500 \text{ N}}$$

* y-axis $\Rightarrow \Sigma F_y = \text{zero}$

$$W - F_s = 0 \Rightarrow W = F_s = \boxed{100 \text{ N}}$$





$$* w = m \cdot g = 100 \text{ N}$$

$$* w = m \cdot g = 100 \text{ N}$$

$$* x\text{-axis} \Rightarrow \Sigma F_x = 0$$

$$* x\text{-axis} \Rightarrow \Sigma F_x = 0$$

$$F \sin 37^\circ - n = 0$$

$$F \sin 37^\circ - n = 0$$

$$0.6 F = n = 0.6(108.6) = n$$

$$0.6 F = n = 0.6(108.6) = n$$

$$F = 65.16 \text{ N}$$

$$F = 65.16 \text{ N}$$

$$* fs = \mu_s \cdot n$$

$$* fs = \mu_s \cdot n$$

$$fs = 0.2(0.6 F)$$

$$fs = 0.2(0.6 F)$$

$$fs = 0.12(108.6)$$

$$fs = 0.12(108.6)$$

$$F_s = 13.032 \text{ N}$$

$$F_s = 13.032 \text{ N}$$

$$* y\text{-axis} \Rightarrow \Sigma F_y = 0$$

$$* y\text{-axis} \Rightarrow \Sigma F_y = 0$$

$$w - F \cos 37^\circ - fs = 0$$

$$F \cos 37^\circ - fs - w = 0$$

$$100 - 0.8 F - 0.12 F = 0$$

$$0.8 F - 0.12 F - 100 = 0$$

$$100 - 0.92 F = 0$$

$$0.68 F = 100$$

$$100 = 0.92 F$$

$$F_{\max} = 147 \text{ N}$$

$$F_{\min} = 108.6 \text{ N}$$

الحد الأدنى للشد 108.6

الحد الأقصى للشد 147

الحد الأقصى للشد 147

$$F \cos 37^\circ - fs - w = 0$$

$$0.8 F - 0.12 F - 100 = 0$$

$$F = 147 \text{ N}$$

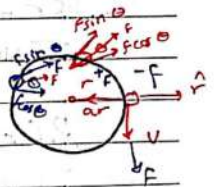
"Circular motion"

and other Application of newton laws.

* r-axis $\Rightarrow \Sigma F_r = m a_r$

$$\Sigma F_r = m \frac{v^2}{r}$$

$\hookrightarrow T, W, N, F$



particle zero velocity

* The Conical pendulum.

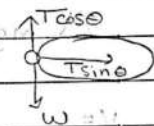
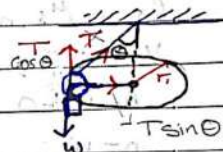
* r-axis $\Rightarrow \Sigma F_r = m \frac{v^2}{r}$

$$T \sin \theta = m \frac{v^2}{r} \quad (1)$$

* y-axis $\Rightarrow \Sigma F_y = 0$

$$T \cos \theta - W = 0$$

$$T \cos \theta = mg$$



(1) $\div$ (2)

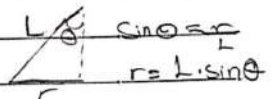
$$\frac{T \sin \theta}{T \cos \theta} = \frac{m \frac{v^2}{r}}{mg}$$

$$\tan \theta = \frac{v^2}{rg}$$

$$\tan \theta = \frac{v^2}{rg}$$

$$v = \sqrt{rg \cdot \tan \theta}$$

$$v = \sqrt{L g \sin \theta \tan \theta}$$



• Resultant force. R.F

$$R_f = \sqrt{(\Sigma F_r)^2 + (\Sigma F_y)^2} = \sqrt{(\Sigma F_r)^2 + 0}$$

$$R_f = \Sigma F_r$$

$$\frac{v^2}{r} (R_f = m \frac{v^2}{r}) = (T \sin \theta)$$

2nd app

The Conical pendulum.

$$\Sigma Fr = m \frac{v^2}{r}$$

$$T \sin \theta = m \frac{v^2}{r}$$

$$v = \sqrt{r g \tan \theta}$$

$$R.F = \Sigma Fr = m \frac{v^2}{r} = T \sin \theta \leftarrow \text{إطلاق}$$

طريق أفقي دائري (دوران غير منتظم) حول عمود ثابت

* The unbanked Roadway. level of inner and outer edge of the road is same.

R-axis =

$$\Sigma Fr = m \frac{v^2}{r}$$

$$f_s = m \frac{v^2}{r} \leftarrow 1$$

$$f_s = \mu_s \cdot n \leftarrow 2$$

Y-axis =

$$\Sigma F_y = \text{zero}$$

$$n - w = 0 \quad n = w \leftarrow 3$$

لعموم 2 و 3

$$f_s = \mu_s \cdot Mg \rightarrow 4 \leftarrow f_s = \mu_s \cdot n = f_s = \mu_s \cdot m = f_s = \mu_s \cdot Mg$$

لعموم 1 و 4

$$\mu_s Mg = m \frac{v^2}{r} = \frac{\mu_s \cdot m \cdot g}{1} = \frac{m \cdot v^2}{r} = \mu_s \cdot g = \frac{v^2}{r}$$

$$v = \sqrt{r \cdot g \cdot \mu_s} \leftarrow v_{\text{max}}$$

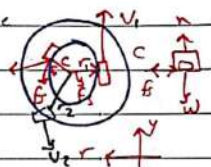
$$* R.F = \sqrt{(\Sigma Fr)^2 + (\Sigma Fy)^2} = 0$$

$$R.F = \Sigma Fr = "m \frac{v^2}{r}" = f_s \leftarrow \text{إطلاق}$$

* Making circular motion

$$f_{s1} = f_{s2}$$

$$\mu \frac{v_1^2}{r_1} = \mu \frac{v_2^2}{r_2} \Rightarrow \frac{v_1^2}{r_1} = \frac{v_2^2}{r_2}$$



لأنه لا يوجد ميل في الطريق

لأنه لا يوجد ميل في الطريق

نفسه

* The Banked Roadway.

طريقة اخرى لاجابة السؤال السابق باننا اذا كان

كيف يجب ان تكون السرعة

normal force or reaction

السرعة والزاوية



* r-axis =

$$\sum F_r = m \frac{v^2}{r}$$

$$n \sin \theta = m \frac{v^2}{r} \rightarrow 0$$

* y-axis =

$$\sum F_y = \text{zero}$$

$$n \cos \theta - w = 0 \rightarrow n \cos \theta = w \quad w = m \cdot g$$

$$n \cos \theta = m \cdot g \rightarrow \textcircled{2}$$

2 equations and 2 unknowns

$$\frac{n \sin \theta}{n \cos \theta} = \frac{m \frac{v^2}{r}}{m \cdot g} = \frac{v^2}{r \cdot g} \tan \theta$$

$$R.F. = \sqrt{(\sum F_r)^2 + (\sum F_y)^2}$$

$$R.F. = \sum F_r = m \frac{v^2}{r} = n \sin \theta \leftarrow \text{split both}$$

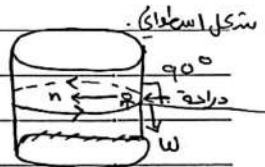
$$\rightarrow \theta = 90^\circ \rightarrow n = m \frac{v^2}{r}$$

normal force

السرعة والزاوية

$$\sin 90 = 1$$

$$R.F. = \sqrt{n^2 + w^2}$$



* Circular vertical motion.

① Top point

$$\Sigma F_r = m \frac{v^2}{r}$$

$$T + w = m \frac{v^2}{r} \leftarrow \textcircled{1} = T = m \frac{v^2}{r} - w$$

$$T = m \frac{v^2}{r} - m \cdot g \leftarrow w = m \cdot g$$

(في الحالة الجذبية أو أقل من نصف أو يساوي نصف)

$T =$ السحب

في حالة التوازن

$$T = m \left(\frac{v^2}{r} - g \right) \geq 0$$

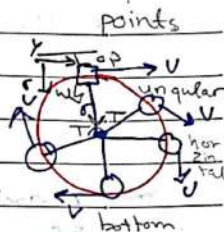
$$= \frac{v^2}{r} - g \geq 0$$

$$\frac{v^2}{r} - g = 0$$

$$v_{\min} = \sqrt{r \cdot g}$$

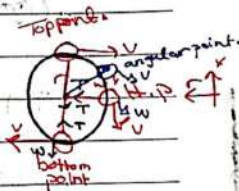
$$R.F \leq \sqrt{(\Sigma F_r)^2 + (\Sigma F_t)^2} \text{ (في حالة التوازن)}$$

$$R.F = \Sigma F_r \leq m \frac{v^2}{r} \leq T + w \leftarrow \text{في حالة التوازن}$$



The circular vertical motion:

Top Point $\left\{ \begin{array}{l} V_{min} \leftarrow \underline{\text{Top point s}} \cdot \sqrt{r_g} \\ R.f.s \quad \Sigma f r = m \cdot v^2 \cdot (T+W) \end{array} \right.$ ^{apls}



Bottom point.

$$\sum f r s \text{ m } \underline{v_2}$$

$$T - w = m \frac{v^2}{r} \quad \text{--- (1)} \quad T = m \frac{v^2}{r} + w \quad [w = m \cdot g]$$

$$T = m \frac{v^2}{r} + m \cdot g > 0$$

لا يجوز قولي على $R.F \sqrt{(E.F)^2 + (P.F)^2}$

$$12f = \sum f r = m \frac{v^2}{r} = T - W \leftarrow \text{ap. balls}$$

"Horizontal point"

— R-axis

$$\sum F_r = m \frac{v^2}{r}$$

$$T = m \frac{v^2}{r} \quad (1)$$

$$R.f = \sqrt{(\sum f_x)^2 + (\sum f_y)^2}$$

$$Rf = \sqrt{(m \cdot \frac{v^2}{r})^2 + (m \cdot g)^2}$$

$R \cdot f \leq \sqrt{T^2 + W^2} \leftarrow 90^\circ \leftarrow \text{حالة خاصة}$

"angular point"

R. axis

$$\Sigma f_r = m v^2$$

$$T + W \cos \theta = m \frac{v^2}{r} \quad \text{--- (1)}$$

$$T = m \frac{v^2}{r} - mg \cos \theta \geq 0$$

$$T = m(\frac{v^2}{r} - g \cos \theta) \geq 0$$

$$= \frac{v^2}{r} - g \cos \theta \geq 0 \quad \text{--- (2)}$$

$$(V_{\min})^2 - g \cos \theta \neq 0 \quad \text{--- (3)}$$

$$V_{min} = \sqrt{r \cdot g \cos \theta}$$

$$R.f = \sqrt{(T + W \cos \theta)^2 + (W \sin \theta)^2} \quad \text{Sol}$$

$$R.f = \sqrt{(m \cdot v_r)^2 + (m \cdot g \sin \theta)^2}$$

Loop-The-Loop

Top point.

$$Efr = m v^2$$

$$n + W = m v^2$$

$$n = m v^2 - m \cdot g \geq 0$$

normal force ≥ 0 اذا كان اقل من 0

$$= m (v^2 - g) \geq 0$$

$$= \frac{v^2}{r} - g \geq 0$$

$$\frac{v_{min}^2}{r} - g = 0$$

$$v_{min} = \sqrt{rg} = 0$$



1.9 Q13

$$Efr = m v^2$$

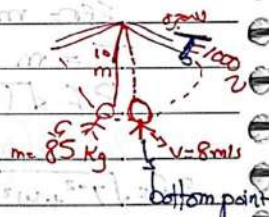
$$T - W = m v^2$$

$$T - (85 \times 10) = 85 \cdot \frac{8^2}{10}$$

$$T - 850 = 544$$

$$T = 544 + 850$$

$$T = 1394 N > 1000 \leftarrow \text{اذا جيتحط breaking}$$



اذا جيتحط +

وكان اقل من 1000

ما يتخطى اذا الج

يتخطى

Q1 3kg :-

R-axis

$$\sum F_r = m \frac{v^2}{r}$$

$$+ T = m \frac{v^2}{r} \quad (1)$$

Y-axis =

$$\sum F_y = \text{zero}$$

$$+ T - W_2 = 0 \quad (2)$$

$$T = W_2 = 250 \text{ N}$$

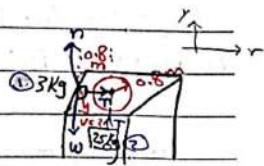
Answer

1 → Given 2-Step

$$250 = 3 \cdot \frac{v^2}{0.8}$$

$$v = \sqrt{250 \cdot 0.8}$$

$$v = 8.1 \text{ m/s}$$



تension T, T

وزن W

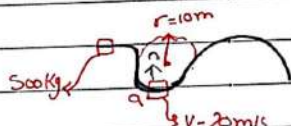
Q14 What is the force exerted by the track on the car? at the Point A?

normal force

$$\sum F_r = m \frac{v^2}{r}$$

$$n - W = m \frac{v^2}{r} = n - 500 \times 10 + 500 \left(\frac{20^2}{10} \right)$$

$$n = 2500 \text{ N} = 25 \text{ kN}$$



b) What is the maximum speed of the vehicle can have on point B?

point A $\Rightarrow \sum F_r = m \frac{v^2}{r}$

$$W - n = m \frac{v^2}{r} \quad (1)$$

maximum speed $\Rightarrow$ normal force = Zero

$$W = m \frac{v^2_{\text{max}}}{r} = m g$$

$$v_{\text{max}} = \sqrt{r g}$$

$$v_{\text{max}} = \sqrt{15 \cdot 10} = \sqrt{150} = 12.2 \text{ m/s}$$

* If the speed equals 10 m/s, find the normal force?

$$W - n = m \frac{v^2}{r} \quad n = 500 - 3350$$

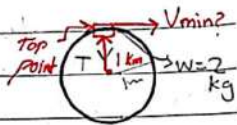
$$500 \cdot 10 - n = 500 \cdot \frac{10^2}{15}$$

$$n = 1650 \text{ N}$$

Ex// Circular Vertical motion.

① $r = 1 \text{ km}$, Find the minimum speed at top Point?

$$v_{\min} = \sqrt{rg} = \sqrt{1000 \cdot 10} = 100 \text{ m/s}$$



② at the top point, if the maximum tension equals $50w$, find the velocity maximum?

$$\sum F_r = m v^2$$

$$T + W = m v^2 \quad \text{---} \quad T_{\max} + W = m v_{\max}^2$$

$$50 + 2 \cdot 10 = 2 \cdot v_{\max}^2$$

$$1000 \times 70 = 2 v_{\max}^2$$

$$v_{\max} = \sqrt{35000} = 187 \text{ m/s}$$

Ex// Banked Roadway:-

$v_{\max} = 10 \text{ m/s}$, find θ ?

$$v = \sqrt{rg \tan \theta}$$

$$10^2 = \sqrt{5 \cdot 10 \tan \theta}$$

$$100 = 5 \tan \theta$$

$$\theta = \tan^{-1} \left(\frac{100}{5} \right)$$

$$\theta = \tan^{-1}(2) = 63.4^\circ$$

Energy of a system

Dot product:

$$\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$$

$$\vec{B} = B_x \hat{i} + B_y \hat{j} + B_z \hat{k}$$

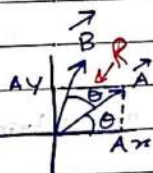
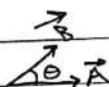
$$\vec{A} \cdot \vec{B} = (A_x B_x) \hat{i} \cdot \hat{i} + (A_y B_y) \hat{j} \cdot \hat{j} + (A_z B_z) \hat{k} \cdot \hat{k}$$

$$A = \sqrt{(A_x)^2 + (A_y)^2 + (A_z)^2}$$

$$B = \sqrt{(B_x)^2 + (B_y)^2 + (B_z)^2}$$

$$\vec{A} \cdot \vec{B} = AB \cos \theta \rightarrow$$

$$\theta = \tan^{-1}\left(\frac{|A_y|}{A_x}\right)$$



$$\text{Ex: } \vec{A} = 2\hat{i} + 3\hat{j}$$

$$\vec{B} = -\hat{i} + 2\hat{j} + 2\hat{k}$$

$$\textcircled{1} \text{ find } \vec{A} \cdot \vec{B} ? (2 \cdot -1) \hat{i} \cdot \hat{i} + (3 \cdot 2) \hat{j} \cdot \hat{j} + (0 \cdot 2) \hat{k} \cdot \hat{k} = -2 + 6 + 0$$

$$\vec{A} \cdot \vec{B} = 4$$

② find the angle between A and B?

$$A = \sqrt{2^2 + 3^2} = \sqrt{13}$$

$$B = \sqrt{(-1)^2 + 2^2 + 2^2} = \sqrt{9} = 3$$

$$\vec{A} \cdot \vec{B} = AB \cos \theta$$

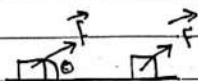
$$4 = \sqrt{13} \cdot 3 \cos \theta$$

$$\theta = \cos^{-1}\left(\frac{4}{\sqrt{13} \cdot 3}\right) = 68.3^\circ$$

$$W \text{ or } R [N \cdot m] = [J] = W$$

$$W = \vec{F} \cdot \vec{\Delta r}$$

$$\begin{aligned} \text{dot prod} &= F_x \Delta x + F_y \Delta y + F_z \Delta z \\ &= F \Delta r \cos \theta \end{aligned}$$



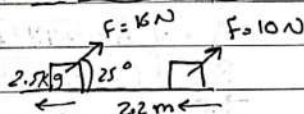
Ex: Determine the work done by:

1) the applied force? $\rightarrow 16 \cdot 1.52$

$$W_F = F \Delta r \cos \theta$$

$$16 \cdot 2.2 (\cos 25^\circ)$$

$$\Rightarrow W_F = 31.9 \text{ J}$$



2) Normal force?

$$W_n = n \cdot \Delta r \cos 90^\circ$$

$$\Rightarrow W_n = \text{Zero}$$

3) the gravitational force? "weight"?

$$W_w = w \cdot \Delta r \cos 90^\circ$$

$$\Rightarrow W_w = \text{Zero}$$

4) find the total work?

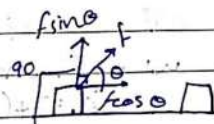
$$W_a + W_n + W_w$$

$$31.9 + 0 + 0$$

$$= 31.9 \text{ J}$$

$$= W = f_x \Delta x \overset{\cos \theta = 1}{\cos \theta}$$

$$(f \cos \theta) \Delta x$$



Ex: $\vec{F} = 6\mathbf{j} + 4\mathbf{j}$ find the total

$\Delta\vec{r} = 3\mathbf{i} - 3\mathbf{j}$ worth?

$$W = \vec{F} \cdot \Delta\vec{r}$$

$$(6 \cdot 3) + (4 \cdot -3)$$

$$= W = 6J$$

* Work done by

$$W = \int \vec{F} \cdot d\vec{r}$$

$$W = \int_{x_1}^{x_2} F_x dx + \int_{y_1}^{y_2} F_y dy + \int_{z_1}^{z_2} F_z dz$$

Ex: $\vec{F} = (3x^2\mathbf{j} + 4\mathbf{j})N$

from the origin to $(2, 3)m$

$$W = \int_0^2 3x^2 dx + \int_0^3 4 dy$$

$$\left[\frac{3x^3}{3} \right]_0^2 + \left[4y \right]_0^3$$

$$= (2^3 - 0^3) + (4 \cdot 3 - 4 \cdot 0)$$

$$W = 8 + 12 = 20J$$

$$W = \int F_r dr$$



(1) Find the work to go to $x = 5m$?

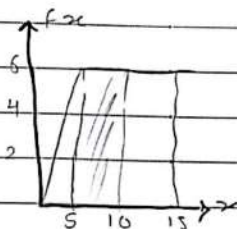
$$(1) W_1 = \text{area}_1 = \frac{1}{2} \cdot 5 \cdot 6 = 15J$$

(2) $5m \rightarrow 10m$?

$$W_2 = \text{area}_2 = 5 \cdot 6 = 30J$$

(3) Total work? from $0 \rightarrow 10m$?

$$\text{Total} = W_{\text{work}_1} + W_{\text{work}_2} = 15 + 30 = 45J$$



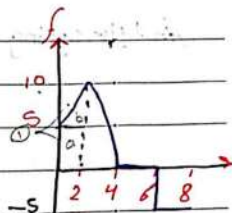
1) Find the work from 0-2m?

$$W_1 = W_a + W_b$$

$$= 2.5 + \frac{1}{2} \cdot 2.5$$

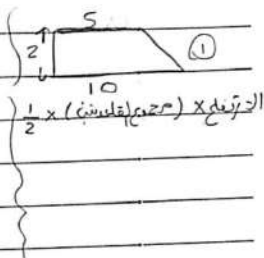
$$W_1 = 10 + 5 = 15J$$

$$\text{or } W_1 = \frac{(5+10)}{2} \cdot 2 = 15J \leftarrow \text{area of triangle (مساحة مثلث)}$$



2) 2m → 4m?

$$W_2 = \frac{1}{2} (2)(10) = W_2 = 10J$$



3) 4m → 6m?

$$W_3 = \text{Zero} \leftarrow \text{zero work}$$

4) 6m → 8m?

$$W_4 = -2.5 = -10J$$

5) Find the total work?

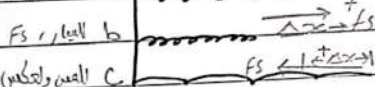
$$W_1 + W_2 + W_3 + W_4$$

$$15 + 10 + 0 - 10 = W = 15J$$

work done by a spring.

الشغل الناتج عن نابض

Δx is a, $x=0, F_s=0$

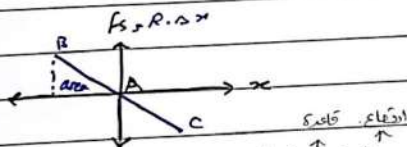


$$F_s = R \Delta x$$

$$F_s = R \Delta x$$

R: spring constant [N/m]

F_s: Spring force [N]



$$W_s = \text{area} = \frac{1}{2} (\Delta x) F_s$$

$$= \frac{1}{2} (\Delta x) (R \Delta x)$$

$$W_s = \frac{1}{2} R \Delta x^2$$

find the spring const?



$$\sum F_k = 0$$

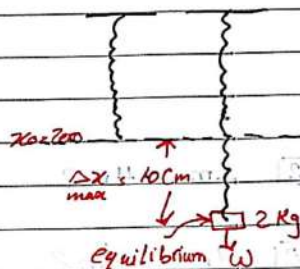
$$F_s - W = 0$$

$$F_s = W$$

$$R \Delta x_{max} = mg$$

$$R(0.1) = 2 \cdot 10$$

$$R = \frac{20}{0.1} = 200 \text{ N/m}$$



$$W = \vec{F} \cdot \Delta \vec{r}$$

$$= F_x \Delta x + F_y \Delta y + F_z \Delta z$$

$$= F \Delta r \cos \theta$$

$$= \int F_x dx + \int F_y dy + \int F_z dz$$

$$= \frac{1}{2} R \Delta x^2$$

$$= \text{area} \quad \left[\begin{array}{l} F_r \\ \text{area} \\ \text{area} \end{array} \right]$$

Kinetic Energy - work

$$K = \frac{1}{2} m (\vec{v} \cdot \vec{v})$$

$$K = \frac{1}{2} m (v^2)$$

$$\text{work } K = \int \vec{F} \cdot d\vec{r}$$

$$= \int \vec{F} \cdot d\vec{r}$$

$$= m \left\{ \frac{d\vec{v}}{dt} \cdot d\vec{r} \right\}$$

$$= m \int \frac{d\vec{v}}{dt} \cdot \frac{d\vec{r}}{dt} dt$$

$$= m \int \frac{d\vec{v}}{dt} \cdot \vec{v} dt$$

$$= m \int \vec{v} \cdot d\vec{v}$$

$$= m \int \vec{v} \cdot d\vec{v}$$

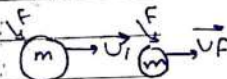
$$= m \cdot \left. \frac{1}{2} v^2 \right|_{v_i}^{v_f} = \frac{1}{2} m v^2 \Big|_{v_i}^{v_f}$$

$$= \frac{1}{2} m v_f^2 - \frac{1}{2} m v_i^2$$

$$= K_f - K_i$$

$$= \Delta K$$

$$\left\{ W = \Delta K \Rightarrow W = K_f - K_i \right\} \leftarrow \text{الشغل النهائي}$$



Q) $m = 3\text{ Kg}$, $v_i = (6\mathbf{j} - 2\mathbf{j})\text{ m/s}$

(A) what is kinetic energy at this time?

$K = \frac{1}{2} m v^2 \rightarrow v_i = \sqrt{(6)^2 + (-2)^2}$

$K = \frac{1}{2} (3) (\sqrt{40})^2 \quad v_i = \sqrt{36 + 4}$

$K = \frac{3}{2} \cdot 40 = 60\text{ J}$ $v_i = \sqrt{40}$

$K = 60\text{ J}$

(B) Find the total work, if: $\vec{v}_f = (8\mathbf{j} + 4\mathbf{j})\text{ m/s}$.

$\rightarrow K = 60\text{ J}$

$\rightarrow K_f = \frac{1}{2} m v_f^2 \rightarrow v_f = \sqrt{(8)^2 + (4)^2}$

$K_f = \frac{1}{2} \cdot 3 \cdot (\sqrt{80})^2 \quad v_f = \sqrt{64 + 16}$

$K_f = \frac{3}{2} \cdot 80 = 120\text{ J}$ $v_f = \sqrt{80}\text{ m/s}$

$K_f = 120\text{ J}$

$\rightarrow W_{\text{total}} = K_f - K_i$

$120 - 60 = 60\text{ J} \leftarrow W_{\text{total}}$

* الجسم عندما يتحرك حركة دائرية دائمة $\rightarrow$ "Zero"

* 2 إذا رجع الجسم لنفس النقطة التي انطلق منها $\rightarrow$ " $\Delta v = \text{zero}$ " و " $W = \text{zero}$ "

* 3 إذا كانت الزاوية $\leftarrow (\theta = 90^\circ) \leftarrow \cos 90^\circ = 0$ و " $W = \text{zero}$ "

* 4 إذا كانت السرعة (contact speed) $\leftarrow (\Delta v = \text{zero}) \leftarrow (\Delta K = \text{zero}) \leftarrow (W = \text{zero})$

Q) Find the speed at $(x=5\text{m})$, $(x=10\text{m})$ and $(x=15\text{m})$? $\uparrow f(x)$

A) (0-5m) s

$$w_1 = \text{area} = \frac{1}{2} \cdot 5 \cdot 3 = \frac{15}{2}$$

$$W_1 = 7.5 \text{ J}$$

$$W_1 = \frac{1}{2} m v_1^2 = \frac{1}{2} m v_1^2 \leftarrow \text{from the rest}$$

$$7.5 = 1 \cdot 4^2 \cdot v_f^2$$

$$7.5 = 2 \sqrt{f}$$

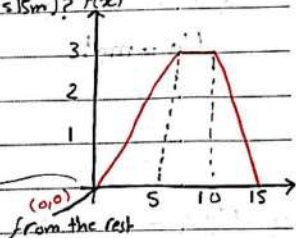
$$\sqrt{v_f^2} = \sqrt{\frac{7.5}{7}}$$

$$V_f = 1.9 \text{ m/s}$$

$$V_{f1} = V_{i2}$$

→ Speed at $x = 5\text{ m}$

Speed = 1.9 m/s



B) (5-10m) ±

afen 5.3 $\rightarrow W_2 = 15,7$

$$W_2 = \frac{1}{2} \cdot 4 \cdot v_f^2 = \frac{1}{2} \cdot 4 \cdot (1.9)^2$$

$$15 = 2vf^2 - 7.5$$

$$15 + 7.5 = 2vf^2$$

$$\sqrt{22.5} = \sqrt{\frac{2}{3} V f^2}$$

$$v_f = 3.35 \text{ m/s} = v_{ig}$$

→ speed at $x = 10\text{m}$

Speed = 3.35 m/s

عاشق احل على جوانب الحرية لازم تكون اقرب وابنة

فلسفان اطلع المسارع (يعني A و C) هادقوا اطلعه

$$(5-10)m = \Sigma F = ma = \frac{3}{4} = \frac{4a}{4}$$

$$v_f^2 = v_i^2 + 2a\Delta x \quad \text{--- (iii)}$$

$$v_f^2 = (1.9)^2 + 2 \cdot \frac{9.8}{10} \cdot 5$$

$$v_f^2 = 3.61 + 7.5 \therefore \therefore$$

$$\sqrt{v^2} = \sqrt{|v|^2}$$

$$v_f = 3.35 \text{ m/s} \therefore \Delta$$

sorted at xslom.

c) $(10-15\text{m}) =$

$$W_3 = \text{area} = \frac{1}{2} \cdot 5 \cdot 3 = W_3 = 7.5 \text{ J}$$

$$W_3 = \frac{1}{2} \cdot \frac{2}{4} \cdot 4^2 - \frac{1}{2} \cdot \frac{2}{4} \cdot (3.35)^2$$

$$7.5 = 2V_f^2 - 22.5 = 7.5 + 22.5 = 2V_f^2$$

$$\sqrt{\frac{30}{2}} = \sqrt{\frac{2}{2} v_f^2} \quad v_f = 3.87 \text{ m/s}$$

$\Rightarrow$ speed at $x = 15 \text{ m}$

→ speed = 3.87 m/s

H.W.

(O_2) and

(0.15 m)

Physics

potential energy of a system work.

$$U_g = mgh$$

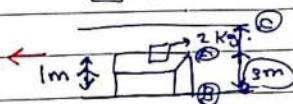


☐ +V
☒ U = zero
☐ -V

$$V_{gA} = mgh_A = \text{Zero}$$

$$V_{gB} = mgh_B = 2 \times 10 \times 1 \text{ m} = +20 \text{ J}$$

$$V_{gC} = mgh_C = 2 \times 10 \times 2 = -40 \text{ J}$$



$$W = -\Delta V_g$$

$$= -(V_{gf} - V_{gi})$$

$$= -(mgy_f - mgy_i)$$

$$W = \int \vec{F}_x dx$$

$$W = -\Delta V_g$$

$$-\Delta V_g = \int_{x_i}^{x_f} \vec{F}_x dx$$

$$\Delta V_g = V_{gf} - V_{gi} = \int \vec{F}_x dx$$

$$\Delta V = \int_{x_i}^{x_f} \vec{F}_x dx$$

$$\vec{F}_x = -\frac{dV}{dx}$$

$$\vec{F} = -\left(\frac{dV}{dx} \hat{i} + \frac{dV}{dy} \hat{j} + \frac{dV}{dz} \hat{k}\right)$$

Ex) $V = -A/x^2 \rightarrow$ find the force at $x = 2 \text{ m}$ $\leftarrow A = \text{Constant}$

$$F = -\frac{dV}{dx} = -\frac{d(-Ax^{-2})}{dx}$$

$$= -2Ax^{-2} = -2A/x^2$$

$$F(x=2 \text{ m}) = \frac{-2A}{2^2} = -\frac{A}{4} \text{ N}$$

① $\vec{F} = 3x^2 \hat{i}$ ← find ΔV from $x_i = 1\text{m}$ to $x_f = 3\text{m}$?

$$\Delta V = - \int_{x_i}^{x_f} F dx$$

$$\int_{x_i}^{x_f} 3x^2 dx = - \left. \frac{3x^3}{3} \right|_1^3 = - [3 - 1] = -26 \text{ J}$$

② If final, potential energy equal 10J, find V_i .

$$\Delta V = V_f - V_i = - \int_{x_i}^{x_f} F dx$$

$$10 - V_i = -26$$

$$V_i = 10 + 26$$

$$V_i = 36 \text{ J}$$

CH8: Conservation of Energy

$$E = K + U_g$$

E = Mechanical energy

fraction less + without spring

$$E_i = E_f$$

$$K_i + V_{gi} = K_f + V_{gf}$$

$$E_x = m = 2 \text{ kg}$$

① Find H_B ?

$$E_A = E_B$$

$$K_A + V_{gA} = K_B + V_{gB}$$

$$0 + mgh_A = \frac{1}{2}mv_B^2 + mgh_B$$

$$10 \times 100 = \frac{1}{2}(20)^2 + 10 H_B$$

$$1000 = 200 + 10 H_B$$

$$H_B = \frac{1000 - 200}{10}$$

$$H_B = 80 \text{ m}$$

② Find the speed at C point? v_C ?

$$E_A = E_C$$

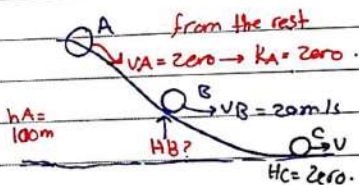
$$K_A + V_{gA} = K_C + V_{gC}$$

$$mgh_A = \frac{1}{2}mv_C^2$$

$$2 \times (10(100)) = \left(\frac{1}{2}v^2\right) \times 2$$

$$v = \sqrt{2000}$$

$$v = 44.7 \text{ m/s}$$



$$E = K + Vg$$

$$E_i = E_f$$

$$K_i + Vg_i = K_f + Vg_f$$

fraction less without spring

③ find the speed at h point

$$V_H = 44.7 \text{ m/s}$$

$$K_C + Vg_C = K_H + Vg_H$$

$$mV_C^2 = mV_H^2$$

$$V_C = V_H = 44.7 \text{ m/s}$$

$$* K_i + Vg_i + V\dot{s}_i = K_f + Vg_f + V\dot{s}_f + |work|$$

find Δx max

$$K_{ic} + Vg_{ic} + V\dot{s}_{ic} = K_{fc} + Vg_{fc} + V\dot{s}_{fc} + |W_{fKc \rightarrow f}|$$

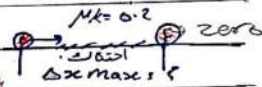
$$K_C = W_{fKc \rightarrow f}$$

$$\frac{1}{2} m V_C^2 = MK \cdot g \cdot \Delta x_{max}$$

$$\frac{1}{2} (44.7)^2 = 0.2 \cdot 10 \cdot \Delta x_{max}$$

$$1020 = 2 \Delta x_{max}$$

$$\Delta x_{max} = 500 \text{ m}$$



$$\begin{aligned} \sum F_y &= 0 \\ n &= w \\ f_k &= \mu_k \cdot n \\ f_k &= \mu_k \cdot m \cdot g \\ \mu_f &= f \Delta x_{max} \end{aligned}$$

* find the speed at (b) point?

$$K_A + Vg_A + V\dot{s}_A = K_B + Vg_B + V\dot{s}_B + |W_{fKc \rightarrow f}|$$

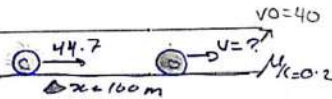
$$Vg_A = K_A + |W_{fKc \rightarrow f}|$$

$$mgh_A = \frac{1}{2} m V_0^2 + MK \cdot g \cdot \Delta x$$

$$10 \cdot 100 = \frac{1}{2} (V_0^2) + 0.2 (10) (100)$$

$$2000 - 1000 = \frac{1}{2} V_0^2 + 200$$

$$\sqrt{2 \times (800)} = \left(\frac{1}{2} V_0^2 \right)^2 \quad V = \sqrt{1600} = V = 40 \text{ m/s}$$



physics

25. Dec. 2020

$$K_c + V_{gc} + V_{sc} + K_r + V_{gr} + V_{sr} + \cancel{M \times \cancel{v_{cr}}}$$

Find $\Delta x'_{max}$?

$$K_c = V_{sr}$$

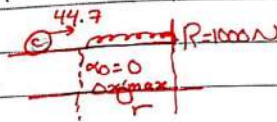
$$\frac{1}{2} m v_c^2 = \frac{1}{2} \cdot R (\Delta x'_{max})^2$$

$$\frac{1}{2} (2)(44.7)^2 = \frac{1}{2} (1000) (\Delta x'_{max})^2$$

$$2000 = 500 (\Delta x'_{max})^2$$

$$\sqrt{(\Delta x'_{max})^2} = \sqrt{4}$$

$$\Delta x'_{max} = 2m$$



$$E_i = E_f$$

$$K_i + V_{gi} = K_f + V_{gf}$$

* fractional less without spring.

$$K_i + V_{gi} + V_{si} = K_f + V_{gf} + V_{sf} + (W_{fK})$$

fraction + spring.

Find the final speed?

$$K_i + V_{gi} = K_f + V_{gf}$$

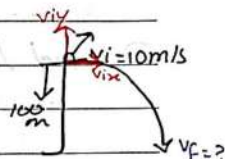
$$\frac{1}{2} m v^2 + m g H = \frac{1}{2} m v^2 + 0$$

$$\frac{1}{2} (10)^2 + (10)(100) = \frac{1}{2} v^2$$

$$2 \times (50 + 1000) = \frac{1}{2} v^2 \times 2$$

$$\sqrt{2100} = \sqrt{v^2}$$

$$v = \sqrt{2100} \text{ m/s.}$$



* power :- $\leftarrow P$

$$P = \frac{W}{\Delta t} [\text{J/s}] \leftarrow [\text{watt}]$$

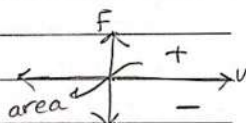
$$P = \textcircled{1} \frac{W}{\Delta t}$$

$$P = \textcircled{2} F \cdot v$$

$$\vec{F} \cdot \frac{\Delta \vec{r}}{\Delta t} = \vec{F} \cdot \vec{v}$$

$$= F_x \cdot v_x + F_y \cdot v_y + F_z \cdot v_z$$

$$= F v \cos \theta$$



$$P = \int F_x dx + \int F_y dy + \int F_z dz$$

① $\vec{F} = 2\hat{i} + 3\hat{j}$ / $\vec{v} = 5\hat{i} - \hat{j}$, find the power?

$$P = (2 \times 5) + (3 \times -1) = 10 - 3 = 7 \text{ watt}$$

② $\Delta t = 3\text{s}$, find the total work?

$$P = \frac{W}{\Delta t}$$

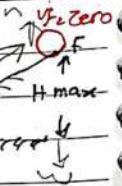
$$7 = \frac{W}{3} \Rightarrow W = 7 \times 3$$

$$W = 21 \text{ J}$$

① Find H max?

(horizontal) m/s

$\mu K = 0.2$



$$K_i + V_{gi} = K_f + V_{gf}$$

$$\frac{1}{2} m v^2 = m g H_{max}$$

$$\frac{1}{2} (10)^2 = 10 H_{max}$$

$$\frac{50}{10} = 10 H_{max}$$

$$H_{max} = 5 \text{ m}$$

② find L max?

$$\sin 30 = \frac{H_{max}}{L}$$

$$\frac{1}{2} = \frac{5}{L}$$

$$L = \frac{5}{0.5}$$

$$L = 10 \text{ m}$$

③ find WFR 0 → F?

$$K_i + V_{gi} = K_f + V_{gf} + |W_{fr}|$$

$$W_{fr} = F \times L' \sin \theta$$

$$\frac{1}{2} m v^2 = m g h_{max} + \mu K m g \cos \theta \cdot L' \sin \theta$$

$$(\mu K n) (L' \sin \theta)$$

$$\frac{1}{2} (10)^2 = 10 h' + 0.2 \cdot 10 \cos 30 \cdot L' \sin 30$$

$$(\mu K n) (m g \cos \theta) L' \sin \theta$$

$$\frac{1}{2} (10)^2 = 10 h' + 0.2 \cdot 10 \cdot 0.87 \cdot L' \sin 30$$

$$50 = 10 h'_{max} + 1.74 \cdot L' \sin 30$$

$$\sin 30 = \frac{h'_{max}}{L' \sin 30} = 0.5$$

$$50 = 10 (0.5) L' \sin 30 + 1.74 \cdot L' \sin 30$$

$$50 = 6.74 L' \sin 30$$

$$L' \sin 30 = 7.4 \text{ m}$$

L' displacement

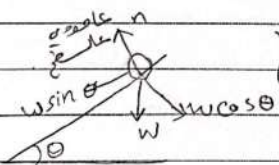
$$h'_{max} = 0.5 \cdot L' \sin 30$$

displacement

$$= 0.5 (7.4)$$

$$h'_{max} = 3.57 \text{ m}$$

H displacement



$$\sum F_y = 0 = n - W \cos \theta = 0 \quad n = W \cos \theta$$

← normal force

Linear momentum and Collision.

$$K = \frac{1}{2} m v^2$$

$$\vec{p} = m \vec{v}$$

$$\sum \vec{F} = m \vec{a} = m \frac{d\vec{v}}{dt}$$

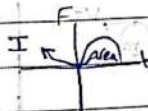
$$\sum \vec{F} = \frac{d(m\vec{v})}{dt}$$

$$\sum \vec{F} = \frac{d\vec{p}}{dt}$$

$$\int \frac{d\vec{p}}{dt} dt = \int \sum \vec{F} dt$$

$$\Delta \vec{p} = \vec{p}_f - \vec{p}_i = \int \sum \vec{F} dt$$

$$\vec{I} = \text{Impulse} = \vec{I} = \sum \vec{F}_{ave} \Delta t$$



1) Ex// Find the Impulse?

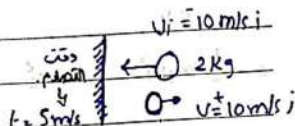
$$\vec{I} = \vec{p}_f - \vec{p}_i$$

$$\vec{I} = m \vec{v}_f - m \vec{v}_i$$

$$\vec{I} = 2(10\hat{j}) - 2(-10\hat{j})$$

$$\vec{I} = 20\hat{j} + 20\hat{j}$$

$$\vec{I} = 40 \text{ Kg m/s } \hat{j} \text{ or } 40 \text{ N.s } \hat{j}$$



2) Ex// Find the average force?

$$\vec{I} = \Delta \vec{p} = \vec{F}_{ave} \Delta t$$

$$40 = \vec{F}_{ave} \cdot 5 \times 10^{-3}$$

$$\vec{F}_{ave} = \frac{40}{5 \times 10^{-3}}$$

$$\vec{F}_{ave} = 8000 \text{ N}$$

Ex// Q9.

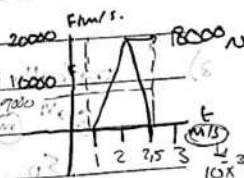
of Find the Impulse?

$$I = \text{area} = \frac{1}{2} (1.5 \times 10^3) (18000) = 13.5 \text{ N.s}$$

of Find the average force?

$$I = \vec{F}_{ave} \Delta t = 13.5 = \vec{F}_{ave} \cdot (1.5 \times 10^{-3}) = \vec{F}_{ave} = 9000 \text{ N } \text{ or } 9 \text{ kN}$$

$$I = \vec{F}_{ave} \Delta t = \text{area}$$

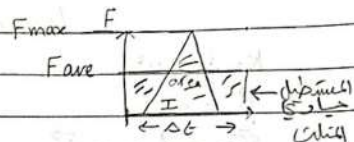


$$I = \text{area} \times \text{width} \quad (\text{مساحة المثلث} \times \text{العرض})$$

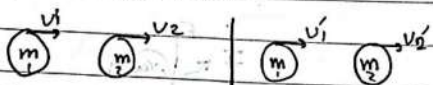
$$= \frac{1}{2} (\Delta t) (F_{\text{max}})$$

$$I = \text{area} \times \text{width}$$

$$(\Delta t) (F_{\text{ave}}) = F_{\text{max}} \times F_{\text{ave}}$$



1) Elastic Collision:



$$\Sigma p$$

$$m_1 v_1 + m_2 v_2$$

$$\Sigma K$$

$$\frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2$$

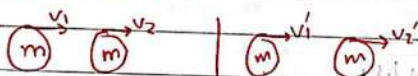
$$= \Sigma p'$$

$$= m_1 v_1' + m_2 v_2'$$

$$\Sigma K'$$

$$\frac{1}{2} m_1 v_1'^2 + \frac{1}{2} m_2 v_2'^2$$

2) Inelastic Collision:

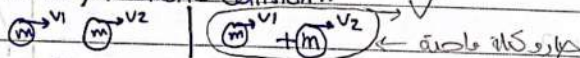


$$\Sigma p = \Sigma p'$$

$$m_1 v_1 + m_2 v_2 = m_1 v_1' + m_2 v_2'$$

$$\Sigma K \neq \Sigma K'$$

3) perfectly Inelastic Collision:



$$\Sigma p = \Sigma p'$$

$$m_1 v_1 + m_2 v_2 = (m_1 + m_2) V$$

$$\Sigma K \neq \Sigma K'$$

Exel elastic Collision::

$m_1 = 8\text{K}, v_1 = 5\text{m/s} / m_2 = 2\text{Kg}, v_2 = 3\text{m/s}$, Find v_1' and v_2' ?

$$\Sigma p = \Sigma p'$$

$$\Sigma K = \Sigma K'$$

$$m_1 v_1 + m_2 v_2 = m_1 v_1' + m_2 v_2'$$

$$\frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2 = \frac{1}{2} m_1 v_1'^2 + \frac{1}{2} m_2 v_2'^2$$

$$8 \cdot 5 + 2 \cdot 3 = 8 v_1' + 2 v_2'$$

$$\frac{1}{2} (8) (5)^2 + \frac{1}{2} (2) (3)^2 = \frac{1}{2} (8) v_1'^2 + \frac{1}{2} (2) (v_2')^2$$

$$2 \div 46 = 8 v_1' + 2 v_2' \leftarrow [1]$$

$$109 = 4 v_1'^2 + v_2'^2 \leftarrow [2]$$

$$2 \div 109 = 4 v_1'^2 + v_2'^2 \leftarrow [2]$$

$$23 = 4 v_1' + v_2'$$

$$v_2' = 23 - 4 v_1' \leftarrow [3]$$

$$[3] \rightarrow [2]$$

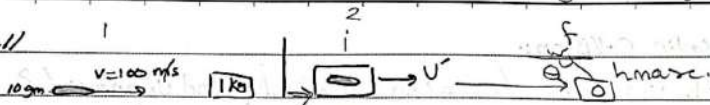
$$109 = 4 v_1'^2 (23 - 4 v_1')^2$$

$$109 = 4 v_1'^2 + 529 - 184 v_1' + 16 v_1'^2$$

$$20 v_1'^2 - 184 v_1' + 420 = 0$$

$$v_1' = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Ex 11



$$\Sigma p = \Sigma p'$$

$$m_1 v_1 + m_2 v_2 = (m_1 + m_2) v'$$

$$\frac{10}{100} \times 100 + 1 \times 0 = (1 + 0.01) v'$$

$$1 = 1.01 v'$$

$$v' = \frac{1}{1.01} = 0.99 \text{ m/s}$$

4- 2 - 3

$$K_i + U_{g_i} = K_f + U_{g_f}$$

$$\frac{1}{2} (m_1 + m_2) v'^2 = (m_1 + m_2) g h_{\text{max}}$$

$$\frac{1}{2} \cdot (0.99)^2 = 10 h_{\text{max}}$$

$$0.49 = 10 h_{\text{max}}$$

$$h_{\text{max}} = 0.049 \text{ m} \approx 4.9 \text{ cm}$$

$$1 - 0.049 = 0.951$$

$$\cos^{-1}(0.951)$$

$$\theta = 18^\circ$$

