

# الإمبراطور

في

## الخرسانة المسلحة 1

عز الدين عاشور



**Civilittee**

اللجنة الأكاديمية لقسم الهندسة المدنية

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## بسم الله الرحمن الرحيم

الدوسية الاتية دوسية الخرسانة المسلحة واحد  
عبارة عن المحاضرات الصفية بالترتيب للدكتور بلال أبو الفول ...  
بالإضافة إلى شرح لشرح الدكتور وتلخيص لأساليب الحل  
وبعض النصائح إضافة لبعض أسئلة السنوات المضافة لمادة  
الفيرست أما مادة سنوات مادة السكند والفينل سيتم تزويدها  
بمرفق خارجي لاحقا ...

إضافة للتعديلات الطفيفة على المادة التي حصلت في اخر  
فصل ...

الرجاء التنبه وعدم الاتباع العمياني للدوسية فكل بني ادم  
خطاء ...

كل تمنياتي لكم بالتوفيق والسداد  
والله يرزقكم الـ +A كل الحب لكم

عز الدين عاشور

للاستفسار عن أي شيء غير واضح بالدوسية تواصل معي عبر  
الفييس

<https://www.facebook.com/ezrawille>

## Advantages of concrete

- 1) Relatively low cost material
- 2) Fire resistance 1 to 3 hours without special fire proofing
- 3) Suitability of material for structural and architectural functions
- 4) Rigidity
- 5) availability of material

## disadvantages of concrete

- 1) Low tensile strength
- 2) Forms and shoring → يتطلب extra time and work
- 3) Relatively low strength per unite weight or unite vloume
- 4) Time dependent Volume changes → Drying Shrinkage due to Hydration  
→ Creep (Deformation under sustained load)

## Sources of Uncertainty

كلما زادت الـ  
Safety Factor زاد الـ

- 1) Actual load magnitude and distribution may differ from assumed in the design
- 2) Asumption and simplification in the analysis may result in different internal forces
- 3) Aactual behavior may be different
- 4) Actualmember Dimension may differ from those in the desing
- 5) Reinforcement may not be in its proper position
- 6) Actual material strength may be different from specified in the design

$$\text{Safety Philosophy}$$
$$\Phi S_n \geq \gamma Q_d$$

Q : strength reductin factor < 1 (always)

$\gamma$  : Over load factor > 1 but it can be < 1 (not always more than 1) م

S<sub>n</sub>: nominal strength

Q<sub>d</sub> : design load or actual load or unfactoral load

## Load factor and combination per ACI code

$$U = (1.2)DL + (1.6)LL$$

Principle Variable load

$$U = (0.9)DL + (1.6)WL$$

Combination action variable load

DL : Dead load مثل وزن المبنى

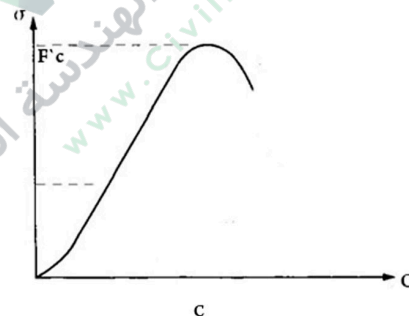
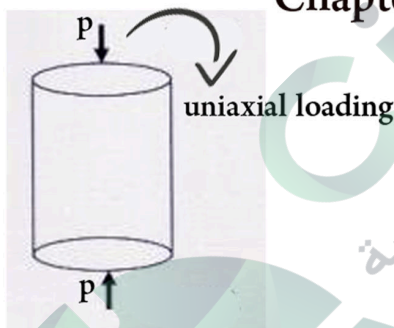
LL : Live load

U : ultimate load

في المعادلة الثانية أصبح الـ safety للـ 0.9 DL (ليش قللنا لما صار مع الـ wind) لأن تأثير DL عمودي بينما WL أفقي فالـ combination أقل

لماذا الـ safety للـ DL أقل من الـ LL؟ لأن DL ثابت تقريباً أما الـ LL ممكن يتغير

## Chapter 2 : (Materials)



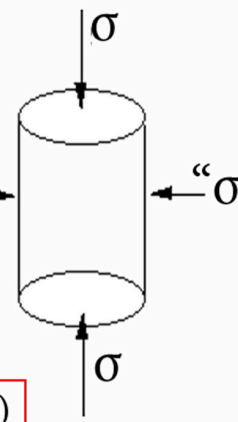
Stages of micro loading and failure in concrete subject to uniaxial loading :

- 1-Shrinkage of the paste during hydration -No load bond cracks بين الـ paste والـ agg
- 2-At stresses up to 30% to 40% of compressive strength → Bond Cracks  
حولين جزيئات الـ agg
- 3-Discontinuity Limit at stresses up to 60% of compressive strength (Mortar Cracks) بين جزيئات الـ agg  
بعد ذلك يبدأ → stable crack propagation
- 4-Critical stress At 75% of the Ultimate load عندها No. of Mortar Cracks increase  
حتى لو أوقفت القوة المؤثرة لن تتوقف التشققات بعد هذه المرحلة  
→ Unstable crack propagation → Fewer undamaged portions  
to carry the load

## Triaxial loading

Confining Stress

Gives more stress than Uniaxial because confining resist indirect stress that try tp spill the sample



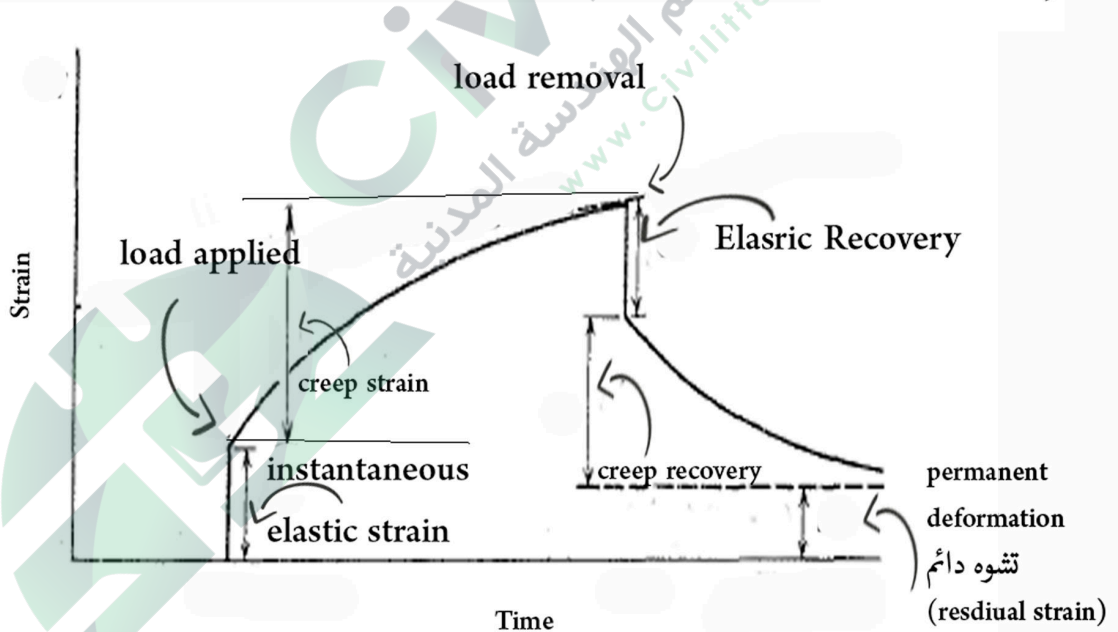
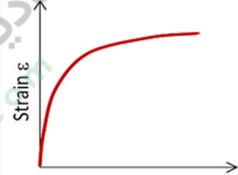
Compressive stress الازداد Confining stress كلما زاد (مهم)

Comp stress ال Confining stress يقاوم ال Tension الناتج من ال

Time dependent Volume Changes → Shrinkage

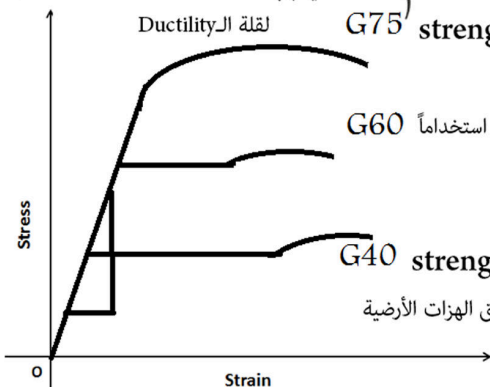
→ Creep (لما يكون عندي Strain with time)

## Creep Test



## Reinforcement

قد يسبب sudden failure  
لقلّة ال Ductility



G75 strength أعلى و ductility أقل

G60 الأكثر استخداماً

G40 strength أقل و أعلى ductility

يستخدم في مناطق الهزات الأرضية

كلهم الهم نفس ال modulus of elasticity

يطبق Hooks law

$$\sigma = \epsilon \times E$$

فقط في منطقة ال elastic region

## Chapter Three

### The design process

**Objectives Of Design** -Structure Should Satisfy

1-Appropriateness : Designed to serve it intended use

2-Economy : overall Cost should not exceeds client's budget

3-Structure Adquency (كفاءة) :be strong enough to support al anticipated loads <sup>متوقع</sup> and it should not diflect , tilt ميلان ,vibrate or crack in a way that affects its usefullness

4-maintainability الصيانة :Minimum and simple maintence procdure

### The Design process

Phase 1 :Defining client's needs and priorites

Phase 2 :Development of project Concept → Preliminary cost estimates

→ No. of possible Layouts

Phase 3 :Design of indivdual systems

Structural Saftey : sources of uncertainty تضاف للسابقة sources

consequences of failure : -loss of life -cost of clearing depris

- cost to society in lost time

### Limit State and the Design of Reinforced concrete

**limit state** : When a structure or an element become unfit for it intended use  
it said it reached the limit state

## Groups of limit state

**1-Ultimate limit state** : structure collapse of part or all the structure

Examples : 1-loss of equilibrium    2-Rupture of critical parts of the structure  
 3-Progressive collapse انهيار تدريجي    4-instability due to deformation (buckling)  
 5-fatigue سببه لوود متكرر    6-formation of plastic mechanism

**2-servicability limit state** : Involves disruption of the functional use of the structure

Examples : 1-excessive deflection    2-undesirable vibration    3-excessive crack width  
 مثل تعطل سكة الحديد

**3-Special limit state** : involves damage or failure due to abnormal conditions

1-extreme earthquakes    2-fire    3-explosions    4-vehicular collisions  
 انتبه الزلازل المتوقع حدوثه وليست ال extreme تقع ضمن Ultimate limit state وليس special

limit state design process

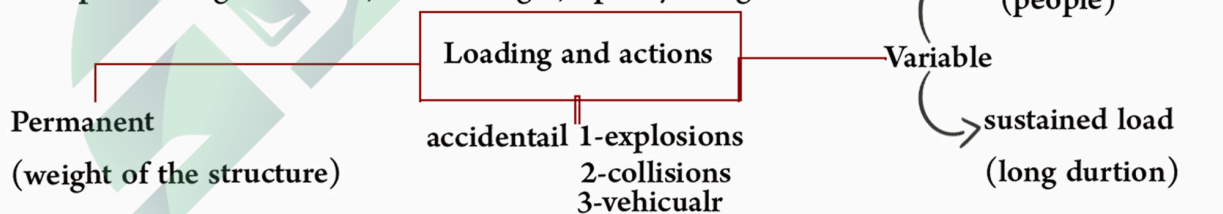
- identification of all anticipated modes of failure
- Determination of all acceptable level of safety per ACI code

Design process specified in ACI code

1-strength design  $\Phi S_n \geq \gamma Q_d$

2-Working stress design  $\Phi S_n \geq Q_d$   
 working load or structural load

3-plastic design method ,limit design ,capacity design



## Chapter Four

### Flexural basic concept (Rectangular beam)

$$\Phi M_n \geq M_u$$

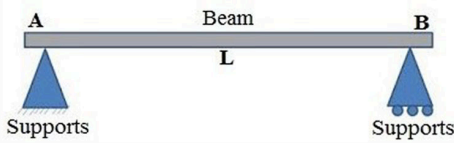
ملاحظة :

Beam----->يتعرض flexural and shear  
coloumns ->يتعرض- axial and bending

$\Phi$  : strength reduction factor ( يتراوح بين 0.6 و 0.9 )  
 $\Phi M_n$  : Design moment capacity  
 $M_n$  : nominal moment capacity  
 $M_u$  : Required ultimate moment

مهم جدا تكون عارف هاي المعلومات

#### simply supported beam



$$M_u = \frac{wL^2}{8} \quad \text{ماكس مومنت}$$

$$V_{MAX} = \frac{wL}{2} \quad \text{ماكس شير}$$

مومنت موجب والتسليح سفلي

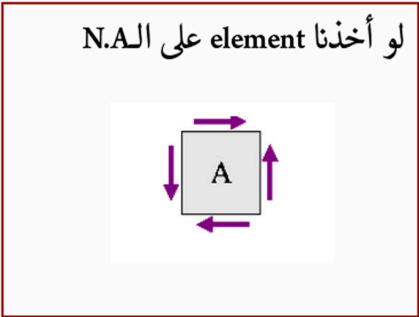
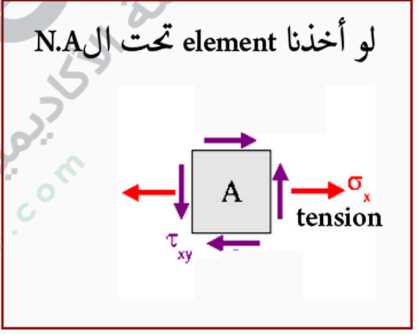
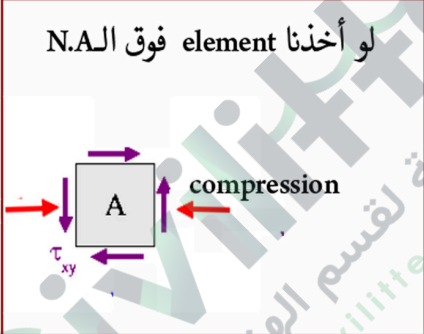
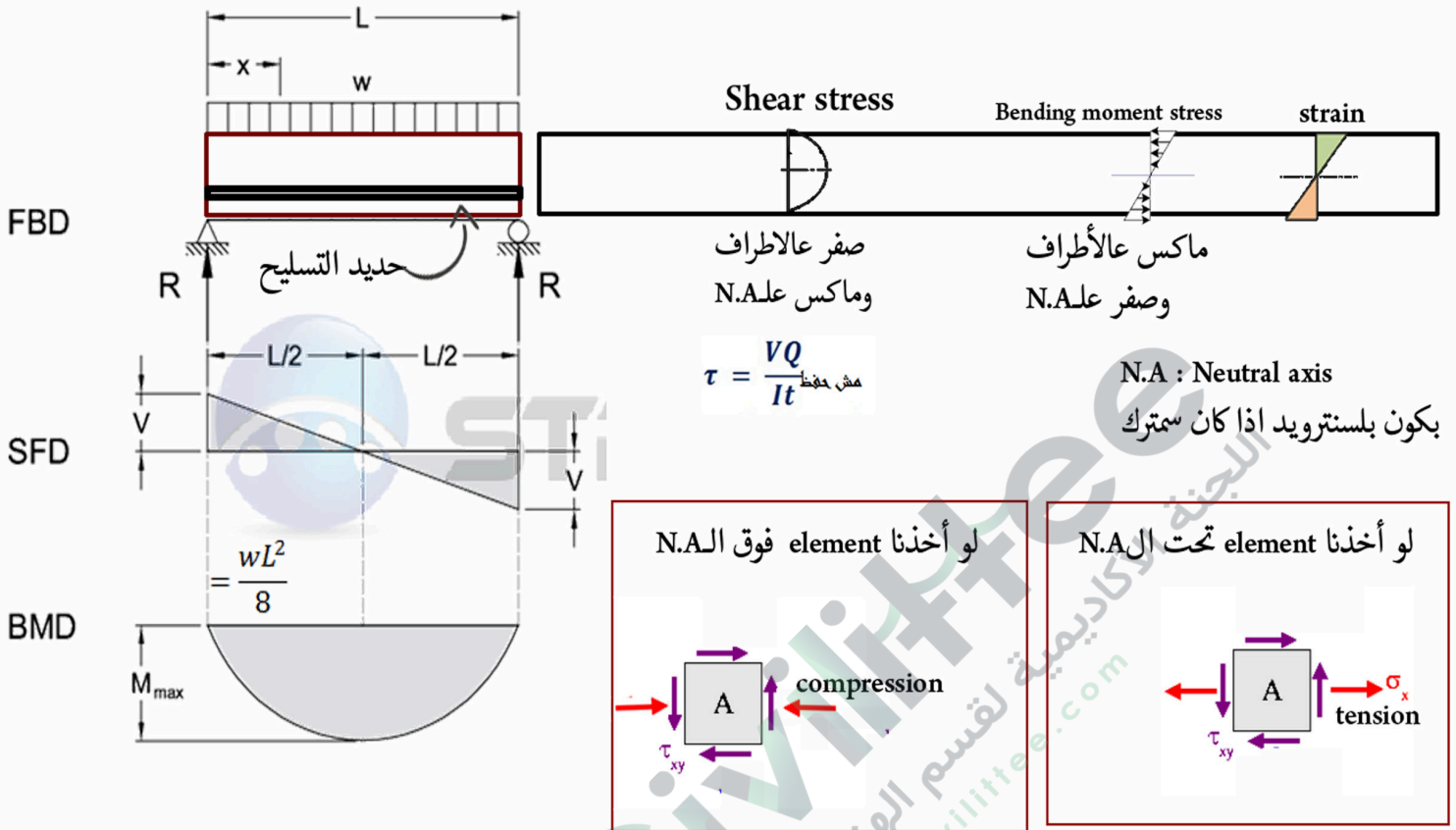
#### Cantilever



$$M_u = \frac{wL^2}{2} \quad \text{ماكس مومنت}$$

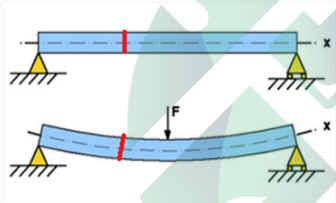
$$V = wL \quad \text{ماكس شير}$$

مومنت سالب والتسليح علوي



### Basic assumption in flexural theory

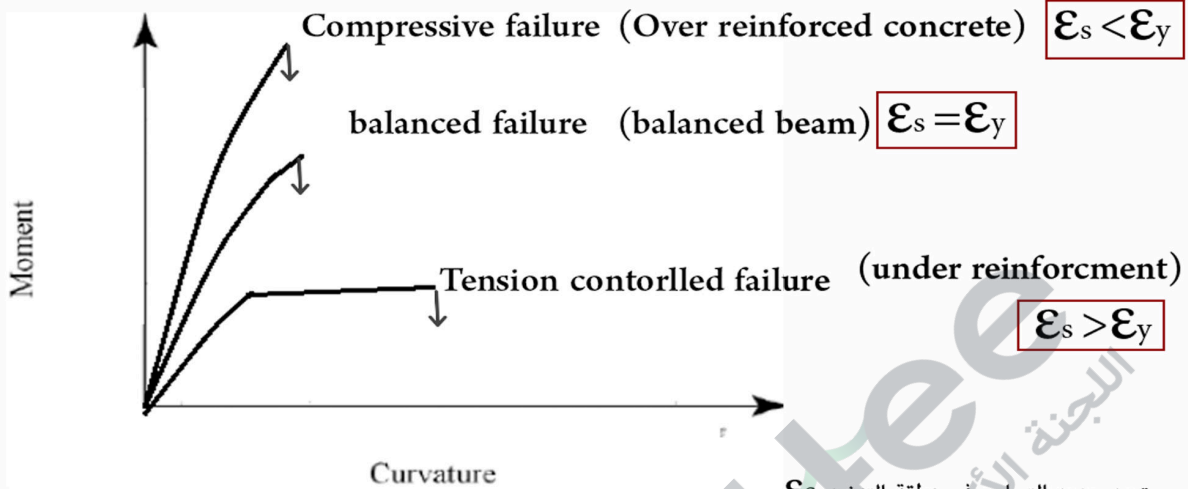
1-Sections perpendicular to the axis of bending that are planes before bending remains planes after bending



- 2-strain reinforcement = Strain of the concrete at the same level (perfect bonding)
- 3-tensile strength of concrete is neglected in flexural calculations
- 4-Concrete is assumed to fail when the maximum compressive strain reaches a limiting value

$$\epsilon_{cu} = 0.003$$

## Flexural failure may occur in three ways



سترين حديد التسليح في منطقة التشن  $\epsilon_s$

$\epsilon_c = \epsilon_{cu} = 0.003$  (الذي يحدد أن البيم وصل لل failure)

إياك تخربط بين  $\epsilon_c$  و  $\epsilon_y$  أوعى تحكيالي  $\epsilon_y = 0.003$

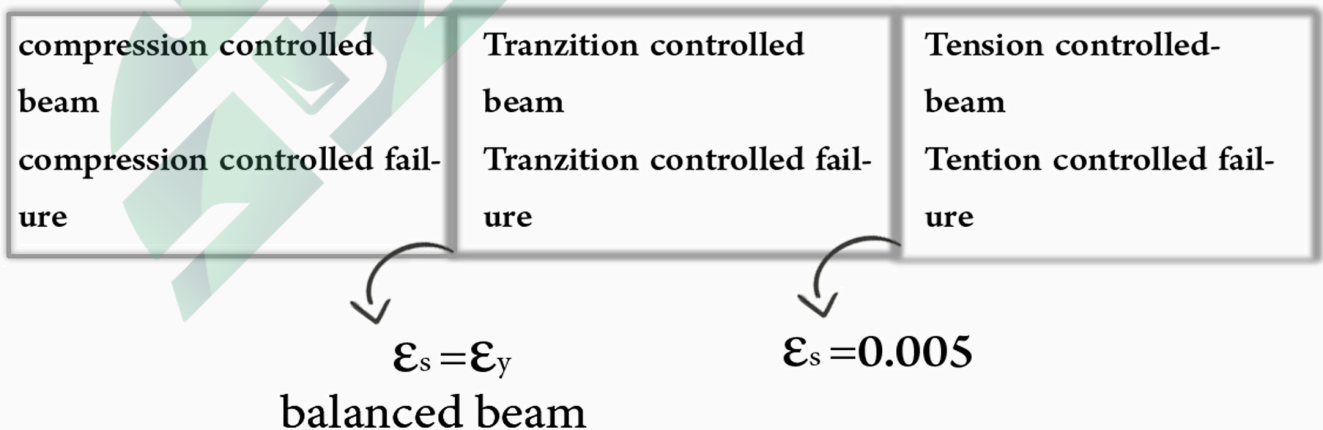
انتبه سؤال F و T

Over reinforced beam means that the beam has more reinforcement than required

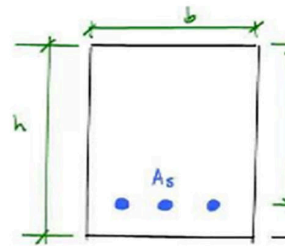
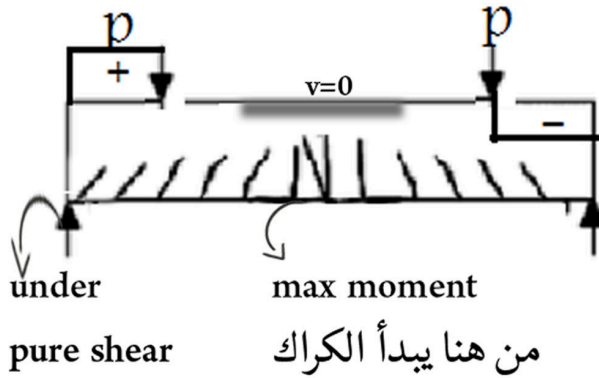
False

## Strain limit method for analysis and design

there are four types of beams depending on anticipated modes of failure



# Flexural behavior



الكراك بزواية 45 هنا

beams failed as a result of the crushing of concrete at the top of the beam

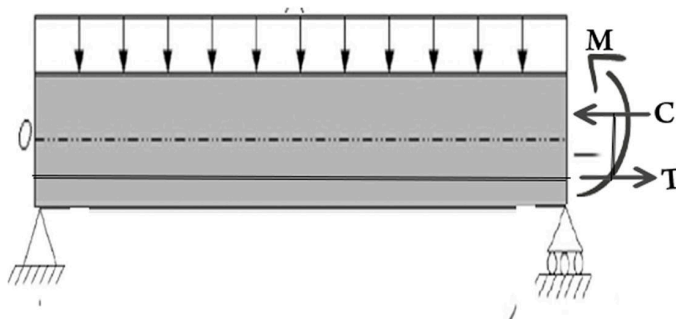
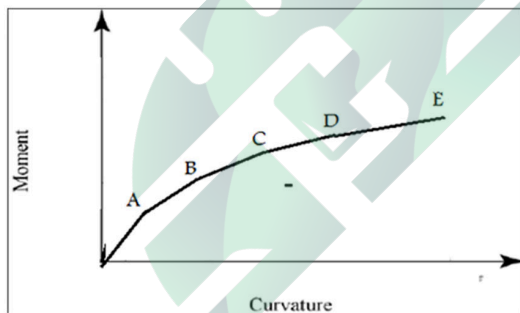
**Stage A** : before cracking

**Stage B** : Cracking (Start from the max moment)

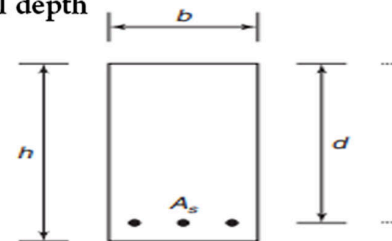
**Stage C** : After cracking before yielding of reinforcement when stress transmit from concrete to steel there will be micro cracking

**Stage D** : yielding of reinforcement curvature increase rapidly with very little increase in moment من أسباب تسليح المنطقة العلوية

**Stage E** : Failure



$h$  : over all depth

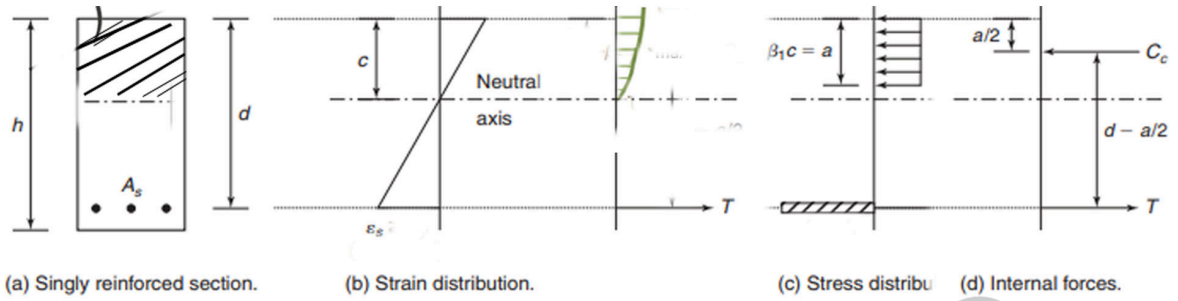


$d$ : effective depth

من منتصف حديد التسليح لآخر البيم فوق

Internal forces

المسافة بين C و T اسمها moment arm



$$\epsilon_s = 0.003 \left( \frac{d - c}{c} \right)$$

$C_c$  ,  $0.85 f'_c$  assumed to be easy with calculations and it calls equivalent stress block

مهم بيحي سؤال دائره

$$C_c = 0.85 f'_c b a$$

$$T_s = A_s f_s$$

If  $\epsilon_s < \epsilon_y$  then  $f_s = E \epsilon_s$

If  $\epsilon_s > \epsilon_y$  then  $f_s = f_y$

$$a = \beta c$$

قيمة  $\Phi$  (حسب قيمة  $\epsilon_s$ )

قيمة  $\beta$  (حسب  $f'_c$ )

$$\Phi = 0.9 \quad \text{if } \epsilon_s \geq 0.005$$

(tension controlled)

$$\beta = 0.85 \quad \text{if } f'_c \leq 28 \text{Mpa}$$

$$\Phi = 0.65 + (\epsilon_s - 0.002) 250/3$$

if  $\epsilon_y < \epsilon_s < 0.005$   
(Tranziton)

المعادلة مش حفظ

$$\beta = 0.85 - 0.05(f'_c - 28/7)$$

if  $28 \text{Mpa} < f'_c \leq 56 \text{Mpa}$

$$\Phi = 0.65 \quad \text{if } \epsilon_s \leq \epsilon_y$$

(Compression and balanced)

$$\beta = 0.65 \quad \text{if } f'_c > 56 \text{Mpa}$$

## Minimum amount of Tension reinforcement


مصطلحات بتفيدك :

$$A_s \text{ min (Larger of)} = \frac{0.25\sqrt{f'_c}}{f_y} b_w d,$$

$$= \frac{1.4b_w d}{f_y}$$

لما يكون عندي min باخذ الـ larger of  
ولما يكون عندي max باخذ الـ smaller of

rectangular beams الـ b w = b

أما بالـ T يميز 

مهم : وضعت هذه الكميات  $A_s \text{ min}$  لأنه عند انتقال اللود من Concrete للـ steel يكون مفاجيء Sudden لذلك وضعت من أجل

To guarantee safe transfer of tension force (مليون خط تحت tension) from

Concrete to Steel

نعوض كل من الاتي بالوحد الاتية : (لا تحول)

Mpa بالـ  $f'_c$

mm بالـ b

Mpa بالـ  $f_y$  والـ mm<sup>2</sup> بالـ  $A_s$

خطوات حل سؤال الـ analysis (إفهم ولا تحفظ)

(1) نفرض أن  $\epsilon_s > \epsilon_y$  وبالتالي  $f_s = f_y$

(2) نسوي (T=Cc) <----- ( $0.85f'_c ab = A_s f_y$ )

دخلها بالالة الحاسبة كمعادلة بمجهول x لإيجاد a رح تطلع a بوحد mm

(3) نجد C من المعادلة فوق وانتبه لقيمة بيتا حسب  $f'_c$  ثم نجد  $\epsilon_s$

(4) نتحقق من الفرض تاينا هل ( $\epsilon_s > \epsilon_y$ ) <---- نعم <---- خطوة 5

<---- لا <---- ارجع للخطوة 1 وضع بدل  $f_y$  بـ  $f_s$  حيث ( $f_s = E \epsilon_s$ )

ثم جد c و a وشيك لـ  $\epsilon_s$  للتأكد لازم تطلع  $\epsilon_s < \epsilon_y$

ملاحظة لما تستخدم  $f_s$  رح يكون قيمة c مجهولة فيها بالتالي بصير معك معادلة بمجهول C على الطرفين استخدم الالة الحاسبة لحل معادلة الهذي بدون ما تنقل شي ولا تحفظ المعادلة التربيعية الي رح يكتبها الدكتور عوض قيمة  $E = 200 \times 10^3$  بهذا الشكل بالمعادلة حتى تطلع c بالـ mm

$$(A_s * E * 0.003 (d-c)/c = 0.85 f'_c b * c * \beta)$$

(5) نجد  $M_n$  حيث ( $M_n =$  إحدى القوتين في المسافة بينهما)

$$M_n = T \left( d - \frac{a}{2} \right) = C_c \left( d - \frac{a}{2} \right)$$

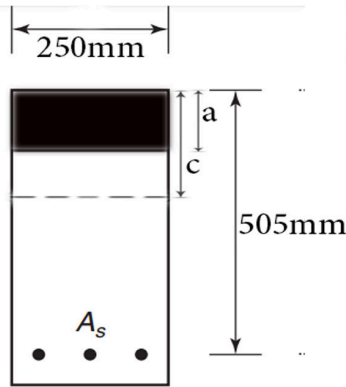
في حالة Rectangular beam

إضرب الناتج  $10^{-6}$  حتى يعطيك بالـ Kn.m

Check  $A_s \text{ min}$  (7)

(6) جد قيمة فاي حسب قيمة  $\epsilon_s$  ثم  $\Phi M_n$

## Example 1



$A_s = 1530 \text{ mm}^2$        $f'_c = 20 \text{ Mpa}$        $f_y = 420 \text{ Mpa}$   
 $E = 200 \text{ Gpa}$       find the design moment capacity

Sol

assume  $\epsilon_s \geq \epsilon_y$  then  $f_s = f_y$

$$T = C_c \rightarrow 0.85 f'_c a b = A_s f_y$$

$$a * 250 * 20 * 0.85 = 420 * 1530$$

$$a = 151.2 \text{ mm} \quad c = a / \beta \quad \text{which } \beta = 0.85$$

$$c = 177.88 \text{ mm}$$

now check  $\epsilon_s \rightarrow \epsilon_s = 0.003 * (d - c) / c$        $\epsilon_s = 0.0055$

check  $\epsilon_y = f_y / E = 420 / (200 * 10^3) = 0.0021$

$\epsilon_s > \epsilon_y$  (yielded) assumption ok

$$M_n = T(d - a/2) = A_s f_y (d - (a/2)) = 1530 * 420 * (505 - 0.5 * 151.2) = 275.9 \text{ Kn.m}$$

حسب قيمة  $\epsilon_s$  كما سبق       $\Phi \epsilon_s > 0.005$        $\Phi = 0.9$        $\Phi M_n = 248.3 \text{ Kn.m}$

Now check  $A_s \text{ min} = 336 \text{ mm}^2$  or  $420 \text{ mm}^2$  (the larger) and  
 $420 < 1530$  then Ok

نفس السؤال السابق ولكن غيرنا  $A_s = 3060 \text{ mm}^2$

$$C_c = T \quad 0.85 f'_c a b = A_s f_y \quad a = 302.4 \text{ mm} \quad c = 355.76 \text{ mm}$$

check  $\epsilon_s = 0.003 * (d - c) / c = 0.001512 < \epsilon_y = 0.0021$

assumption not ok

الآن نرجع للمعادلة  $T = C_c$  ونضع بدل  $f_y$  نضع  $f_s$  حيث  $f_s = E * \epsilon_s$  حيث يكون المجهول بالمعاجلة هو  $c$

$$0.85 f'_c * c * \beta * b = A_s f_s$$

$$c * 0.85 * 250 * 20 * 0.85 = \frac{(505 - c) * 0.003 * 1000 * 200 * 3060}{c} \quad c = 312.65 \text{ mm}$$

$$a = c * 0.85 = 265.76 \text{ mm}$$

دخلها بمجهول  $x$  بدل  $c$  بالالة الحاسبة

$$\epsilon_s = 0.00184 < \epsilon_y \text{ then ok}$$

$$M_n = A_s f_s (d - (a/2)) = \text{or } 0.85 f'_c a * b * (d - (a/2)) = 420 \text{ kn.m}$$

تابع

$$\Phi M_n = M_u \quad \text{ملاحظة}$$

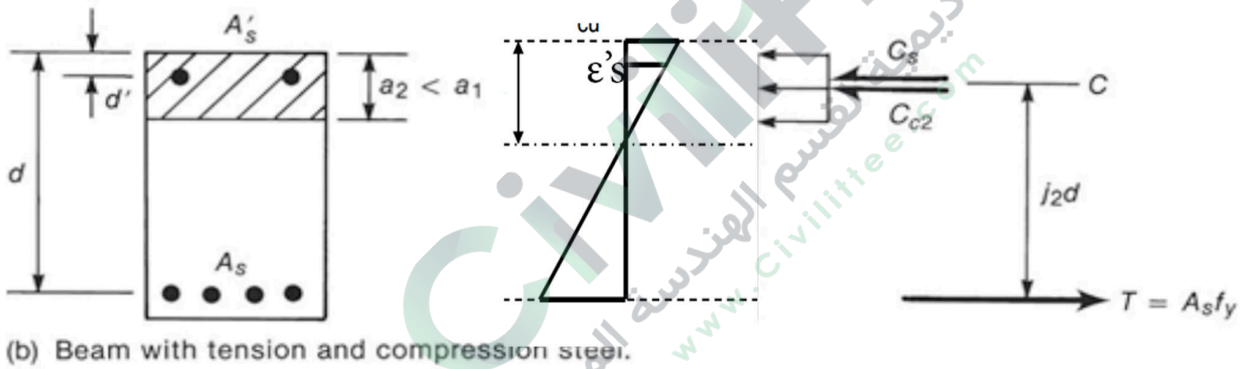
$$W \text{ لو طلب}$$

$$\Phi M_n = \frac{W I^2}{8}$$

$\epsilon_s < \epsilon_y$  then  $\Phi = 0.65$   $\Phi M_n = 273 \text{ Kn.m}$   
 Check  $A_s$  min then ok

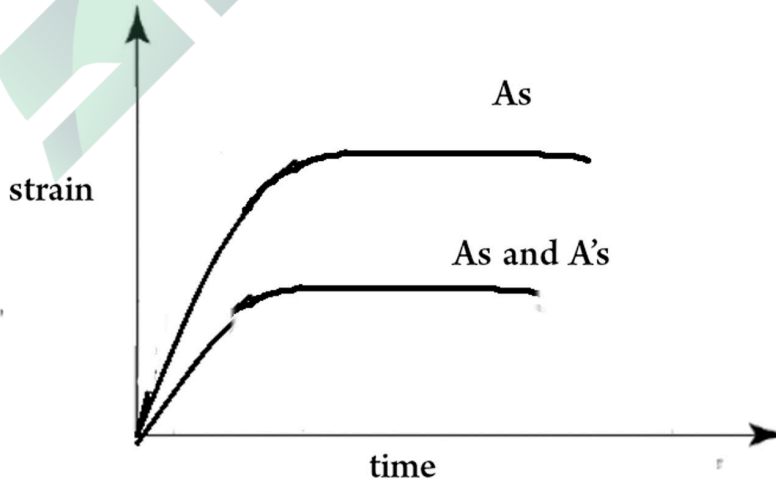
ملاحظات هامة جداً :

زيادة كمية الحديد في منطقة التشن لها (significant effect) على (Mn) nominal moment capacity  
 ولها تأثير قليل على design moment capacity  
 زيادة الحديد تقلل من  $\epsilon_s$   
 زيادة الحديد في منطقة الـ compression كما سترى لاحقاً لها تأثير كبير على الـ design moment capacity ( $\Phi M_n$ )



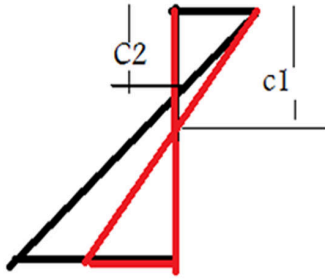
Reasons of doubly rein forcment

1-Reduce sustained load deflection (the creep )



يساعد الخرسانة في منطقة الـ comp على تحمل الضغط بالتالي سيكون الانحناء أقل

## 2-Increase Ductility



C2 : بعد النويترال اكسس في حالة doubly reinforcement

C1 : بعد النويترال اكسس بحالة single reinforcement

حيث أن استخدام الحديد في منطقة الكومبرشن يؤدي لارتفاع N.A. تجاه منطقة الكومبرشن

## 3-change mode of failure

compression

from

balance

to tension controlled due to increase of  $\epsilon_s$

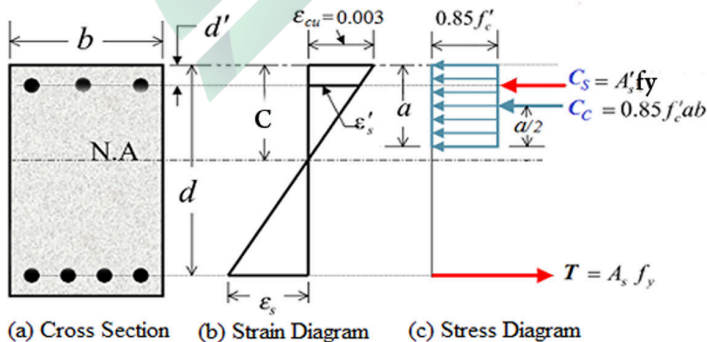
transition

## 4-Fabrication Ease

providing small bars in concrete of the stirrups to hold the steel in place

إذا سلحت منطقة الكومبريشن لأجل هذا السبب فإن قيمة  $A_s'$  تهمل ويعامل البيم كـ single reinforcement

## Analysis of beams with tension and compression reinforcement



$$\epsilon'_s = 0.003 \left( \frac{c - d'}{c} \right)$$

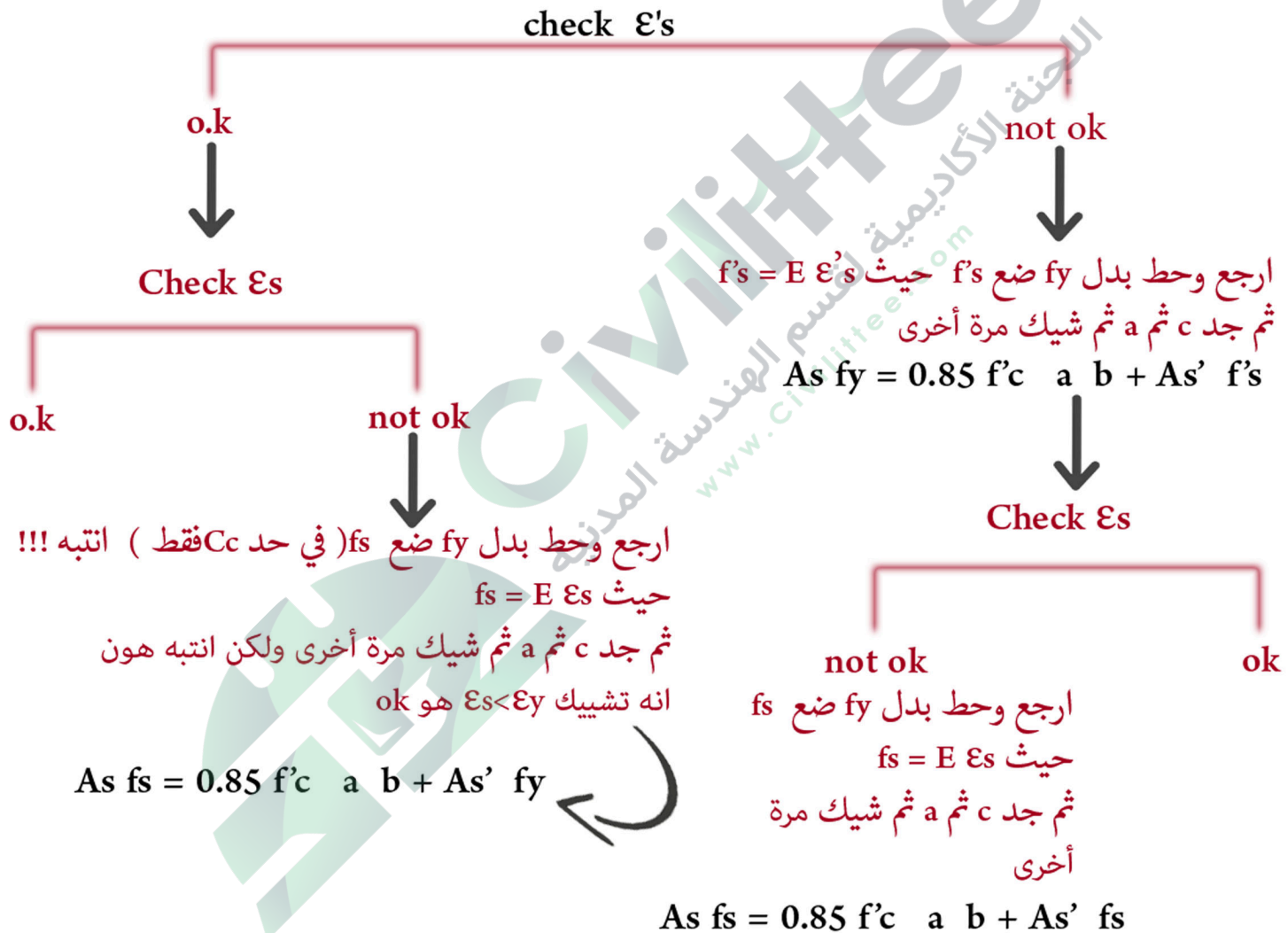
## طرق حل ال Doubly reinforcement

### الطريقة الأولى:

(1) نفرض أن  $\epsilon_s \geq \epsilon_y \rightarrow f_s = f_y$  and  $\epsilon'_s \geq \epsilon_y \rightarrow f'_s = f_y$

(2)  $T = C_s + C_c$  حيث  $f_s = 0.85 f'_c$   $a$   $b$  +  $A_s' f_y$  ثم نجد  $a$  و  $c$

(3) نشيك كالتالي (ركز منيح وافهم فهم تلاقيه سهل)



(4) بعد ما شيكنا وكل شي OK نجد  $M_n = C_c(d - (a/2)) + C_s(d - 65)$   $M_n$  نجد OK

$M_n = 0.85 f'_c ab * (d - (a/2)) + A_s (f'_s \text{ or } f_y) * (d - 65)$

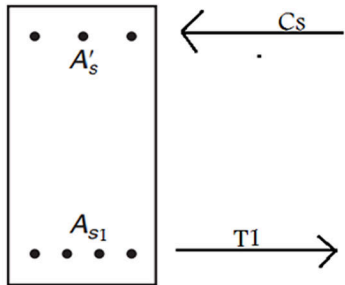
(5) نجد  $\Phi$  (انتبه  $\epsilon'_s$  مالها دخل بنوع ال failure) الذي يحدد نوع ال failure هو  $\epsilon_s$

نجد  $\Phi$  حسب  $\epsilon_s$  ثم  $\Phi M_n$  ثم شيك  $A_s \min$  فقط حيث  $A_s$  مالها  $\min$

## الطريقة الثانية (مهة بالتصميم)

نقسم البيم لقسمين

قسم فيه نهمل في الكونكريت



$$Cs = T1$$

في حالة الاثنين yielded

$$As1 Fy = As' Fy$$

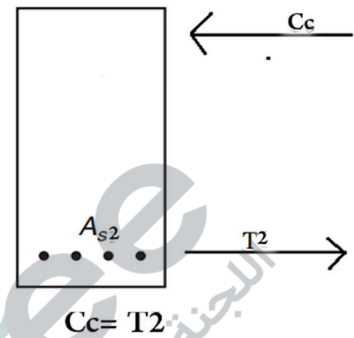
$$\text{then } As1 = As'$$

حيث

$$As = As1 + As2$$

نرجع هون ونجد  $As2$

قسم نهمل فيه الحديد comp



$$Cc = T2$$

$$As Fy = f'c a b 0.85$$

جد  $c$  و  $a$  ثم شبيك  $\epsilon_s$  و  $\epsilon_s$

بعد هيك

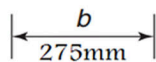
$$\Phi Mn1 = Cs (d-65)$$

$$\Phi Mn2 = 0.85 f'c a b * (d-(a/2))$$

$$\Phi Mn = \Phi Mn1 + \Phi Mn2$$

ثم Check  $As_{min}$

### Example



$$As' = 852 \text{ mm}$$

$$As = 3060 \text{ mm}$$

$$f'c = 20 \text{ Mpa}$$

$$fy = 420 \text{ Mpa}$$

اذا ما أعطاك  $d'$  لازم تعرف انها 65 mm

find desing moment capacity?

Sol : Assume  $\epsilon_s' \geq \epsilon_y$  so that  $f's = fy$

$\epsilon_s \geq \epsilon_y$  so that  $f_s = fy$

$$T = Cs + Cc \quad As fy = As' fy + 0.85 f'c a b$$

$$a = 198 \text{ mm}$$

$$c = 233 \text{ mm}$$

$$\text{check } \epsilon_s' = 0.003(c-d')/c = 0.0022 > \epsilon_y \quad \text{ok}$$

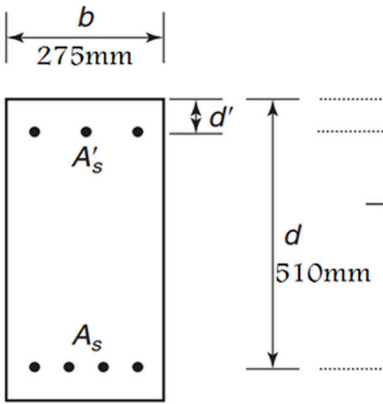
$$\text{check } \epsilon_s = 0.003(d-c)/c = 0.0036 > \epsilon_y \quad \text{ok}$$

$$Mn = Cc(d-0.5*a) + Cs (d-d') = 0.85 f'c a b *(d-0.5*a) + As' Fy (d-65) = 540 \text{ kn.m}$$

$$\epsilon_s = 0.0036 \text{ so } \Phi \text{ حسب العلاقة } \Phi = 0.65 + (0.0036 - 0.002)250/3 = 0.783$$

$$\Phi Mn = 422 \text{ kn.m} \quad \text{now check } As_{min} \text{ take the largest} = 467.5 \text{ mm}^2$$

$As < As_{min}$  then ok



same example with  $A_s' = 1700 \text{ mm}^2$

Assume  $\epsilon_s \geq \epsilon_y$  and  $\epsilon_s' \geq \epsilon_y$

$T = C_c + C_s$  then  $a = 122 \text{ mm}$  and  $c = 143.5$

now check  $\epsilon_s' = 0.0016 > \epsilon_y$  not ok

$$f_s' = \epsilon_s' * E = 200 * 1000 * 0.003 * (c - d') / c$$

$$A_s f_y = 0.85 f_c' \beta c + A_s' * 200 * 1000 * 0.003 * (c - d') / c$$

$$c = 166.55 \text{ mm} \quad a = 141.57 \text{ mm}$$

$$\epsilon_s' = 0.0018 < \epsilon_y \text{ then ok}$$

$$\epsilon_s = 0.0062 > \epsilon_y \text{ then ok}$$

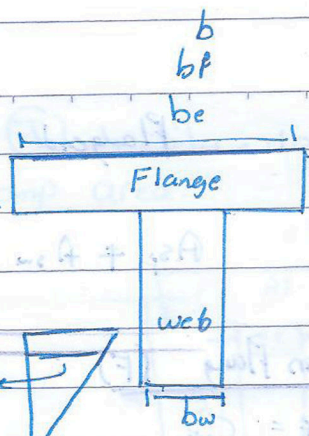
$$M_n = 0.85 f_c' a b (d - 0.5a) + A_s' (f_s') (d - d') = 563.7 \text{ Kn.m}$$

$$\Phi M_n = 507.3 \text{ kn.m}$$

كما تلاحظ زيادة الحديد في منطقة الكومبريشن لها تأثير كبير على القدرة التصميمية

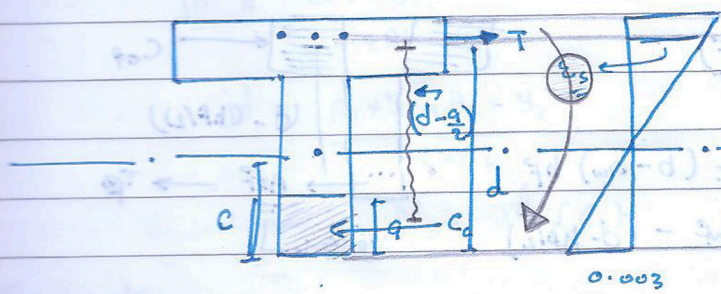
Flexural in T-Beam

(Flange in Tension)  $h_f$



دائراً  
N·A  
الفلنج

Case I:  $\rightarrow$  -ve Moment



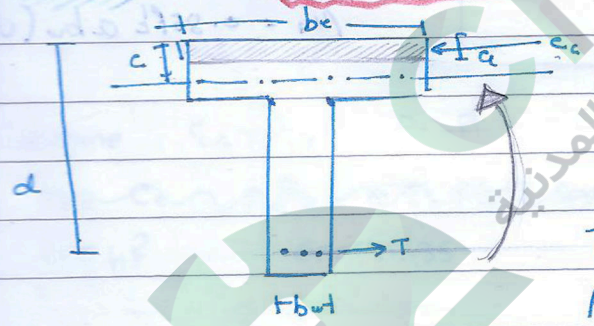
$$T = C_c \rightarrow A_s f_y = 0.85 f'_c a b_w$$

$$M_n = C_c (d - \frac{a}{2})$$

Rectangular beams

Case II: +ve Moment

$a < h_f$



بما أن  $a < h_f$  فلذلك  
Comp. في Rectan. beams  
مثل Rectangular beams

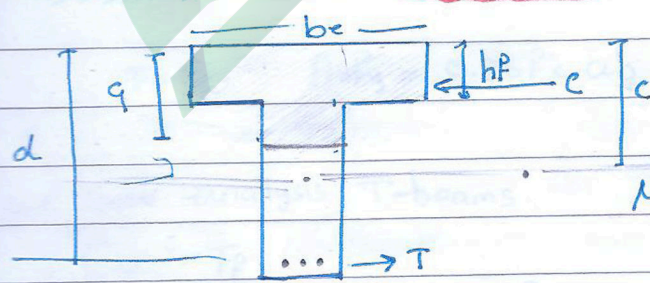
$$T = C_c$$

$$A_s f_y = 0.85 f'_c a b_e$$

$$M_n = C_c (d - \frac{a}{2})$$

Case III: +ve moment

$a > h_f$



$$T = C_c$$

$$A_s f_y = 0.85 f'_c (b_e h_f + b_w (a - h_f))$$

$$M_n = C_c (j d)$$

$\rightarrow$  Not  $(d - \frac{a}{2})$

$$M_n = 0.85 f'_c (b - b_w) h_f (d - \frac{h_f}{2}) + 0.85 f'_c a b_w (d - \frac{a}{2})$$

# طرق حل أسئلة T Beams

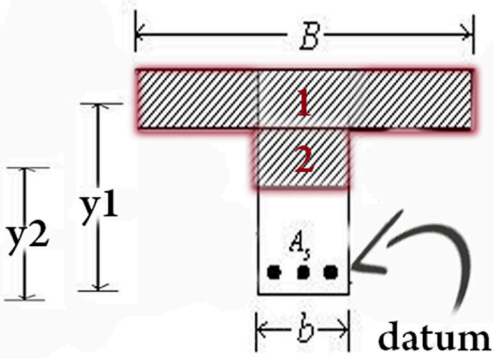
إيجاد السنترويد Jd : الطرق الثانية أفضل

Y1: المسافة من datum لمنتصف المساحة 1

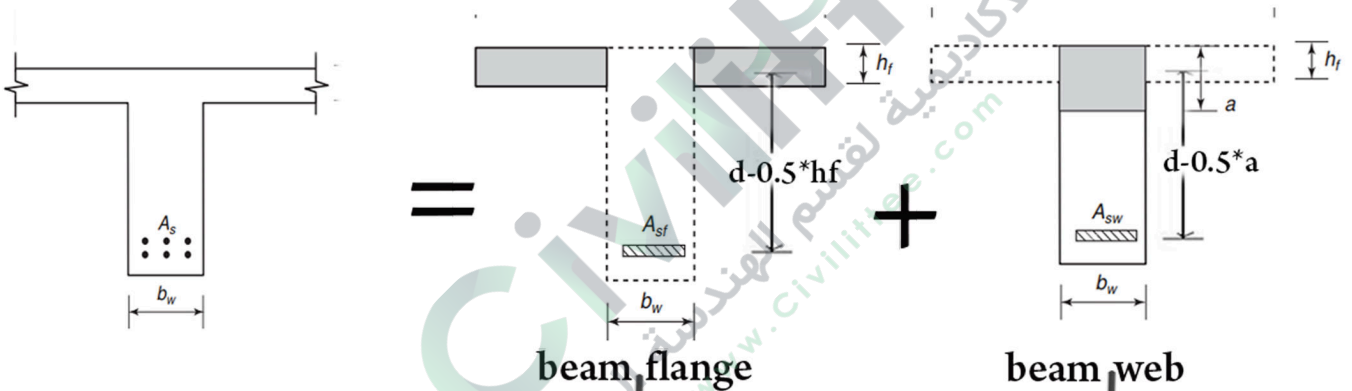
Y2: المسافة من datum لمنتصف المساحة 2

$$jd = \frac{\sum y_i A_i}{\sum A_i}$$

$$jd = \frac{(A_1 y_1 + A_2 y_2)}{(A_1 + A_2)} \text{ then } M_n = T jd$$



## الطريقة الثانية



$$A_{sf} * f_y = 0.85 * f'_c (b - b_w) h_f$$

$$M_{nf} = T_f (d - (h_f/2))$$

$$\text{or } M_{nf} = 0.85 * f'_c (b - b_w) h_f * (d - (h_f/2))$$

$$A_{sw} * f_y = 0.85 * f'_c a b_w$$

$$M_{nw} = 0.85 f'_c a b_w * (d - (a/2))$$

$$\text{Then } M_n = M_{nf} + M_{nw}$$

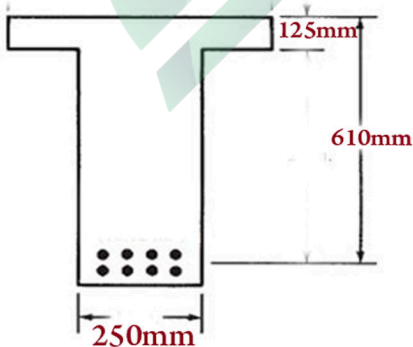
### Example

$$f'_c = 20 \text{ Mpa}$$

$$f_y = 420 \text{ Mpa}$$

$$A_s = 3060 \text{ mm}^2$$

بما أنه حديد التشنن بالأسفل فهو  $v_e+$  مومنت والفلانج تتعرض ل  $comp$  لكن نفرض أول شي أنه  $a < h_f$  ونحل على مثل حل  $rectangular$  beam هكذا :



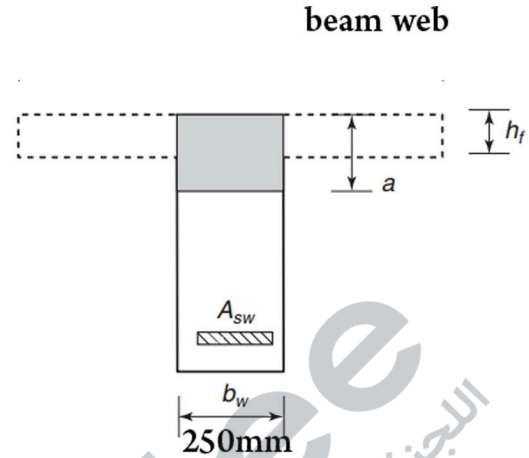
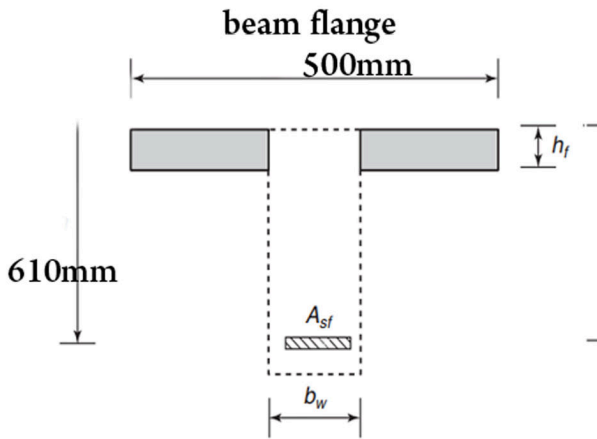
Assume  $\epsilon_s > \epsilon_y$  and  $a < h_f$

$$T = C_c \dots A_s f_y = 0.85 f'_c a b$$

$$a = 151.2 \text{ mm} > h_f \text{ not ok}$$

إذا الان نحل على أساس انه T بيم ونفصل





$$C_{cf} = T_f \quad 0.85 f'c (b-b_w) * h_f = A_{sf} f_y$$

$$A_{sf} = 1264.9 \text{ mm}^2$$

بعد ما أوجدنا  $A_{sf}$  من ييم فلاج

$$A_{sw} = A_s - A_{sf} = 3060 - 1264.9 = 1795.1 \text{ mm}^2$$

$$C_{cw} = T_w$$

$$0.85 f'c a b_w = A_{sw} F_y$$

$$a = 177.4 \text{ mm} \quad \text{and} \quad c = 208.7 \text{ mm}$$

check  $\epsilon_s = 0.0058 > \epsilon_y$  ok

$$M_{nf} = 1264.9 * 420 * (610 - 125/2) = 290.9 \text{ kn.m}$$

$$M_{nw} = 1795.1 * 420 * (610 - 177.4/2) = 393 \text{ kn.m}$$

$$M_n = 290.9 + 393 = 683.9 \text{ kn.m}$$

$$\epsilon_s = 0.0058 > 0.005 \text{ so } \Phi = 0.9$$

$$\Phi M_n = 615.5 \text{ Kn.m}$$

Check  $A_s$  min 406mm<sup>2</sup> or 509mm<sup>2</sup> take the larger and  $A_s > A_{smin}$  then ok

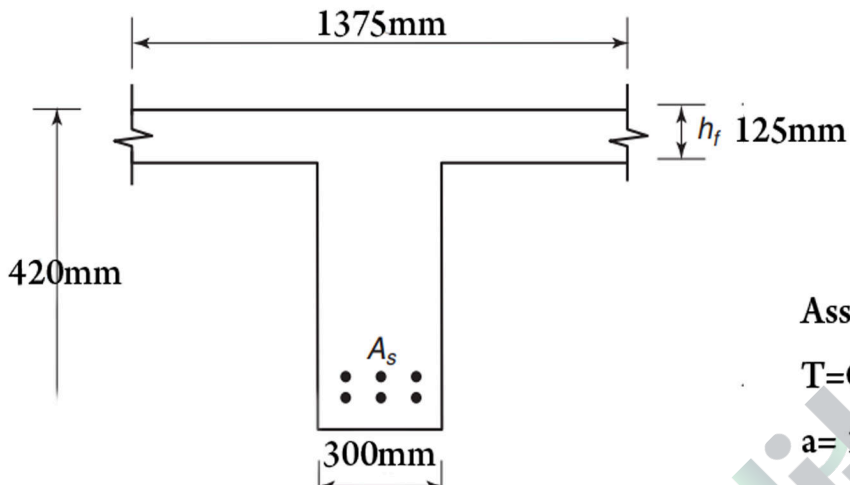
ملاحظة: لما يكون عندي الفلاج بوضع الـ tension يعني حديد الـ tension فوق

نعوض بدل  $b_w$  الأصغر من الاتي  $2b_w$  or  $b_e$  (flange width)

ولكن بشرطين !!

1-flange in tension

2-beam must be statically determined (Cantilever or Simply supported)



$$f'c = 20\text{Mpa}$$

$$Fy = 420\text{ Mpa}$$

$$As = 1704\text{ mm}^2$$

Assume  $\epsilon_s \geq \epsilon_y$   $a \leq h_f$

$$T = Cc \quad As f_y = 0.85 f'c a b$$

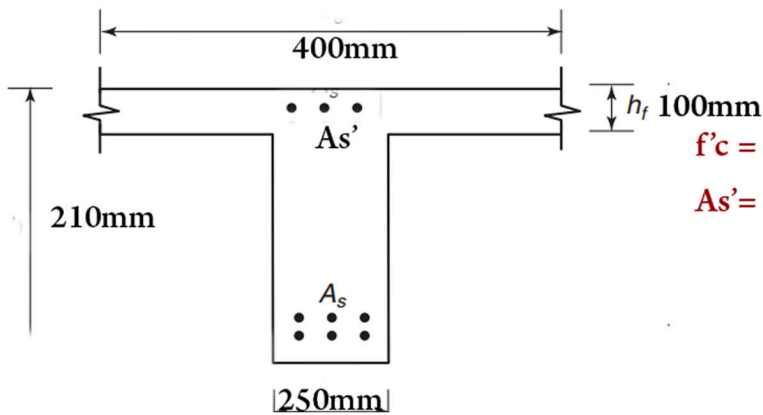
$$a = 21.9\text{ mm} < h_f \text{ ok}$$

$$c = 25.8\text{ mm}$$

$$\epsilon_s = 0.003 * (420 - 25.8) / 25.8 = 0.046 > \epsilon_y \text{ ok}$$

$$M_n = 1704 * 420 * (420 - 21.9/2) = 292.74\text{ kn.m}$$

$$\Phi = 0.9 \quad \Phi M_n = 263.47$$



$$f'_c = 20 \text{ Mpa}$$

$$f_y = 420 \text{ Mpa} \quad A_s = 3060 \text{ mm}^2$$

$$A_s' = 852 \text{ mm}^2$$

$$\epsilon_s \geq \epsilon_y \quad \text{then } F_s = F_y$$

$$\epsilon_s \geq \epsilon_y \quad \text{then } F_s = F_y \quad a \leq h_f$$

$$\epsilon_y = 0.0021 \quad 0.002 = \epsilon_y \quad \text{منه دائما تقريبا}$$

$$F_y = 420 \text{ MPa}$$

$$A_s F_y = 0.85 F'_c b a + A_s' F_y \quad a = 136.4 \text{ mm} < h_f \quad \text{not o.k}$$

$$T = C_c + C_s$$

$$A_s F_y = 0.85 F'_c (b h_f + b_w (a - h_f)) + A_s' F_y$$

$$a = 158.20 \text{ mm}$$

$$c = 186.12 \text{ mm}$$

$$\epsilon'_s = 0.002 < \epsilon_y \quad \text{not o.k}$$

$$A_s F_y = 0.85 F'_c (b h_f + b_w (a - h_f)) + (A_s' \times E \times 0.003 \left(\frac{c - d'}{c}\right))$$

$$c = 191.66 \text{ mm}$$

$$a = 162.911 \text{ mm}$$

$$\epsilon'_s < \epsilon_y$$

$$\text{check } \epsilon_s, \quad \epsilon_s = 0.0003 > \epsilon_y \quad \text{not o.k}$$

$$T = C_c + C_s \quad A_s = (E \times 0.003 \left(\frac{d - c}{c}\right))$$

$$= 0.85 F'_c (b h_f + b_w (0.85c - h_f))$$

$$+ A_s' E \left(0.003 \left(\frac{c - d'}{c}\right)\right)$$

$$c = 158.87 \text{ mm} \quad a = 135.04 \text{ mm}$$

$$M_n = 0.85 F'_c (b - b_w) h_f (d - h_f/2)$$

$$+ 0.85 F'_c (b_w a) (d - a/2)$$

$$+ A_s' F_y (d - d') = 166 \text{ kN.m}$$

$$\phi = 0.65 \quad \phi M_n = 108 \text{ kN.m}$$

$$\text{check } A_{s \text{ min}} \quad 175 \text{ mm}^2$$

## أسئلة True and False

1-increasing the amount of tension reinforcement in any reinforced concrete beam will increase the nominal strength and reduce the ductility **True**

2-the nominal moment capacity of any reinforced concrete beam can be increased significantly by providing reinforcement in the compression side of the section **False**

3-The ACI requires a minimum amount of tension reinforcement to be placed in the beam to guarantee safe transfer of the compression force from concrete to steel after cracking of the concrete before yielding of the reinforcement **False** **التصحيح** in the tension side of tension force

4-In the design safety philosophy for reinforced concrete beams the actual strength is reduced and the design load is increased **True**

5-when concrete is subjected to uniaxial compression the critical stress occurs at 50% to 60% of the ultimate load **False** the correction (75 to 80%)

6-when increasing the confining pressure on concrete subjected to tri-axial loading the compressive strength is expected to decrease **False** Correction (to increase)

7-reinforcement with the highest grade has the highest ductility

**False** correction ( the lowest ductility)

8-economy is considered as one of the design objectives in the design process

**True**

9-if the structure collapses due to fatigue it is said to have reached the ultimate limit state **True**

10-the serviceability limit state involves damage or failure of the part or all the structure due to abnormal conditions **False** Correction (special limit state)

11-Steel reinforcement of grade 40 shows the highest ductility among the other grades

**True**

12-Increasing in the confining pressure on a concrete specimen increases the compressive strength **True**

13-In the uniaxial compressive test on concrete the unstable crack propagation starts at the discontinuity limit **False**

14-In safety design philosophy the strength reduction factor is always less than one and the overload factor is always more than one **False**

15-At the ultimate condition if the tensile strain in reinforcement has not reached the yield strain the beam strain then the beam is called an under - reinforcement beam  
False

16-in beam analysis problems more reduction to the nominal moment capacity is used if the expected mode of failure is tension-controlled

False لأنني بضرب ب 90% بالتشن كونترولد .. يعني الريدكشن قليل (less reduction)

17-rigidity may be considered as one of the advantage of the concrete material  
True

16-Reinforcement grade 60 has more ductility and less strength than grade 75  
True

18-If the structure failed due to progressive collapse due to an explosion it is said to have reached the ultimate limit state  
false

19-Increasing the compressive reinforcement in a doubly reinforced concrete is not expected to have a significant effect on the nominal moment capacity but it might increase the design moment capacity  
True

20-in a creep test for a concrete specimen the elastic recovery occurs at the moment of load application  
False at load removal

21-Increasing the tension reinforcement in a doubly reinforced concrete is expected to have significant effect on the nominal moment capacity but it might decrease the design moment capacity  
True

22-the discontinuity limit occurs at stresses up to 30 to 40% of the compressive strength  
false

23-An over reinforced beam has more reinforcement than required False

24-In a beam analysis problems if the tensile strain in the reinforcement at the ultimate condition is less than the yield strain compressive reinforcement should be used to increase ductility  
False

25-the working stress design procedure based on the unfactored loads True

26-The ACI code requires min area of steel in beam to ensure tension-controlled failure  
False (to ensure safe transmit of tension force from conc to steel)s

1-which of the following is NOT a reason why the equivalent rectangular compressive stress block for concrete is used in the analysis of flexural strength

- A)the actual compressive stress on the concrete section is of a parabolic shape which is difficult to deal with
- b)it gives good approximation to the magnitude and location of the resultant compressive force on the concrete section
- c) It is an exact representation of the compressive stress for concrete

Answer is C

2-which of the following statement is incorrect

- a)when a structure becomes unfit for its intended use it is said to have reached the limit state
- b)Rupture of critical parts of the structure could lead the structure to reach its ultimate limit state
- c)serviceability limit state involves a structural collapse of part or all the structure

Answer is C

3-which of the following statement is incorrect

- A)the actual strength of the structural members will almost always differ from the values calculated by the design
- B)For safe design strength reduction factor is always less than one and the overload factors are always more than one

Answer is b

which of the following is Not a factor affecting the choice of concrete for a structure

- A) Economy , fire resistance and rigidity
- B) suitability of material for architectural and structural functions
- C) Low tensile strength and time dependent volume changes
- D) Availability of materials and low maintenance

Answer is : C

Which of the following statements correctly describes the mortar cracks that develop in concrete due to uniaxial compressive loading

- A) developed before the concrete is loaded due to shrinkage of the paste that occurs during hydration
- B) Develop when concrete is subjected to stresses greater than 30% to 40% of its compressive strength
- c) develops when the load is increased beyond 50 to 60% of the ultimate load

Answer is C

T or F

1-working stress design methodology considers the redistribution of the moments as successive cross sections yield

False

2-the formation of plastic mechanism involves yielding of concrete in the location of maximum bending stress

False

3-when concrete is loaded by compression instantaneous elastic strain develops . If the load remains on the concrete , creep strain develop with time

True

4-the addition of compressive reinforcement to a concrete beam section reduces the compressive force on the concrete and therefore reducing the creep strain

True

5-In flexural theory it is assumed that concrete is assumed to fail when maximum tensile strain reaches a limiting value of 0.003

( false (compressive strain

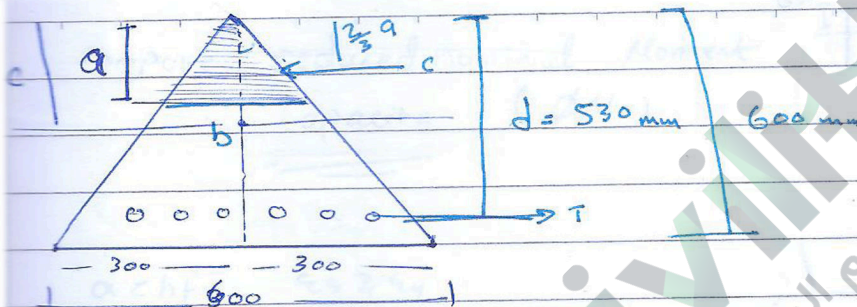
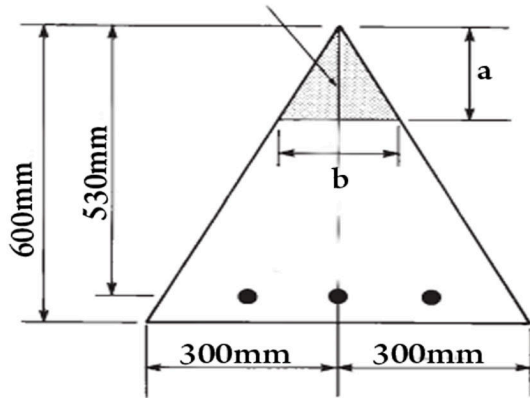
6-The ACI code requires a minimum amount of tension reinforcement in a beam section to guarantee safe transfer of the tensile force from concrete to steel

True



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www.Civilittee.com

$$f'_c = 28 \text{ Mpa} \quad f_y = 420 \text{ Mpa} \quad A_s = 3032 \text{ mm}^2$$



$$f_y = 420 \text{ MPa}$$

$$f'_c = 28 \text{ MPa}$$

$$A_s = 3032 \text{ MPa}$$

$$\frac{\frac{1}{2} b c}{2c} = \frac{b c}{4c}$$

assume  $\epsilon_s \geq \epsilon_y$   $f_s = f_y$

$$T = C_c \rightarrow A_s f_s = 0.85 f'_c \left( \frac{1}{2} b a \right)$$

$$A_s f_y = 0.85 f'_c \left( \frac{1}{2} a^2 \right)$$

$$a = 327 \text{ mm}$$

$$c = 384.7 \text{ mm}$$

$$\frac{300}{\frac{1}{2} b} = \frac{600}{a}$$

$$\epsilon_s = 0.003 \left( \frac{d-c}{c} \right) = 0.0011$$

$$\epsilon_y = 0.0021$$

$$\epsilon_s < \epsilon_y \quad \text{not ok}$$

$$b = \frac{300 a}{0.5(600)}$$

$$a = b$$

$$A_s \cdot E \cdot \epsilon_s = 0.85 f'_c \frac{1}{2} a^2$$

$$a = 318.5 \text{ mm}$$

$$c = 374.7$$

$$\epsilon_s = 0.003 \cdot \frac{d-c}{c} = 0.0012 < \epsilon_y \quad \therefore \text{ok}$$

$$M_n = T \left( d - \frac{2}{3} a \right)$$

$$= 0.85 f'_c \cdot \frac{1}{2} a^2 \cdot \left( d - \frac{2}{3} a \right)$$

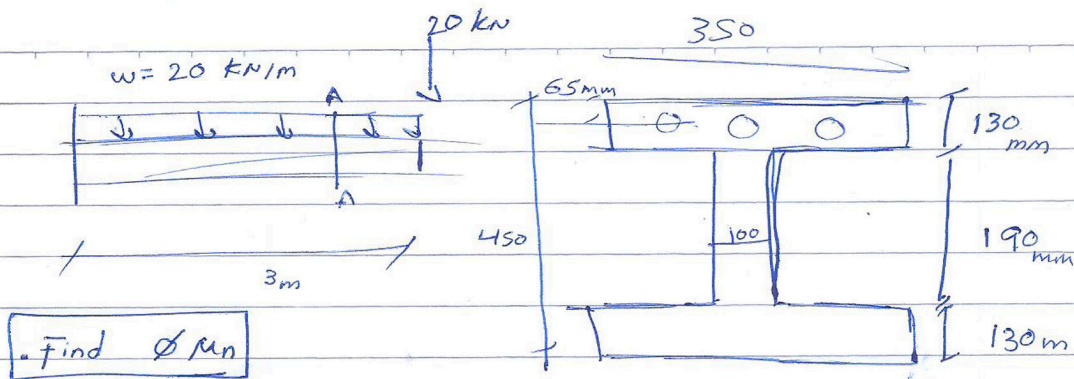
$$= 0.85 \cdot 28 \cdot \frac{1}{2} \cdot (318.5)^2 \cdot \left( 530 - \frac{2}{3} \cdot 318.5 \right)$$

$$= 460.17 \text{ kN.m} \quad \frac{1}{2} a^2$$

$$\phi = 0.65$$

$$\phi M_n = 1179 \text{ kN.m}$$

$$\phi M_n = 299.1 \text{ kN.m}$$



$$\epsilon_s > \epsilon_y \text{ and } a \leq h_f$$

$$A_s = 2413$$

$$f_y = 420$$

$$A_s f_y = 0.85 f_c' \times a \times 350$$

$$f_c' = 25$$

$$a = 136.3 \text{ mm} > h_f \text{ not o.k.}$$

$$A_s f_y = 0.85 f_c' \times (A_c)$$

$$A_c = \text{[Diagram of cross-section]} + \text{[Diagram of cross-section]}$$

$$A_c = (350 - 100)130 + a(100)$$

$$\text{then } a = 151.9 \text{ mm}$$

$$c = 178.73$$

$$d = 385$$

$$\text{check } \epsilon_s = 0.00346 > \epsilon_y \text{ o.k.}$$

$$M_n = 0.85 f_c' (A_c) \times$$

$$M_n = 0.85 \times 25 \left( (350 - 100)130 \right) \times (d - h_f/2)$$

$$+ 0.85 \times 25 \left( a \times 100 \right) \left( d - a/2 \right)$$

$$M_n = 320.76 \text{ kN.m}$$

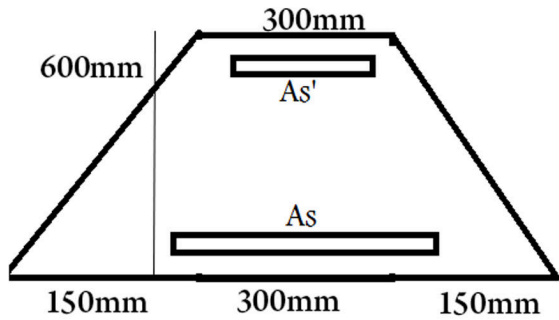
$$\text{لطفة } \phi = 0.9716$$

$$\phi M_n = 247.5 \text{ kN.m}$$

show which beam cross section is adequate to carry the given load

هذا الكلام يعني أنه لازم تجد  $M_u$  ومقارنتها مع  $\phi M_n$  إذا طلعت  $\phi M_n$  أكبر أو تساويها فالجواب yes وإلا No ما قدرت أحله لأن بسؤال السنوات في لود موجود اخر البيم مش مبين قيمته ... لو فرضنا قيمته 20Kn

$$M_u = 20 \times 3 + 60 \times 1.5 = 150 \text{ kN.m}$$



determine the depth of the neutral axis

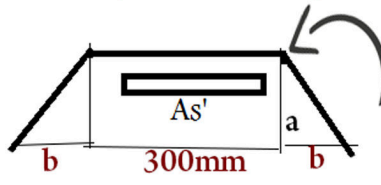
$$f_y = 420 \text{ Mpa} \quad f'_c = 20 \text{ Mpa} \quad A_s = 4020 \text{ mm}^2$$

$$A_{s'} = 852 \text{ mm}^2 \quad d = 535 \text{ mm} \quad d' = 65 \text{ mm}$$

depth of neutral axis is c

$$T = C_c + C_s \quad A_s f_y = 0.85 f'_c (\text{Area}) + A_{s'} F_y$$

Assume  $\epsilon'_s \geq \epsilon_y$  and  $\epsilon_s > \epsilon_y$



Area عبارة عن مساحة مستطيل + مساحة المثلثين  
لكن قاعدة نخليها بدلالة a حتى تصير المجهول الوحيد  
بالمعادلة نجيبها من تشابه المثلثات

$$b = a \cdot 0.25 \quad \frac{a}{b} = \frac{600 \text{ mm}}{150 \text{ mm}}$$

$$\text{Area} = 2 * (0.5 * b * a) + 300 * a = 2 * (0.5 * 0.25 * a * a) + 300 * a$$

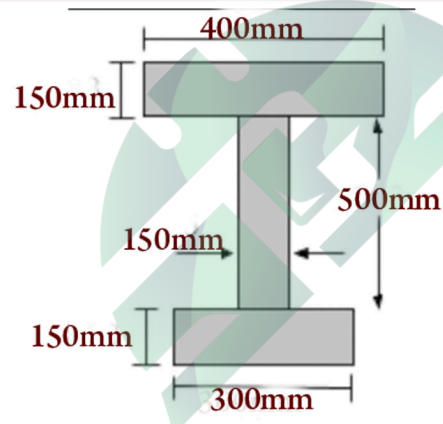
$$A_s f_y = 0.85 f'_c * \text{Area} + A_{s'} F_y \quad \text{معادلة بمجهول}$$

من الآلة الحاسبة

$$a = 220.4 \text{ mm} \quad c = a / 0.85 = 259.3 \text{ mm}$$

Check  $\epsilon'_s = 0.0024 > \epsilon_y$  then ok

check  $\epsilon_s = 0.0032 > \epsilon_y$  then ok



the beam section below is reinforced for negative moment with 1900mm<sup>2</sup> of tension reinforcement and 750 mm<sup>2</sup> of compression reinforcement assuming both tension and compression reinforcement are yielded determine the depth of the assumed equivalent stress block  $f'_c = 25 \text{ Mpa} \quad f_y = 420 \text{ Mpa}$

المطلوب إيجاد a مومنت سالب يعني التشنن فوق

$$d = 150 + 500 + 150 - 65$$

$$735 \text{ mm}$$

assume  $a < h_f \quad \epsilon'_s \geq \epsilon_y$  و  $\epsilon_s > \epsilon_y$

$$T = C_c + C_s \quad A_s f_y = 0.85 f'_c (300 * a) + A_{s'} F_y$$

$$a = 75.76 \text{ mm} < h_f \text{ so ok} \quad c = 89.13 \text{ mm}$$

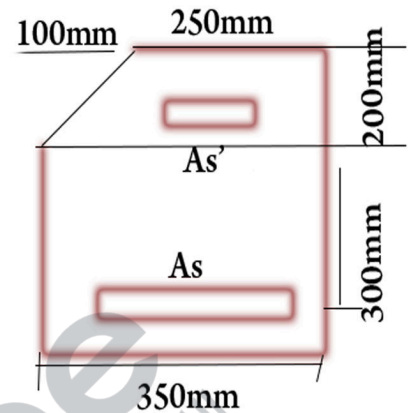
$$\epsilon'_s = 0.0008 < \epsilon_y \text{ not ok} \quad A_s f_y = 0.85 f'_c * c * 0.85 * b + A_{s'} E \cdot 0.003 * (c - 65) / c \quad c = 112.3 \text{ mm}$$

$$a = 95.45 \text{ mm}$$

check  $\epsilon'_s = 0.00126 < \epsilon_y$  ok  $\epsilon_s = 0.0166 > \epsilon_y$  ok

determine the depth of the compression area  $f_y=420 \text{ Mpa}$   $f'_c =30\text{Mpa}$   $A_s=4000\text{mm}^2$

$$A_s' = 500\text{mm} \quad d'=65$$



المطلوب c

Assume  $\epsilon_s' \geq \epsilon_y$  and  $\epsilon_s \geq \epsilon_y$  and  $a < 200$

$$T = C_c + C_s$$

$$A_s F_y = 0.85 f'_c (\text{Area}) + A_s' F_y$$

مساحة المثلث + المستطيل = Area

نفرض قاعدة المثلث b وارتفاعه a

$$a/b = 200/100 \quad b = 0.5a$$

$$\text{Area} = 0.5 * 0.5 * a * a + 250 * a$$

$$A_s F_y = 0.85 f'_c * (0.5 * 0.5 * a * a + 250 * a) + A_s' f_y$$

$$a = 193.24 < 200 \text{ ok}$$

الآن اتبه انه  $f'_c$  فوق 28 لذلك نجب بيتا من القانون

$$\beta = 0.8357 \quad c = 231.23 \text{ mm}$$

$$d = 500$$

check  $\epsilon_s' = 0.00215 > 0.0021$  so ok

check  $\epsilon_s = 0.00348 > \epsilon_y$  so ok

Rectangular beam 300mm width and 550mm effective depth determine the maximum area of tension reinforcement to be placed in the section for it to be a balanced section

$$F_y = 420 \text{ Mpa} \quad f'_c = 35 \text{ Mpa}$$

$$\text{balanced section means } \epsilon_s = 0.0021 = 0.003(550 - c)/c \quad c = 323.53 \text{ mm}$$

$$\text{as } f'_c > 28 \text{ and } < 56 \text{ we get } \beta \text{ from the equation } \beta = 0.8 \quad a = 258.82 \text{ mm}$$

$$A_s F_y = 0.85 f'_c a b \quad A_s = 5499.9 \text{ mm}^2$$

$$f'_c = 28 \text{ MPa} \quad f_y = 420 \text{ MPa}$$

A.  $\phi M_n$ ? in a single reinforcement beam

$$A_s' = 0 \quad A_s = 4210 \text{ mm}^2$$

assume

$$\epsilon_s \geq \epsilon_y \quad f_s = f_y$$

$$T = C_c \rightarrow A_s f_y = 0.85 f'_c \times a \times b$$

$$4210 \times 420 = 0.85 \times 28 \times a \times 400$$

$$a = 185.73 \text{ mm}$$

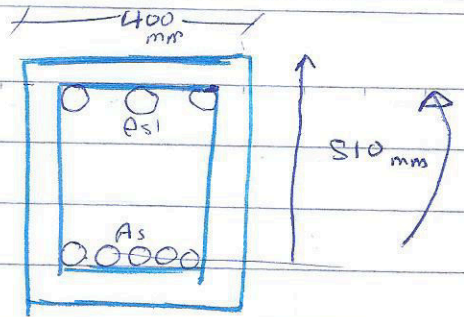
$$c = 218.5 \text{ mm}$$

$$\epsilon_s = 0.003 \times \left( \frac{d-c}{c} \right) = 0.0047 > 0.002 \quad \therefore \text{o.k.}$$

$$M_n = 0.85 \times 28 \times 185.73 \times 400 \times \left( 510 - \frac{185.73}{2} \right)$$

$$= 737.5 \text{ kNm}$$

$$\phi = \text{جبرية} = 0.82 \quad \phi M_n = 604.79 \text{ kNm}$$



b. compute c? (doubly reinforcement)

$$A_s' = 995 \text{ mm}^2$$

$$A_s = 4640 \text{ mm}^2$$

$$\epsilon_s \geq \epsilon_y \quad \epsilon_s \geq \epsilon_y$$

$$T = C_c + C_s \rightarrow A_s f_y = 0.85 f'_c \times a \times b + A_s' f_y$$

$$a = 160.8 \text{ mm}$$

$$c = 189.1 \text{ mm}$$

$$\epsilon_s' = 0.003 \times \left( \frac{d-d'}{c} \right) = 0.0019 < \epsilon_y \quad \text{not o.k.}$$

$$A_s f_y = 0.85 f'_c \times a \times b + A_s' \times E \times \epsilon_s'$$

$$c = 192 \text{ mm}$$

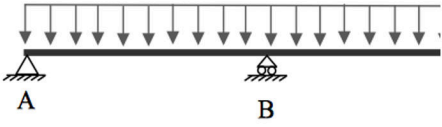
$$a = 163.22 \text{ mm}$$

$$\epsilon_s' = 0.003 \times \left( \frac{c-d'}{c} \right) = 0.0019 < \epsilon_y \quad \underline{\underline{\text{o.k.}}}$$

$$\epsilon_s = 0.003 \times \left( \frac{d-c}{c} \right) = 0.00497 \epsilon_y \quad \underline{\underline{\text{o.k.}}}$$

أفكار أسئلة الفصل الماضي :

السؤال الأول كان معطيني continuous beam بهذا الشكل



وطلب هل السوبورت b بتحمل اللود

لازم تطلع  $\phi Mn$  بالطريقة العادية لكن لكن العبرة من السؤال تعرف وين مكان حديد التسليح لأنه كان قال إنه T beam خوذ سكشن وشوف اتجاه المومنت أو ارسم شير مومنت دايقرام عالسريرع أو بالنظر لأن الجزء B ولليمن عبارة عن كانتلفر فالحديد علوي .

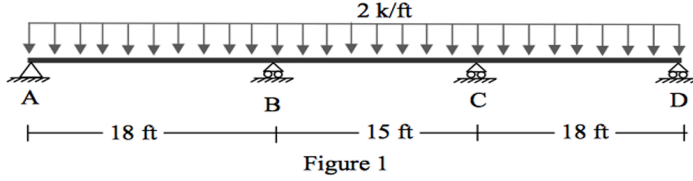
هنا تنتهي مادة الفيرست مع بضع سنوات ... للتقوية والمزيد من الأسئلة حل أسئلة الطالب أنس دواس ...

بالتوفيق للـ 30/30

## Second (The Design )

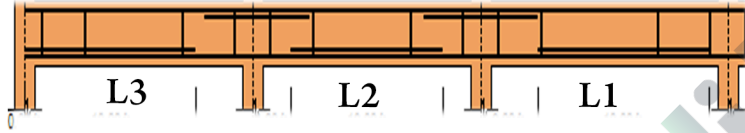
Design of rectangular beam : (the relationship between beam depth and deflection )  
( موجود آخر الدوسية ) Use Table 9.5  $h_{min}$  to avoid deflection

ملاحظة : ازدياد  $h$  يعني زيادة قيمة  $I$  (second moment of inertia) وبالتالي زيادة مقاومة  
البيم للانحناء أي بيم سيحتوي على انحناء ولكنه يجب أن يكون ضمن الـ ACL



مثال هذا continouse beam

هذا البيم الـ  $h_{min}$  3 بين كل عمود  
بنروح الجدول عند (beames or  
(ribbed on way slab

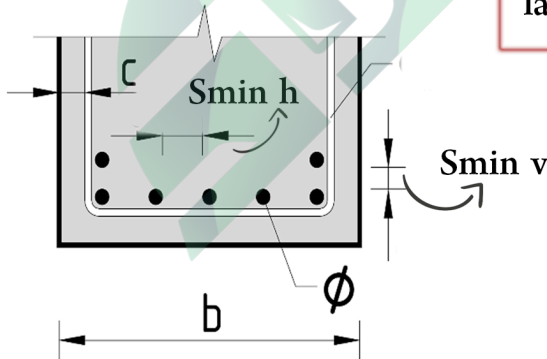


بالنسبة للجزء رقم 1 بما أنه مش متصل بشي من اليمين ومتصل من الشمال فقط فهو One end  
continuous لذلك  $h_{min} = L1/18.5$  (L from center to center)

بالنسبة للجزء 2 فهو متصل من اليمين واليسار لذلك هو both end continuous بالتالي  
 $h_{min} = L/21$ , والجزء 3 نفس الجزء 1 ... هيك بصير عندك ثلاث قيم للـ  $h_{min}$  نختار أكبر وحدة فيهم  
لو ما فهمت بشكل كامل مش مشكلة للأمام رح تفهم بمثال

## Concrete Cover and Bar Spacing

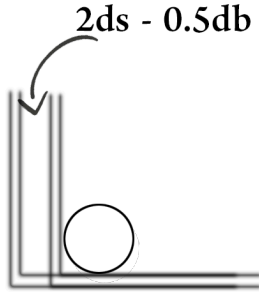
cover for beams is = 40 mm



$S_{min v} \longrightarrow 25mm$   
larger of  $\longrightarrow 1.33$  max coarse aggregate size

$S_{min H} \longrightarrow$  Bar diameter  
 $\longrightarrow 25mm$   
 $\longrightarrow$  diameter of vibrator  
 $\longrightarrow 1.33$  max c.a size

- Resons of cover :
- 1-Protect steel from fire
  - 2-Protect steel from abrasion
  - 3-to bond concrete and steel so both act together



حديد التسليح المفروض يبي على الزاوية القائمة لكن أحياناً ما يبي  
لذلك اعتبرنا مسافة (2ds-0.5db) ضمن حساب bar spacing

حساب الـ b min

bmin : the minimum width of the beam to put the bars in one layer

$$b \text{ min} = 2 * \text{cover} + 2 * \text{sirrups diameter} + n (\text{No. of bars}) * \text{diameter of bar} + (n-1) * S_{\text{min}} + 2(2ds-0.5db)$$

$$b_{\text{min}} = 2 * 40 + 2 * 10 + n * db + (n-1) * S_{\text{min}} + 2(2ds-0.5db)$$

if  $b > b_{\text{min}}$  bars in (one layer) ✓

if  $b < b_{\text{min}}$  bars in (two layers) ✓

Estimating the effective depth of the beam (d)

$$d = h - 65 \text{mm} \quad \text{if one layer}$$

$$d = h - 90 \text{mm} \quad \text{if two layer}$$

bmin should not be less than : preferably (300mm)  
absolutly (250mm)

Mu اضربها بـ 10<sup>6</sup>  
وعوض الباقي بـ mm والـ Mpa

العبرة من عملية تصميم البيم إني أجد كمية الحديد As و أبعاد البيم

معلومات وقوانين لازم تعرفها قبل ما ندخل التصميم

$$A_s = \frac{M_u}{\phi f_y (jd)}$$

Ultimate load or U or W الأكبر

$$U = 1.2DL + 1.6 LL \quad \text{or} \quad U = 1.4DL$$

نعتبر  $\Phi$  هنا = 0.9 دائماً

قيمة j :

j=0.9 for narrow comp area (الليم المستطيل أو T بيم والكومبرشن عدلـ web)

j=0.95 for wide comp area (T بيم كومبرشن ع الفلانج)

$$a = \frac{A_s f_y}{0.85 f'_c b}$$

سؤال التصميم يكون على شكلين

الأول أبعاد البيم معطاه

الثاني أبعاد البيم غير معطاه أو أحدهم معطاه

طريقة حل النوع أول (أبعاد البيم معطاه)

(1) إيجاد ال Mu وذلك عن طريقة ← إيجاد U من  $U=1.2DL+1.6LL$  في حال قلي DL(including Self weight) عوض مباشرة  
 أما DL(excluding self weight) بدك تحسب self weight ثم تصيفه لل  
 DL ثم تعوض بـ U  
 $Self\ weight = b * h * \gamma$   
 $Mu = WL^2/2$  for cantiliever  $Mu = WL^2/8$  for simply supp ←

(2) نفرض One layer or two layer ثم نجد d

(3) نجد  $As = Mu / \Phi fyjd$  ثم بنسوي iteration هكذا

$$As = Mu / \Phi fyjd \quad As = Mu / \Phi fy(d-0.5a) \quad As = Mu / \Phi fy(d-0.5a)$$

$$a = Asfy / f'c \cdot 0.85 b \quad a = Asfy / f'c \cdot 0.85 b \quad a = As = required$$

(4) نجد  $As$  provided من الجدول بتشوف قيمة ال required الي طلعت واختار أكبر منها بشوي أو حسب تقديرك المهم أكبر بالامتحان بقيدك بديامتر معين ...

(5) check one layer or two layer لل one layer ( $b > b_{min}$ ) ولل two layer ( $b < b_{min}$ ) إذا ماكانو ok ارجع للخطوة 2 واحسب d جديدة وارجع عيد (لا تقلق ما رح يوخذ وقت اذا مارس)

(6) check  $As_{min}$  (حالياً) و  $As_{max}$  (لاحقاً بس توخذه) إذا طلع أقل من ال mim استخدم ال Min  
 (7) الان نرجع لل analysis مثل الفيرست ولازم يطلع  $\Phi Mn \geq Mu$

### Example

$$f'c = 20 \text{ Mpa}$$

$$fy = 420 \text{ Mpa}$$

$$LL = 35 \text{ Kn/m} \quad DL = 14 \text{ Kn/m} \quad (\text{excluding self wt}) \quad \gamma = 24 \text{ Kn/m}$$

$$\text{sol} ::: \text{ self wt} = \gamma b h = 24 * 600 * 600 * 10^{-6} = 8.64 \text{ Kn/m}$$

$$DL = 8.64 + 14 = 22.64 \text{ kn/m} \quad U = 1.2DL + 1.6LL = 83.2 \text{ Kn/m}$$

$$\text{Assume One layer} \quad d = h - 65 = 535 \text{ mm}$$

$$As_{required} = My / \Phi fy jd = 3657 \text{ mm}^2 \quad \text{now iterations}$$

$$a = Asfy / f'c \cdot 0.85 b = 150.6 \text{ mm} \quad As = Mu / \Phi fy (d - 0.5 * a) = 3830.4 \text{ mm}^2$$

$$a = 157.7 \text{ mm} \quad As = 3860.2 \text{ mm}^2 \quad a = 159 \text{ mm} \quad As = 3865.6 \text{ mm}^2 \text{ that is } As \text{ required}$$



As provided from table =4080mm<sup>2</sup> 8No25M

بدور على ديامتر وعدد بارز تحقق الrequired أو أكثر

لو قيدني بديامتر معين وبدي أعرف كم سيخ بروح للجدول عند الديامتر الي اعطاني ياه  
بجيب المساحة ل bar عندئذ

العشري يقرب للأكبر عدد الاسياخ = As req / As of one bar

check one layer b<sub>min</sub>=40\*2+2\*10+8\*25+7\*25+2(2\*10-0.5\*25)=490mm <600 ok

لو طلع b أقل من ال b min ارجع افرض two layers وعيد حساب d ثم As لا تقلق الشغلة مش  
صعبة مثل ما تتوقع أو يمكن تكبير الديامتر لكن إن ما فرض عليك ارجع عيد الحسابات أفضلك  
check As min = 854mm<sup>2</sup> or 1070 mm<sup>2</sup> larger is 1070mm<sup>2</sup> and it is ok

الان نرجع للanalysis للتأكد من الtension controlled

As f<sub>y</sub> = 0.85 f'<sub>c</sub> ab a=168mm c =197.6mm ε<sub>s</sub>=0.0051 then it is tension con-  
trolled Mn=772.8Kn.m Phi Mn=695.9Kn.m PhiMn>Mu then ok

الطريقة الثانية : b and h and As are Unknowns شوية قوانين مش حفظ

$$\rho = \frac{A_s}{bd}$$

steel ratio  
reinforcement ratio  
percentage of reinforcement

$$a = \rho \frac{f_y}{f'_c} \times \frac{d}{0.85}$$

$$\omega = \rho \frac{f_y}{f'_c}$$

Mechanical steel ratio

$$a = \frac{\omega d}{0.85}$$

$$Kn \text{ or } R = \omega f'_c (1 - 0.59\omega)$$

flexural resistance factor

$$Mu = \Phi Mn = \Phi (bd^2 \omega f'_c (1 - 0.59\omega))$$

$$bd^2 = \frac{Mu}{\phi Kn}$$

طريقة حل هذا النوع (ملاحظة الكلام كله هذا شارحه الدكتور ضمن مثال رح تشوفه للأمام انا حبيت أبين الاسلوب قبل ما تدخل المثال)

1-estimation of self weight : the weight of rectangular beam will be roughly (10%-15%) of the unfactored loads it must carry

1-self weight = (10%-15%)\*(DL+LL)

2- h=(1/18 to 1/12 ) of L

L : span length in mm

then b=0.5 h then self wt = gamma\*hb

قيم b و h هذي بس عشان فرض self wt لا تيجي وتقلي b و h معلومات

2- : قيمة ρ

ρ for economic considerations= 0.01 (أو إذا ما حتى كم قيمتها اعتبرها هيك)

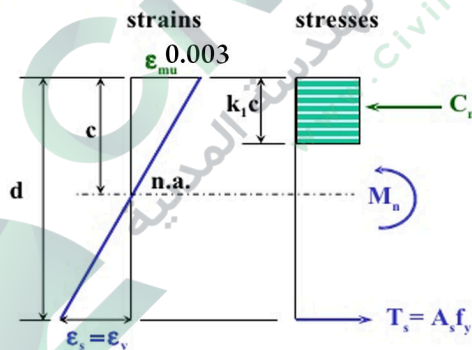
ρ Ductility considerations= (0.35-0.4) ρ<sub>b</sub> ρ<sub>b</sub>=balanced steel ratio

$$\rho_b = \frac{A_{sb}}{bd}$$

balanced condition ε<sub>s</sub>=ε<sub>y</sub> كمية الحديد في حالة ال

by placing considerations it may be hard to place the reinforcement ما لازم تتعداه ρ max = 0.015 that means ρ exceeds =0.015

strain compactability



من تشابه المثلثات

strain compactability

$$\frac{0.003}{c} = \frac{0.003 + \epsilon_y}{d}$$

$$c = \frac{0.003}{0.003 + \epsilon_y} d \dots 1$$

$$a = \frac{A_{sb} f_y}{0.85 f'_c b} = \frac{\rho b d f_y}{0.85 f'_c b}$$

$$c = \frac{\rho b d f_y}{0.85 f'_c \beta}$$

from 1 and 2 
$$\rho_b = \frac{0.85 \beta_1 f'_c \left( \frac{0.003}{0.003 + \epsilon_y} \right) \times \frac{E}{E}}{f_y} = \frac{0.85 \beta_1 f'_c \left( \frac{600}{600 + \epsilon_y} \right)}{f_y}$$

مش حفظ لكن افهم فهم لأنه ممكن يقلك بدى عن سترين معين مش ε<sub>y</sub> نفس الخطوات بس بتغير بدل ε<sub>y</sub> حط القيمة

3- نجد Mu و Kn (حسب قوانينهم سابقا)

$$4- bd^2 = \frac{M_u}{\phi Kn}$$

هون بدنا نفرض 3 قيم تقريباً ل b و بنوجد 3 قيم ل d

نختار القيم الي فيها تقريباً 0.5b=d لكن غالباً بالامتحان بجددلك قيمة b وإذا

بدك تقرب قيمة d قربها لأكبر ثم نجد h حسب فرض ال layers

one leayer h=d+65

two layers h=d+90

5-check h min hmin الى طلعتها لازم تكون أكبر من  
إذا ما كانت خوذ الhmin وارجع احسب الd

6-check self wt and recvise Mu

Self weight القيمة الفعلية لـ self wt

لا تنسى تضيف ال self wt لل DL  $w_{new} = 1.2 DL + 1.6 LL$

$Mu_{new} = WL^2/8$  if simply supp or  $WL^2/2$  if cantilever

$$\frac{M_{u \text{ جديد}} - M_{u \text{ قديم}}}{M_{u \text{ قديم}}} \times 100\% \quad \text{ثم حساب النسبة}$$

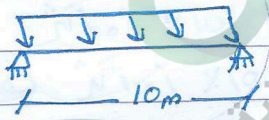
يجب أن لا تكون الزيادة 10% أو أكثر  
إذا كانت الزيادة في 10% أو أكثر نعيد ال design عندئذ بنحط

$$bd = \frac{Mu_{new}}{\Phi kn}$$

7-find As and do the iterations then As provided then check Asmin and max

8-check b min 9-analysis

Example 8



$L_h = 25.5 \text{ k/m}$        $DL = 14.5 \text{ k/m}$  (excluding self wt)  
 $f'_c = 25 \text{ MPa}$        $f_y = 420 \text{ MPa}$

1 Estimate Self wt

$$h = \left(\frac{1}{18} - \frac{1}{12}\right) * 10,000 = (555 - 833)$$

$$b \approx 0.5h = (277 - 416)$$

$$\text{Self wt} = \gamma bh = (3.68 - 8.3) = 8 \text{ k/m}$$

2 نجد b و d

$$bd^2 = \frac{Mu}{\Phi kn} \rightarrow Mu = \frac{wL^2}{8} \quad w = 1.2(14.5 + 8) + 1.6(25)$$

$$Mu = 848 \text{ kNm}$$

$$\omega = \frac{0.01 * 420}{25} = 0.168$$

$$\phi kn = 0.9 [25(0.168)(1 - 0.168)] = 3.41$$

$$bd^2 = \frac{848}{3.41} = 248.7 * 10^6 \text{ mm}^3$$

نقرب قيمة لـ b

باعتبار هذه القيمة تقريباً  $b = 400 \text{ mm}$        $d = 788 \text{ mm}$

$$h = d + 90 = 878 \text{ mm} \quad (\text{assume 2-layers})$$

زيتيلا 900 mm للتسديد

$$d = 900 - 90 = 810 \text{ mm}$$

- check h<sub>min</sub>

$$h_{min} = \frac{L}{16} = \frac{10,000}{16} = 625 \text{ mm} < 900 \therefore \text{O.K.}$$

- check self wt and revise M<sub>u</sub>

$$\text{self wt}_{new} = 24 \times 0.9 \times 0.4 = 8.64$$

$$W_{new} = (8.64 + 14.5) \times 1.2 + 1.6 (28.5) = 68.57 \text{ kN}$$

$$M_u = \frac{68.57 (10)^2}{12} = 857 \text{ kN.m}$$

\* يجب ان لا تكون الزيادة 10% او اكثر

\* اذا كانت الزيادة في M<sub>u</sub> 10% او اكثر فعيد ال Design

\* عندئذ ستتم اعادة الحساب ~~بجدول~~ بجدول آخر الا بعد

لانه اعيد بحسابي .  $bd^2 = \frac{M_u}{\phi k}$  او  $AS$

$$\frac{Mu_{old} - Mu_{new}}{Mu_{new}} \times 100\%$$

\* صان نسبة

$$= 1.1\% < 10\% \text{ O.K.} \checkmark$$

$$AS = \frac{Mu}{\phi f_y j d} = \frac{857 \times 10^6}{0.9 (420) 0.9 (810)} = 3110 \text{ mm}^2$$

iterations

①  $AS = 3110 \text{ mm}^2$

$a = 153.7 \text{ mm}$

②  $AS = 3092 \text{ mm}^2$

$a = 152.8 \text{ mm}$

$AS = 3090.5 \text{ mm}^2$

(required)

نيلج للجدول use 7 N025 M ;  $AS = 3570 \text{ mm}^2$

- check AS<sub>min</sub>

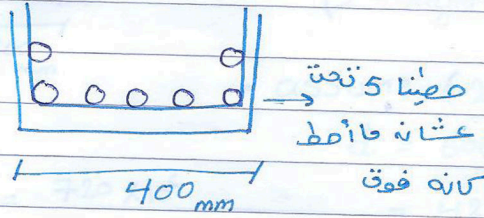
964 mm<sup>2</sup>

1080 mm<sup>2</sup> <  $AS = 3570 \text{ mm}^2$  O.K. ✓

$$\text{check } b_{min} = 2 \times 40 + 2 \times 10 + 7 \times 25 + 6 \times 25 + 2(20 - 0.5 \times 25) = 440 \text{ mm}^2$$

$$440 \text{ mm} > 400 \text{ mm} \quad \checkmark \quad \text{o.k.}$$

Two layers



$$b_{min} (5 \text{ No } 25 \text{ M}) \quad \text{o.k.}$$

- Analysis

$$a = \frac{357.5 \times 420}{0.85 \times \dots} = 176.4 \text{ mm}$$

$$c = 267.5 \text{ mm}$$

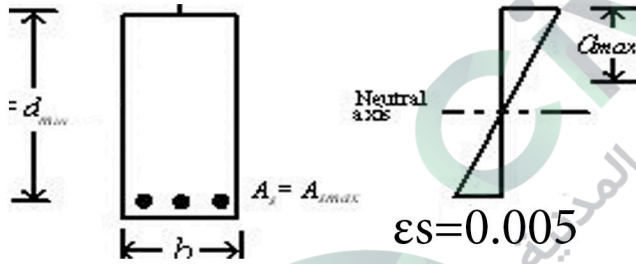
$$\epsilon_s = 0.003 \left( \dots \right) = 0.0087 \quad \text{tension controlled}$$

$$\phi = 0.9$$

$$\phi M_n = 974 \text{ kN.m} \quad \gamma M_u = 857 \text{ kN.m}$$

o.k.

## Maximum Area of tension reinforcement

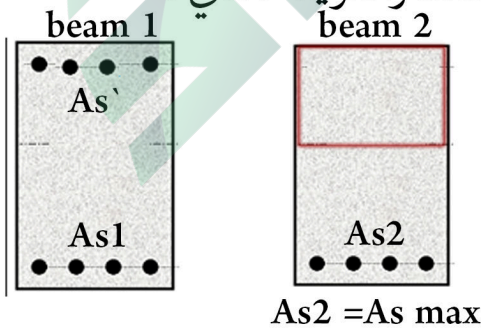


$$A_s \text{ max} = 0.319 \theta \frac{f'_c}{f_y} bd$$

بالامتحان يجيب  $\rho \text{ max}$  أو  $A_s \text{ max}$  لذلك اعرف إنه

$$A_s \text{ max} = \rho \text{ max } bd$$

في حال  $A_s > A_s \text{ max}$  بصير السؤال doubly reinforcement والطريقة كالتالي :



(1) نقسم البيم لقسمين

(2) بيم 2 already yielded بالتالي  $\epsilon_s = 0.005$

بيم 2 (T=Cc) وجيب a و c (قيم c لكل البيم)

(3) احسب  $\Phi M_{n2} = \Phi A_s2 f_y (d - 0.5^*)$

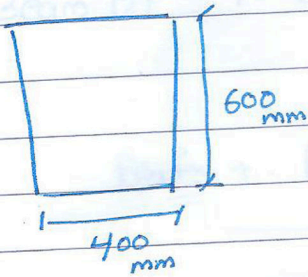
(4) نحسب  $\Phi M_{n1}$  من  $\Phi M_{n1} = M_u - \Phi M_{n2}$  ثم من  $\Phi M_{n1}$  بنحسب  $A_s1$  ثم مجموعهم

بعطيني  $A_s$  ثم جيب ال provided بعد ما جبت provided احسب قيمة  $A_s1$  الجديدة حيث

$A_s2$  ثابتة وهي  $A_s \text{ max}$  بعدها من بيم 1 حتى نعرف  $T = C_s (A_s1 f_y = A_s' f_y \text{ or } f_s)$

(5) analysis شريك على  $\epsilon_s$  ثم  $A_s' \text{ provided}$  (زيادة  $A_s'$  تزيد  $\epsilon_s$ )

Example  $f'_c = 28 \text{ MPa}$   $F_y = 414 \text{ MPa}$   $M_u = 720 \text{ kNm}$



$A_s = 149$

بما أنه لوفتة عاى 2 لى مبرنى حديد كثر  
لذلك لى لى علب هيجون (2-layers)

• assume (2-layers)

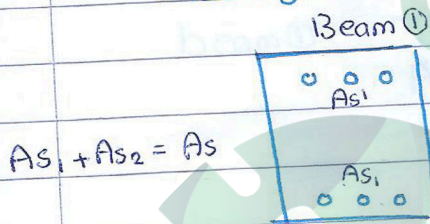
$d = 600 - 90 = 510 \text{ mm}$

$A_s = \frac{720 \times 10^6}{0.9 \times 414 \times 0.9 \times 510} = 4210 \text{ mm}^2$

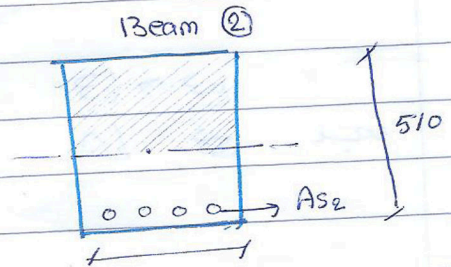
$A_{s \max} = 0.319 (0.85) \frac{28}{414} \times 400 \times 510 = 3741 \text{ mm}^2$

$A_s > A_{s \max} \rightarrow$  (Not tension controlled)

• Doubly reinforced beam:



$A_{s1} + A_{s2} = A_s$



$A_{s2} = A_{s \max} = 3741 \text{ mm}^2$

$\epsilon_s = 0.005$  لى already yielded

Beam 2  $T = C_c$   $3741 \times 414 = 0.85 \times 28 \times 9 \times 400$   
 $a = 162.7 \text{ mm}$   $c = 191.4 \text{ mm}$

Check  $\epsilon_s$  لى شان تىقنه انه مزبوطان

$\epsilon_s = 0.005$  لازم

$\epsilon_s = 0.003 \left( \frac{510 - 191.4}{191.4} \right) = 0.005 \checkmark$

$\phi M_{n2} = \phi A_{s2} F_y (d - 912) = 597.5 \text{ kNm}$

لانى بكم بيم لى لىقده لى  $M_u$

$\phi M_{n1} = 720 - 597.5 = 122.5 \text{ kNm}$

طابىر تستقم (  $A_s = A_{s1} + A_{s2}$  ) لى لى لىقده لى تension controlled

Beam ②  $T = C$   $A_{s2} F_y = 0.85 f'_c ab$   
 $L_c$   $a = \dots$   $C = 191.4 \text{ (mm)}$   
 $\epsilon_s = 0.005$

$$\underline{A_{s1} F_y} + A_{s2} F_y = 0.85 f'_c ab + \underline{C_s}$$

← نفسنا القوة →

لذلك ما إننا نساوي المعادلتين

$$T_1 = C_s = A = A_{s1} F_y$$

يعني

$$\phi M_n = \phi (A_{s1} F_y) (d - d')$$

100      0.9

$$A_{s1} = 728 \text{ mm}^2$$

لوبيك تستخدم  $A_{s1} \times F$

لولا تشييد  $\epsilon_s$

بالإضافة على  $\epsilon_s$  تكون  $F_s$  أنف نستخرج  $F_y$  إذا  $F_s$

$$A_s = A_{s1} + A_{s2} = 728 + 3741 = 4469 \text{ mm}^2$$

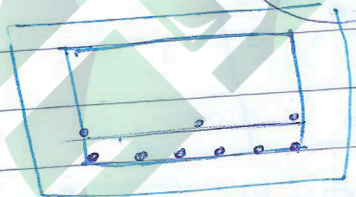
(required) ←

beam ①  $T = C_s$   
 $A_{s1} F_y = A_{s'} F_y$   $\epsilon_s' < \epsilon_y$   
 $A_{s'} = \dots$  نجد

• Selection of  $A_s$

$A_s$  provided 9 No 25 M ;  $A_s = 4590 \text{ mm}^2$

$b_{min} = \dots > 400 \therefore$  two layers ok



beam ①  $A_{s1}$  تجرنا  
 لما اخترنا Provided

$$A_{s1} + A_{s2} = 728 + 3741$$

$$A_{s1} = 4590 - 3741 = 849 \text{ mm}^2$$

لوبيك أعجب  $A_{s'}$  لوبيك  $\epsilon_s$  check

$$F_s = F_{s'} = 396 \text{ MPa}$$

$$\epsilon_s' = 0.00198 \text{ not yielded}$$

$$A_{s1} F_y = A_{s'} F_{s'} \quad 849 \times 4140 = A_{s'} \times 396 \quad A_{s'} = 900 \text{ mm}^2$$

$$A_{s'} \text{ provided} = 995 \text{ mm}^2$$

طابقنا ما ارجعنا اب  $A_{s1}$

لوبيك  $\epsilon_s$  و  $\epsilon_s'$  تجرنا لوبيك

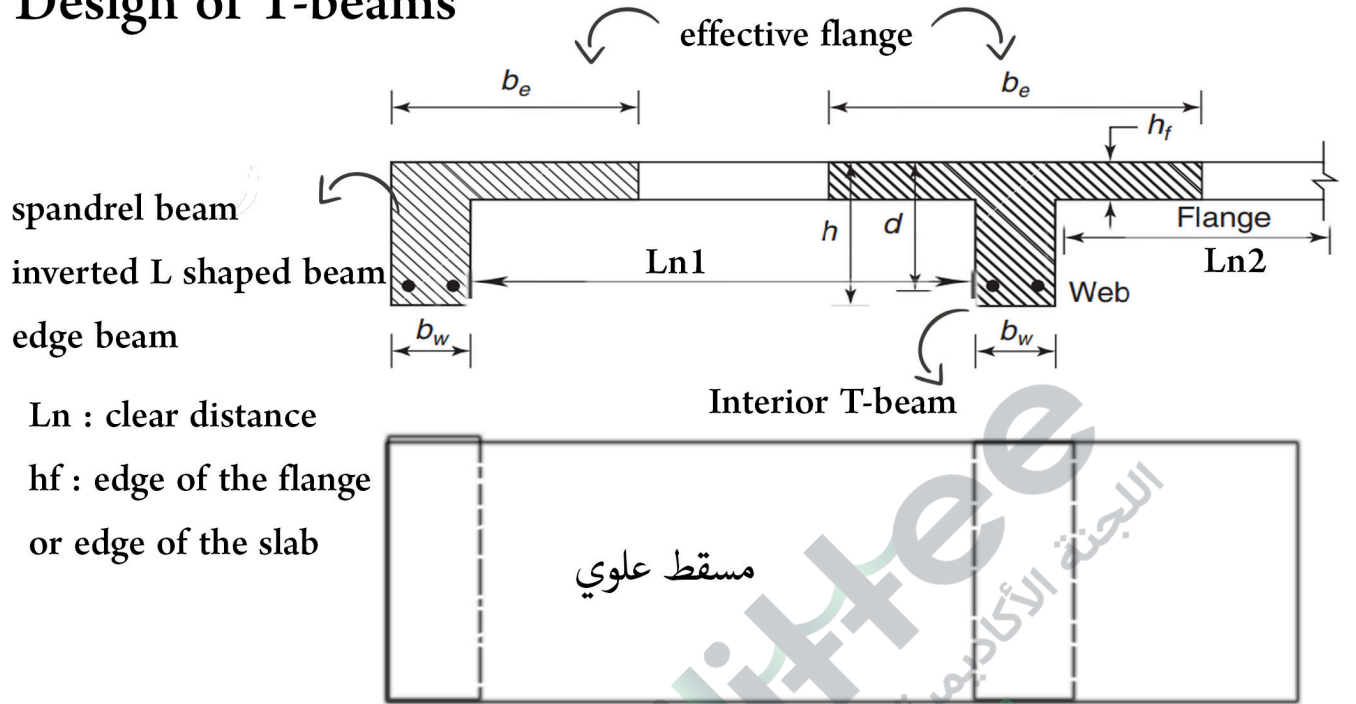
→ Analysis

$\epsilon_s$  yield

$\epsilon_s$  not yield

$$F_s = F_{s'} = 396 \text{ MPa}$$

# Design of T-beams



$Ln$  : clear distance

$h_f$  : edge of the flange  
or edge of the slab

يتشكل الT-بيم لأن الصبة للبيم والاسلاب مع بعض

for spandrel beam

حفظ

for T Beam Interior

حفظ

$$b_e = \begin{cases} b_w + Ln/2 \\ b_w + 6h_f \\ \text{smaller of } b_w + \ell/12 \end{cases} \quad b_e = \begin{cases} b_w + Ln1/2 + Ln2/2 \\ b_w + 2(8h_f) \\ \text{smaller of } \ell/4 \end{cases}$$

مهم جداً

$Ln$  المسافة بين بيمين Face to face

center to center بتكون على نفس البيم من العمود الأول للعمود الثاني  $L$

هالكلام مهم لسؤال الاسلاب لقدام ولو ما فهمت احفظهم هيكل رح تفهم بعدين

أسلوب حل الT beam .. (أسهل سؤال)

(1) بعطيني المومنت أو بعطيك  $W$  غالباً .. المهم بس يكون عندك المومنت أول شي بتجيبه  $As = Mu / \Phi f_y j d$

(2) في تصميم الT beam ما بسوي iterations

ما بشيرك على ال  $As_{max}$  لما يكون flange in Comp

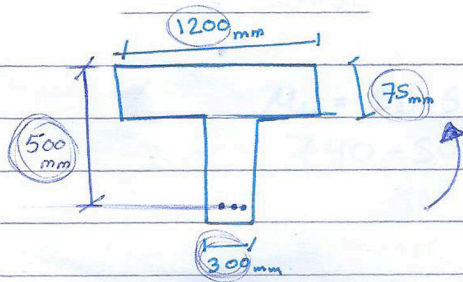
ما بحسب  $b_{min}$

الان بنجيب  $As_{provided}$  ونشيك  $As_{min}$

analysis (3)

(4) Check  $As_{required}$  based on computed  $a$  (ويجب أن يكون  $Provided > Req$ )

رح تفهم كل شي بالمثال الان



$$f'_c = 21 \text{ MPa}$$

$$f_y = 420 \text{ MPa}$$

$$M_u (+ve) = 740 \text{ kN.m}$$

$$A_s = \frac{M_u}{\phi f_y j d} = \frac{740 \times 10^6}{0.9 \times 420 \times 0.95 \times 500} = 4121.41 \text{ mm}^2 \quad \text{Required}$$

Flange  $\leq$   $\frac{1}{4}$   $\leq$   $A_s$  max  $\leq$   $\frac{1}{4}$   $\leq$   $\frac{b_f}{b_w}$  \*  
in Comp

$\frac{d}{h} \leq (d - a)$   $\Rightarrow$  Flange in Comp  $\leq$   $\frac{1}{4}$   $\leq$   $\frac{b_f}{b_w}$   $\leq$   $\frac{1}{4}$   $\leq$   $\frac{b_f}{b_w}$  \*  
in Tension

$$A_s \text{ min} = \left\{ \begin{array}{l} \frac{500 \text{ mm}^2}{400 \text{ mm}^2} \quad \text{O.K.} \\ A_s \text{ provided} = 4590 \text{ mm}^2 \\ 9 \text{ NO28M} \end{array} \right.$$

- analysis

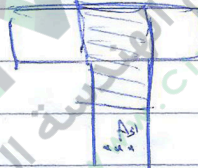
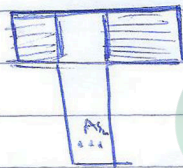
$$a \leq h_f$$

$$T = C$$

$$a = 90 \text{ mm} > 75 \text{ mm} \quad \text{not O.K.}$$

① beam (P)

② beam (W)



$$A_{sw} = 4590 - 2868 = 1721 \text{ mm}^2$$

$$T = C \quad a = 134.98 \text{ mm}$$

$$C = 158.8 \text{ mm}$$

$$A_s 420 = 0.85 \times f'_c \times 75 \times (900)$$

$$A_s = 2868 \text{ mm}^2$$

$$\epsilon_s = 0.006 \quad \text{Yielded}$$

Provided  $\phi M_w = 281.3 \text{ kN.m}$

$$\phi M_{nF} = 501.5 \text{ kN.m}$$

$$\phi M_n = 783 \text{ kN.m} > M_u = 740 \text{ O.K.}$$

• Check  $A_s$  required based on Computed  $a$ .

$$A_{sw} = \frac{M_u}{\phi f_y (d - a/2)}$$

$$\frac{M_u}{\phi} =$$

$$\phi M_n = \phi M_w + \phi M_{nF}$$

$$M_u = 501.6 + M_w$$

$$740 - 501.6 = M_w = 238.4 \text{ kN.m}$$

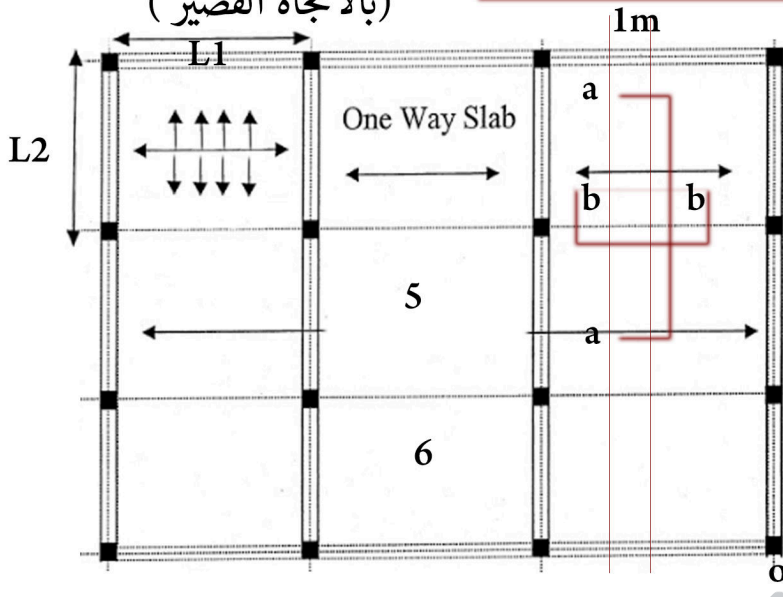
req  $\leftarrow$

$$A_{sw \text{ req}} = \frac{238.4 \times 10^6}{0.9 \times 420 \left(500 - \frac{135}{2}\right)} = 1460 < 1721 \quad \text{O.K.}$$

req  $\leftarrow$  Provided  $\leftarrow$

طريقة انتقال اللود  
من منتصف السلاب  
(بالاتجاه القصير)

## One way Solid Slab



لماذا ينتقل اللود بالاتجاه القصير؟  
لأن  $stiffness (K=4EI/L)$   
علاقة عكسية مع الطول

$$\frac{\text{Larger dimension}}{\text{shorter dimension}} = L1/L2$$

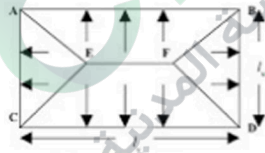
$\geq 2$

one way solid slab

$< 2$

two way slab

تصميم السلاب يكون للمتر المربع لذلك  $w$  بتكون  $Kn/m^2$   
مهم جداً حتى تعرف إنه both end ولا one end دائماً اطلع بالاتجاه القصير  
يعني لو اعتبرنا بالرسمه فوق  $L2$  هو الاتجاه القصير فإن سلاب both end 5 و سلاب one end 6



توزيع اللود بالtwo way solid بهذا الشكل

Section a-a



section bb



slab thickness حساب ال  $h_{min}$

تذكر دائماً ال  $L$  المستخدمة بالاتجاه القصير  
لازم تحدد بالأول one end او two end ثم روح للجدول

دائماً ال width بالسلاب = 1000mm

cover of slab = 20mm

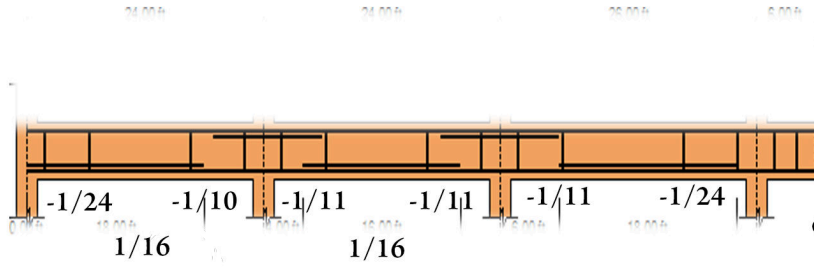
$$A_s = \frac{M_u}{\Phi f_y j d}$$

$j=0.95$  in one way solid slab

ACI code moment and shear coefficient for analysis  
and design of non-prestressed one way slabs and  
continous beams

$$M_u = C_m (W_u L_n^2)$$

$$V_u = C_v (W_u L_n / 2)$$



تصميم السلاب يكون تصميم على مومنتين موجب وسالب .. الارقام بالرسمه هي cofficicnets ولما نصمم بستخدم أكبر مومنت

$$A_s \min = 0.0018 bh \text{ for G60 steel}$$

$$A_s \min = 0.002 bh \text{ for G40,50 steel ماينستخدمه}$$

خطوات تصميم السلاب :

(0) تشييك على one way or to two way slab أكيد لازم يطلع معك الطول كبير تقسيم الطول القصير أكبر من 2 estimate h min(1) بتك تحدد both end or one end وتستخدم الجدول وتجد hmin والقيمة الي بتطلع معك زيدها 10 أو 20mm أو ستخدمها نفسها

(2) Compute factoral load ( self wt = gamma \* h ) بطلع معي بوحده kn/m2 زيدها للDL واحسب U

(3) التصميم للمومنت السالب بتوجد أكبر مومنت سالب بعدها نحسب d حيث  $d = h - \text{cover} (20\text{mm}) - (db/2)$  db بجدده بالامتحان

نجد  $A_s = M_u / \Phi f_y j d$  رح يطلع معك كمية الحديد للمتر الواحد بس

- شيبك  $A_s \min$  ثم إذا طلع أقل من  $A_s \min$  استخدم  $A_s \min$  إذا طلع أكبر سوي itreations وبتطلع معك req - لاتييب الprovided بدل ذلك نحسب spacing

$$\text{spacing} = \frac{1000 A_b}{A_s \text{ req}}$$

$A_b$ : area of one bar

بعد ما جبت spacing بتك تشييك عال  $S \max$

$S_{\max}(\text{smaller of}) = 3h \text{ or } 450 \text{ mm}$  لو طلع أكبر من  $S_{\max}$  بستخدم  $S_{\max}$

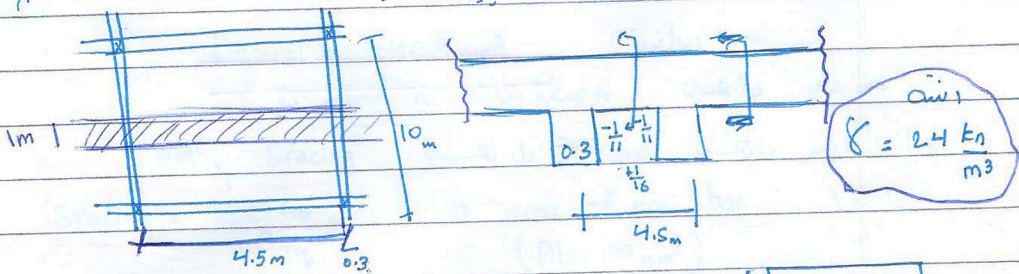
(4) تصميم المومنت الموجب نفس اسلوب خطوة 3 لكن للمومنت الموجب

Per ACI code : shrinkage and temp reinfocment is required perpeneicular to spans of the slabs للصميم من أجل shrinkage والtemp هون بستخدم  $A_s \min$  ثم بتيب spacing

وبشييك على  $S_{\max}$  هذي :  $S_{\max} (\text{Smaller of}) = 5h \text{ or } 450 \text{ mm}$

• Design Example :  $f'_c = 28 \text{ MPa}$   $f_y = 414 \text{ MPa}$   $w_{DL} = 4 \text{ kN/m}^2$

$U = 1.2D_L + 1.6L_L$  Unfactored load  $w_{TL} = 3 \text{ kN/m}^2$



$L_n = 4.5 - (2)(0.15) = 4.2 \text{ m}$

Sol : ① Check one-way or two-way

$\frac{10,000}{4.5 \times 10^3} = 2.2272 \therefore \text{One way}$

② estimate  $h_{min}$  both end con  $h_{min} = \frac{4.5 \times 10^3}{28} = 160 \text{ mm}$

$h_{min} = 180 \text{ mm}$

3- Compute Factoral load

Self wt =  $24 \frac{\text{kN}}{\text{m}^3} \times h = 24 \times 0.18 = 4.32 \text{ kN/m}^2$

$U = (4.32 + 3) \times 1.2 + 1.6(4) = 15.18 \text{ kN/m}^2$

\*  $M_u$

$M_u (-ve) = \frac{w_u L_n^2}{11} = \frac{15.18 (4.2)^2}{11} = 24.34 \text{ kNm}$

بعض الترتيبات (للأعلى)

both end con لفردش ننته (لاشيه)

ال (+) الصبوصة

try use No 16

$d = 180 - 20 - \frac{16}{2} = 152 \text{ mm}$

$A_s = \frac{M_u}{\phi F_y d} = \frac{24.34 \times 10^6}{0.9 \times 414 \times 0.95 \times 152} = 452.4 \text{ mm}^2$

$A_{smin} = 324 \text{ mm}^2 < A_s \text{ o.k.}$

iterations  $a = \frac{A_s f_y}{0.85 f'_c \times b} = 7.87 \text{ mm}$

$A_s = 441 \text{ mm}^2 \quad a = 7.67 \text{ mm} \quad A_s = 440.9 \text{ mm}^2$

$A_s (req) = 440.9 \text{ mm}^2$  (المطلوب)

ماضي داي check عس check a عسرة مقارنة ب h عسرة عسرة

width Spacing Provided by  $\phi$

$\text{Spacing} = \frac{1000 A_b}{A_{sreq}}$   $A_b$ , area of one bar (No 16) ( $A_b = 199 \text{ mm}^2$ )

$S = \frac{1000 \times 199}{440.9} = 451 \text{ mm}$  Use 450 mm

Per ACI  $S_{max} = \begin{cases} 3h & 3h = 450 \text{ mm} \\ 450 \text{ mm} \end{cases}$

$S_{max}$  use 450 mm

$$M_u(+ve) = \frac{w_u l_n^2}{16} = 16.74 \text{ kNm}$$

$$A_s = 311 \text{ mm}^2$$

check  $A_{s \min} = 0.0018(1000)(180) = 324 \text{ mm}^2$

$$A_s < A_{s \min}$$

use  $A_{s \min}$

مطابقاً لـ  $A_{s \min}$  لا توي  $A_s$  لا يطغى  $A_s$   $A_s$   $A_{s \min}$   $A_s$

$A_s$   $A_{s \min}$   $A_s$   $A_{s \min}$

$$S = \frac{1000 \times 199}{324} = 614.2 \text{ mm}$$

$$S_{\max} = \begin{cases} 3(180) = 540 \text{ mm} \\ 450 \text{ mm} \end{cases}$$

Use 450 mm

\* Per ACI-code:

• Shrinkage and Temp reinforcement is required Perpendicular to Spans of the Slabs

(longer dimension)  $\rightarrow$   $A_{s \min}$

$$\therefore A_{s \min} = 0.0018 bh = 324 \text{ mm}^2 \text{ per each meter}$$

$$S = \frac{1000 \times 199}{324} = 614.2 \text{ mm}$$

$$S_{\max} \text{ smaller of } = 5h = 900$$

$$450 \text{ mm} \checkmark$$

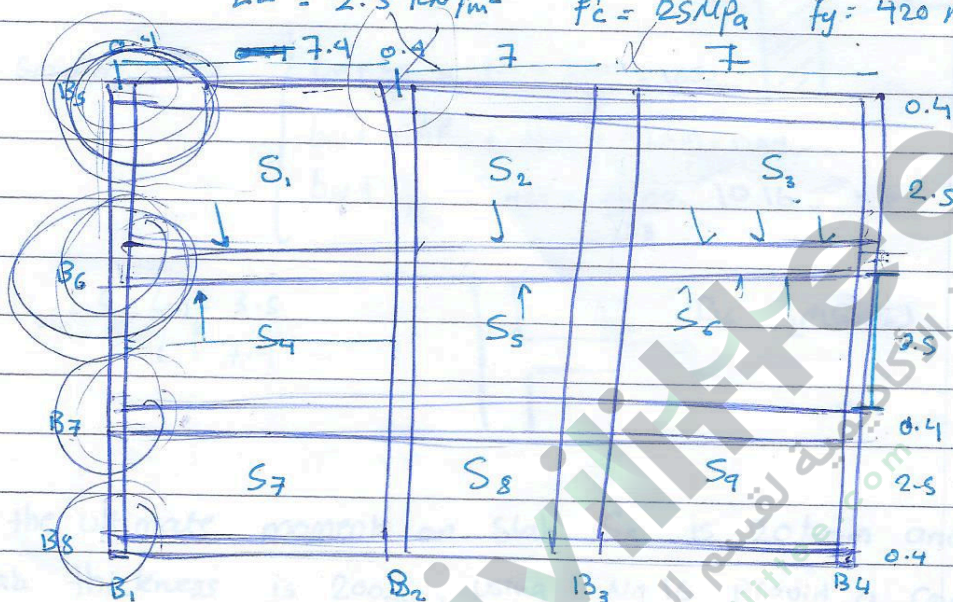
$$\text{Use } S = 450 \text{ mm}$$

You can use another no. of reinforcement for longer dim.

all dimension in m (Face-to-face)

DL (including self wt) =  $3 \text{ kN/m}^2$

LL =  $2.5 \text{ kN/m}^2$   $f_c = 25 \text{ MPa}$   $f_y = 420 \text{ MPa}$



1- the min thickness in mm of S<sub>4</sub> to avoid deflection  
Calculation is most nearly:

two way slab  $h_{min} = \frac{L_n}{28} = \frac{3.5 + 2(0.2)}{28} \times 1000 = 139.28 \text{ mm}$

2- the min thickness in mm of beam B<sub>3</sub> to avoid deflection  
Calculation is

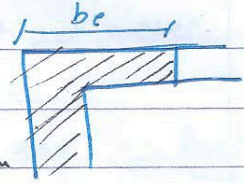
$h_{min} = \frac{L_n}{21} = \frac{18.71}{21} = 89.1$  (قنار الأثر)  
 $h_{min} = \frac{L_n}{18.5} = \frac{156.75}{18.5} = 135.13$

3- the ultimate load in kN transferred from slabs to beam B<sub>6</sub> is most nearly

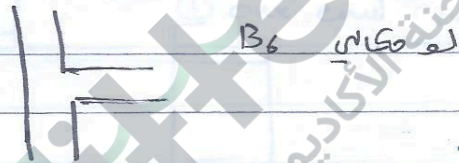
$U = 1.8 \times 3 + 1.8(2.5) = 7.6 \text{ kN/m}^2$  (الضغط النهائي)  
W/Fn B<sub>6</sub> =  $7.6 \times \left(\frac{3.9}{2}\right) + 7.6 \times \left(\frac{2.9}{2}\right) = 25.84 \text{ kN/m}$  (بالنسبة للعرض الواحد)  
من سلاطة، لي تفت من سلاطة الفوف

4. the effective Flange width in mm of beam B5 is most nearly? assume ( $h_f = 200$  mm)

$$b_e \text{ smaller of } \left\{ \begin{array}{l} b_w + \frac{L_n}{2} = 400 + \frac{2500}{2} = 1650 \text{ mm} \\ b_w + 6h_f = 400 + 6(200) = 1204 \text{ mm} \\ b_w + \frac{L}{12} = 400 + \frac{7400}{12} = 1016 \text{ mm} \end{array} \right.$$



$$L_n = 2.5 \quad L_n = 3.5 \\ L = 7.4$$



5) If the ultimate moment on Slab  $S_5$  is  $20 \text{ kN}\cdot\text{m}$  and the slab thickness is  $200 \text{ mm}$ , using No. 16 provide a complete design of the slab (in the short and long dimensions)

$$h = 200 \text{ mm} \quad U = 7.6 \text{ kN/m}^2 \quad M_u = 20 \text{ k}\cdot\text{m}$$

$$d = 200 - 20 - \frac{16}{2} = 172 \text{ mm}$$

$$A_s = \frac{M_u}{\phi F_y j d} = \frac{20 \times 10^6}{0.95 \times 420 \times 0.9 (172)} \approx 323.8 \text{ mm}^2$$

$$A_{s \min} = 0.0018 b h = (0.0018)(1000)(200) = 360 \text{ mm}^2$$

$$A_s < A_{s \min} \text{ we take } A_{s \min} = 360 \text{ mm}^2$$

$$\text{Spacing} = \frac{1000 A_b}{A_s} = 552.77 \text{ mm}$$

$$\text{Spacing max} = \begin{cases} 3(200) \text{ mm} \\ 450 \text{ mm} \end{cases} \quad \text{we use } S = 450 \text{ mm}$$

\* long dimension

$$A_{s \min} = 360 \text{ mm}^2$$

$$S = 552.77 \text{ mm}$$

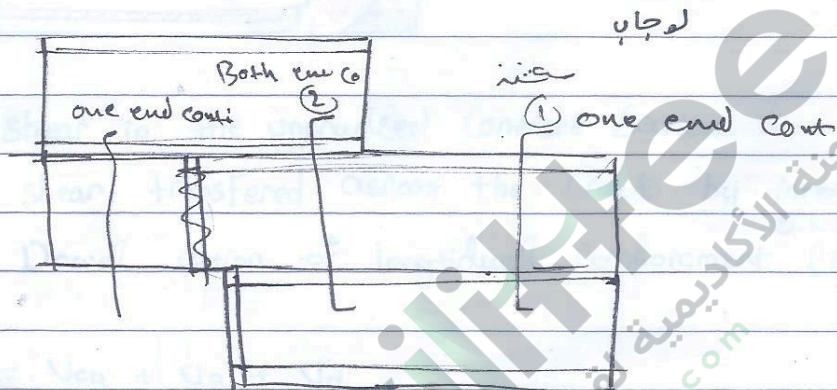
$A_{s \min}$   $\mu$   $\mu$

we use

$$S_{\max} = 450 \text{ mm}$$

⑥ 1 $\phi$  slab (SS) is reinforced with 1N014 spaced at 300 mm the provided area of steel  $A_s$  in  $\text{mm}^2$  per meter width of the slab is most nearly:

$$A_s \text{ Spacing} = \frac{1000 A_b}{A_s} = 300 \quad \underline{\underline{A_s = 513.1 \text{ mm}^2}}$$



هنا تنتهي مادة السكند ...  
سأقوم بإرفاق ملف ملحق بأسئلة السنوات محلولة قبيل الامتحان بإذن الله  
وفي حال لاحظت أي خطأ أو عندك استفسار بالدوسية أو لطلب الملحق  
الالكترونياً  
تواصل معي على الفيس:

<https://www.facebook.com/ezrawille>

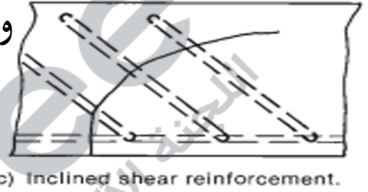
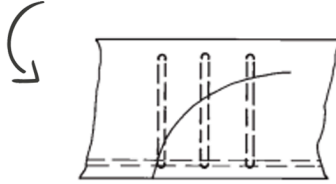
# Final

## shear in beams

Sittups : shear reinfocment      web reinfocment

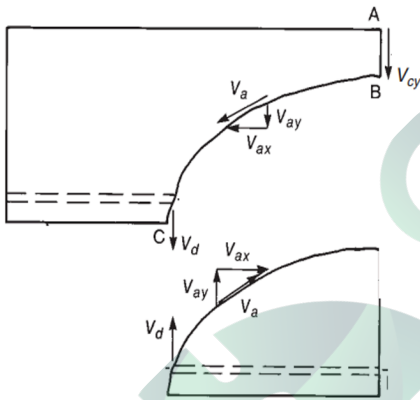
ال Normal stress بعمل crack بزاوية 90 لذلك الحديد يكون عمودي على الكراك  
 ال Shear stress بعمل crack بزاوية 45  
 قلنا أن الحديد يجب أن يكون عمودي على تأثير الشير أو الكراك

ولكن هذا الشيك صعب التطبيق عمليا لذلك نستخدم stirrups



(c) Inclined shear reinforcement.

يكون معظم ال stirrups بالقرب من ال supp حيث ال Shear stress Max



Internal forces in beam without stirrups

$V_{cy}$  : Shear in the uncracked concrete section

$V_a$  : Shear transferd across the crack by interlock

$V_d$  : Dowel action of longitudinal reinfocment

$$V_c = V_{cy} + V_a + V_d$$

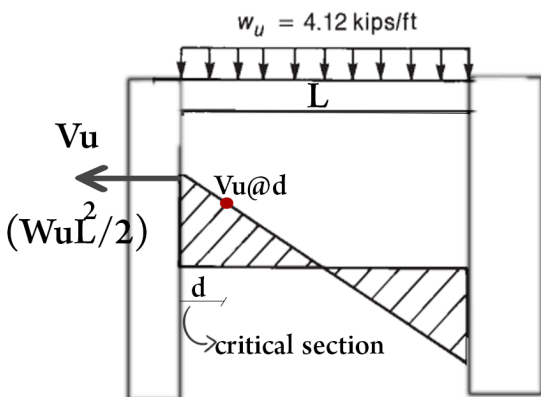
$V_c$  : concrete resistance strength

(Shear carried by the Conctere)

With stirrups :  $V_s$  : shear carried by the stirrups

$$V_n = V_c + V_s \quad V_n: \text{nominal shear strength}$$

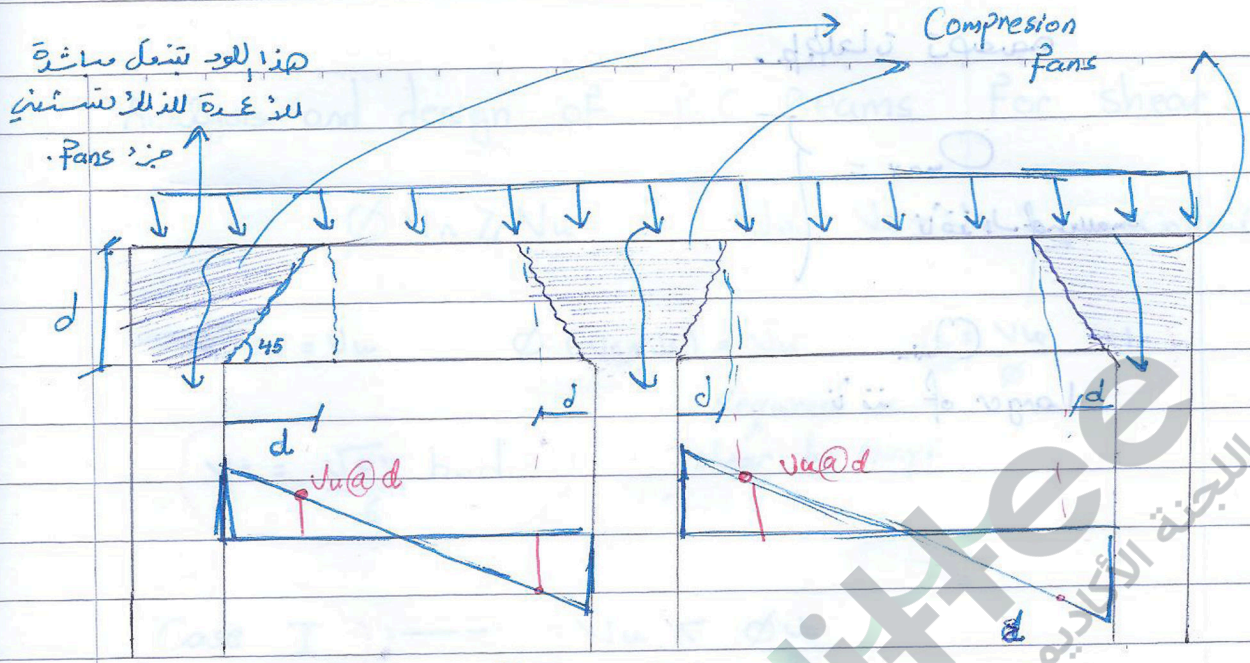
$$\Phi V_n \geq V_u \quad \Phi \text{ in shear is always} = 0.75$$



$V_u$  : at face of the support

لكن نحن بنتعامل بحساباتنا مع  $V_u@d$

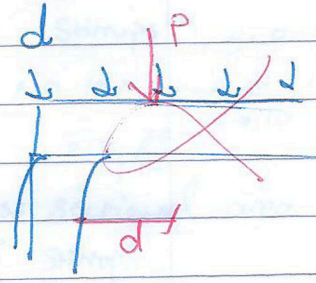
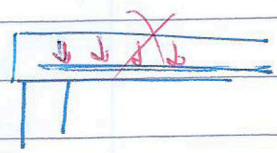
$d$  : effective depth



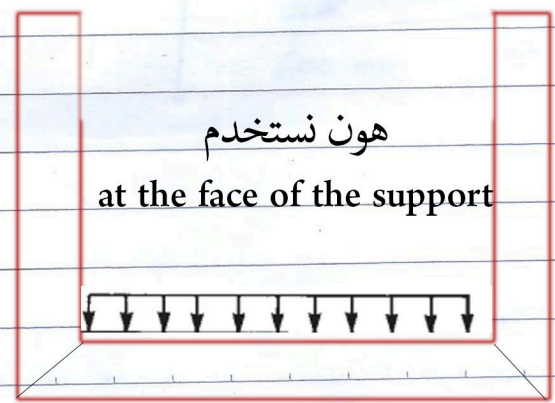
د في د مكانه نمنع به انه لانه لازية تتساوى 945

use  $V_u @ d$  only if :-

- 1- Support reaction ~~reduces~~ introduces Compression into the end region of the beam.
- 2- loads are applied into the top of the beams
- 3- No concentrated force within a distance  $d$  from the face of the support.



Analysis



# Analysis and design of R.C Beams For shear.

$\phi V_n \geq V_u$        $V_n = V_c + V_s$       at Critical Section

$\phi V_n = V_u$

$\phi (V_c + V_s) = V_u$

$V_s = \frac{V_u}{\phi} - V_c$

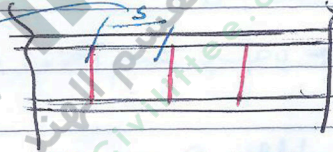
Required shear by stirrups

$V_c = \frac{\sqrt{F_c} b w d}{6}$

Case I :  $V_u \leq \frac{\phi V_c}{2}$

No need for shear reinforcement (لا حاجة لشد) (لا حاجة لشد). (لا حاجة لشد وقاوم الشد)

Stirrups ستخدم في حالة الحاجة لشد فقط



في حالة قوة الشد أكبر من spacing المنصوص عليه في الكود.

Case II :-

$\frac{\phi V_c}{2} < V_u < \phi V_c$

min reinforcement

Smaller of =

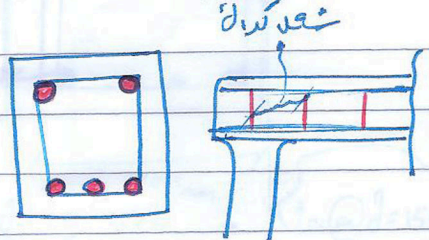
- $\frac{16 A_w f_y}{\sqrt{f_c} b}$
- $\frac{A_w f_y}{0.33 b}$
- $d/2$
- 600 mm

لأن الشد أكبر من قدرة الشد في الخرسانة

Stirrups 10 mm NO 10 mm

$A_w = 2 A_{w1} = 2 \times \frac{\pi}{4} (10)^2 = 157$


$A_{w1}$  : Cross sectional area of stirrups



**Case III** :- and  $V_u > \phi V_c$   
 $V_s \leq \frac{2}{3} \sqrt{f_c'} b_w d \rightarrow 4 V_c$

$S = \text{smallest of}$

- $600 \text{ mm or } \frac{d}{2}; \text{ if } V_s \leq 2V_c$
- $300 \text{ mm or } \frac{d}{4}; \text{ if } V_s > 2V_c$
- $\frac{A_v f_y}{0.33 b_w}$
- $\frac{16 A_v f_y}{b_w \sqrt{f_c'}}$
- $\frac{A_v f_y d}{V_s}$



Dr. Hazim Dwairi

\*  $V_{s \text{ max}} = 4 V_c$

max shear carried by stirrups  
 if  $V_s > V_{\text{max}}$  then enlarge the section

$V_{s \text{ max}} = \frac{2}{3} \sqrt{f_c'} b_w d$  (b and h)  
 \* يجب عدم تجاوز  $4V_c$  والى يزيد  
 • h و b

$V_{u \text{ max}} = \phi (V_c + V_{s \text{ max}}) = 5 \phi V_c$

IF  $V_u < V_{u \text{ max}}$  O.K  $V_u > V_{u \text{ max}}$  enlarge the section

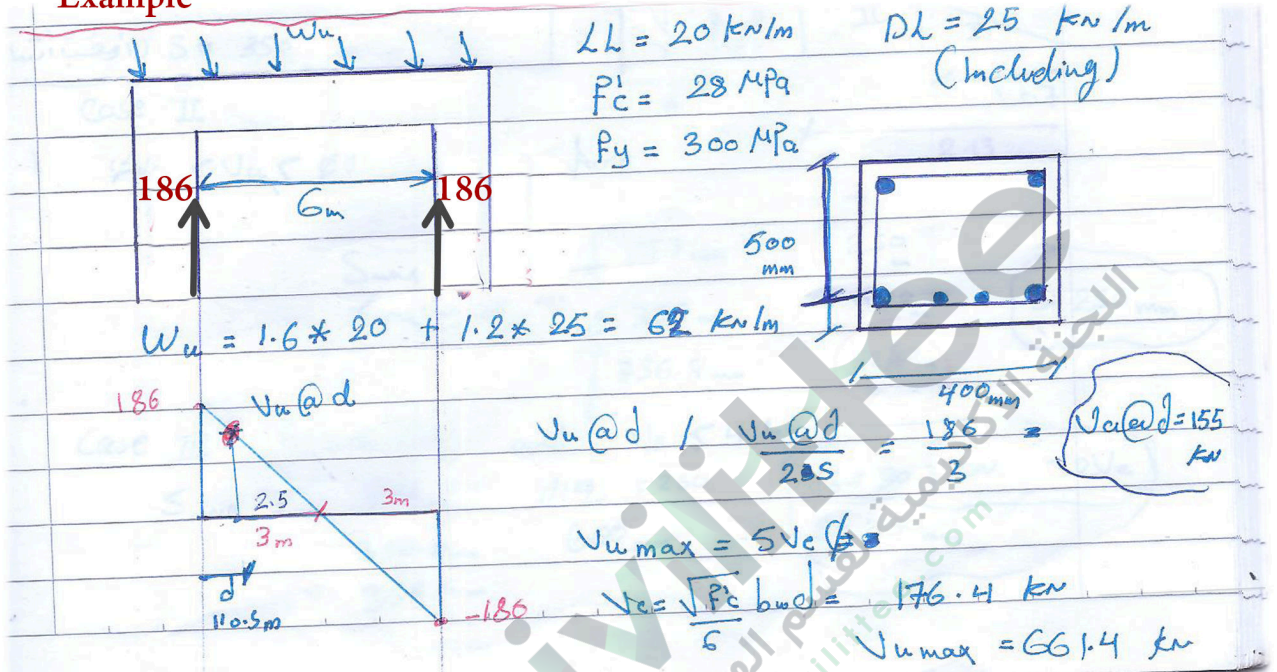
بالتالي لو طلب الماكس شيير كامل فهو :

$$V_u \max = \Phi (V_c + V_{s \max}) = 5 \Phi V_c$$

if  $V_u < V_{\max}$  then ok

if  $V_u > V_{\max}$  then enlarge the section

**Example**



$V_u @ d < V_{u, \max}$  O.K

$\frac{\phi V_c}{2} = 66.15$        $\phi V_c = 132.3$       ? Case

$V_s = \frac{V_u @ d}{2} - V_c = 30.3 \text{ kN}$

$V_u @ d > \phi V_c$        $1.07$

Case I

No need to shear reinforcement

$S = 350 \text{ mm}$

Case II

$\frac{\phi V_c}{2} < V_u < \phi V_c$  min reinfere

$S_{\max} = \begin{cases} 777 \text{ mm} & 250 \text{ mm} \\ \text{Smaller of} & 356 \text{ mm} & 600 \text{ mm} \\ & 356.8 \text{ mm} & 250 \text{ mm} \end{cases}$

Case III  $V_u > \phi V_c$  and  $V_s < 4V_c$

$S_{\max} = \begin{cases} 777 \text{ mm} & d/4 = 250 \\ 356.8 \text{ mm} & 600 \text{ mm} \\ 356.8 \text{ mm} & \end{cases}$

$V_s = 30.3 \text{ kN} < 2V_c$   
 $S = 250 \text{ mm}$

مطالعة ذاتية

Cases of loading

$L_L = 20 \text{ kN/m}$

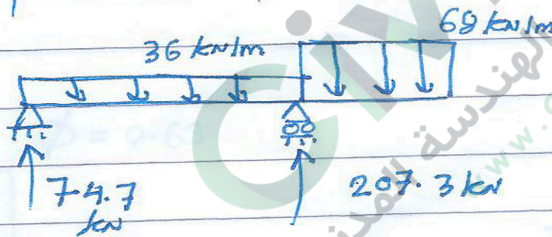
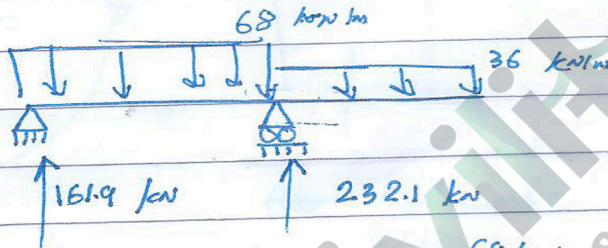
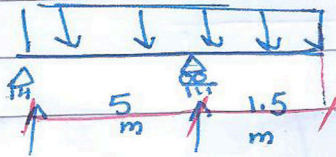
$D_L = 30 \text{ kN/m}$

$1.6 \times 20 = 32$

$1.2 \times 30 = 36$

$W_u = 68 \text{ kN/m}$

$w_t = 68 \text{ kN/m}$



Reaction من الحالات الثلاثة

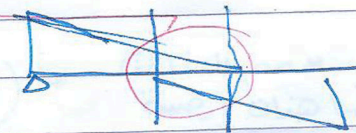
$R_A = 161.9 \text{ kN}$

نقطة آبرضاة لـ

$R_B = 287.3 \text{ kN}$

Shear (cu) dia \*  
Moment dia

عم اسلاك التبريد  
منه في نقطة التبريد  
Case I

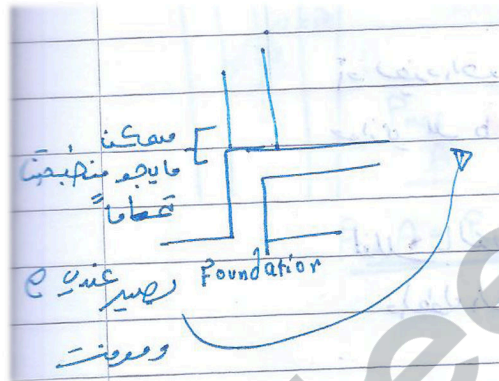
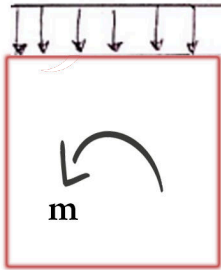


# Design of Coloumns

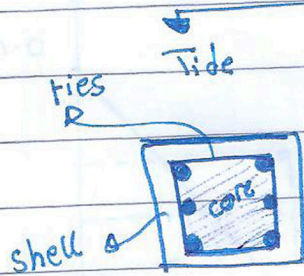
Combined axial loads and bending

Normal stress  $\sigma = p/a$

bending  $\sigma = My/I$

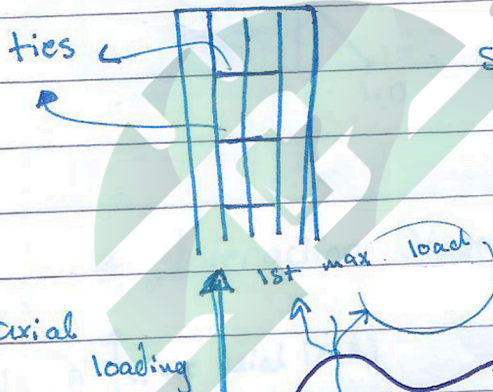
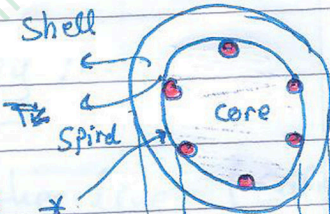


## Coloumns

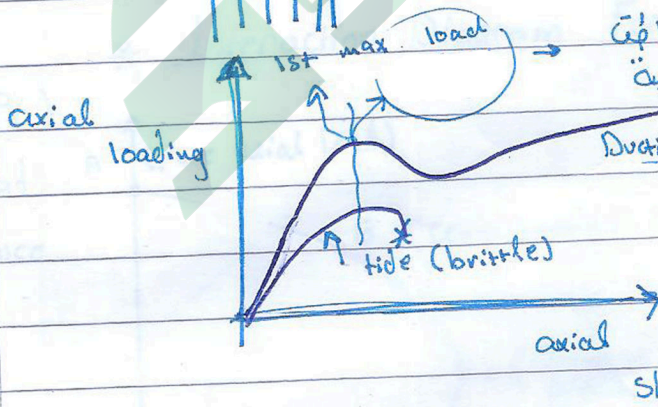


$\phi = 0.65$

$\phi = 0.75$  Spinal



More Confining \*  
For the core  
 $S_{max} = 75$  mm  
Spacing \*  
Ductility \*

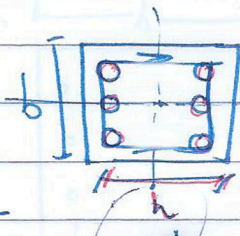


Spinal (low membered  
high cost)

Tide (high membered  
low cost)

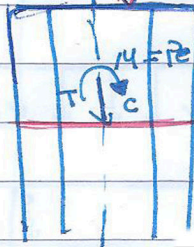
Cross Sectional Area (Spinal)  $\leftarrow$  Cross Sectional Area (Tide)

\* Interaction Diagram



$$\frac{P}{A} + \frac{My}{I} = f_{cu} \text{ (compressive strength)}$$

\* ترتيب الاعداد جهز اشكال (ماتحة)  
 دونه  $I = \frac{bh^3}{12}$  تعطيني قيمة آخر



**Interaction equation**

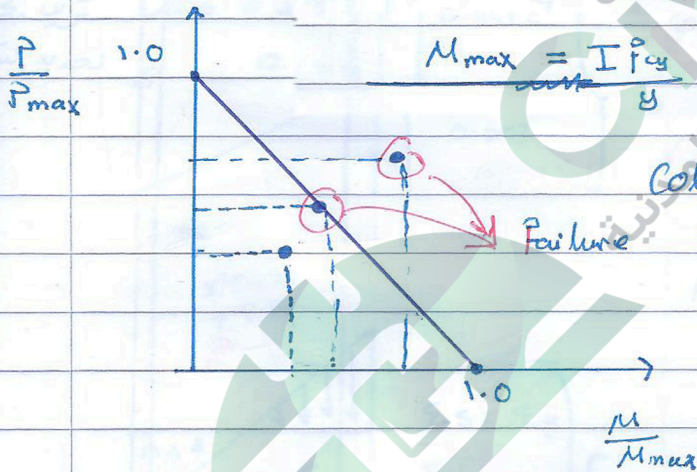
$$\frac{P}{f_{cu} A} + \frac{My}{f_{cu} I} = 1.0$$

$$\frac{P_{max}}{A} \leftarrow \frac{P}{f_{cu} A} \quad \frac{f_{cu}}{I} = \frac{M_{max} y}{I}$$


---


$$\frac{P}{P_{max}} + \frac{M}{M_{max}} = 1.0$$

$f_{cu} A = P_{max}$  (Max axial load of the column can support)

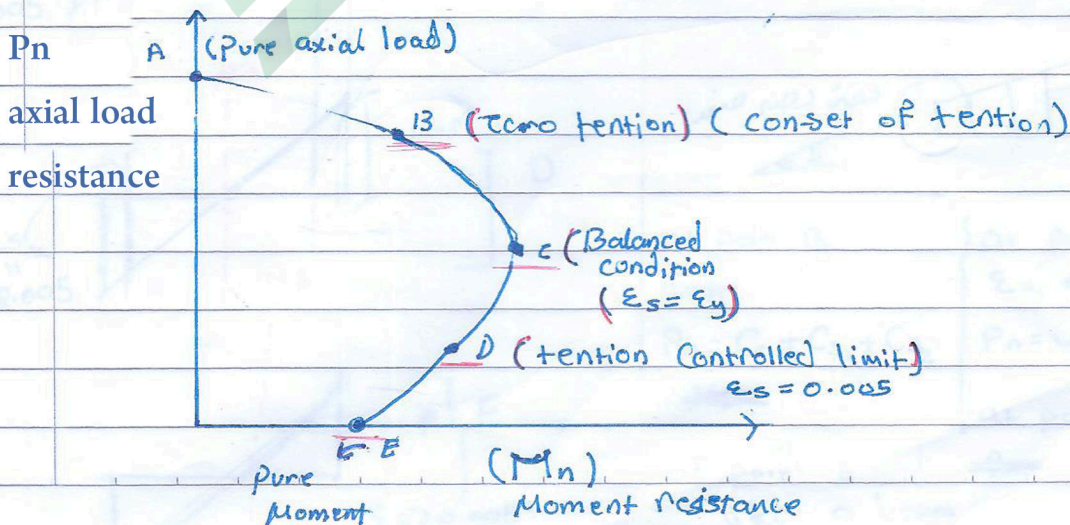


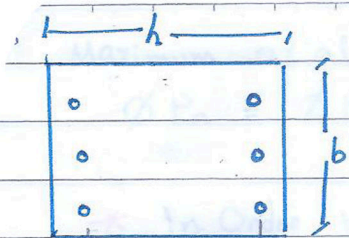
$$M_{max} = \frac{I f_{cy}}{y} \text{ (القيمة القصوى للمoment)}$$

Column Capacity :

under the line (safe)  
 on or above the line (not safe)

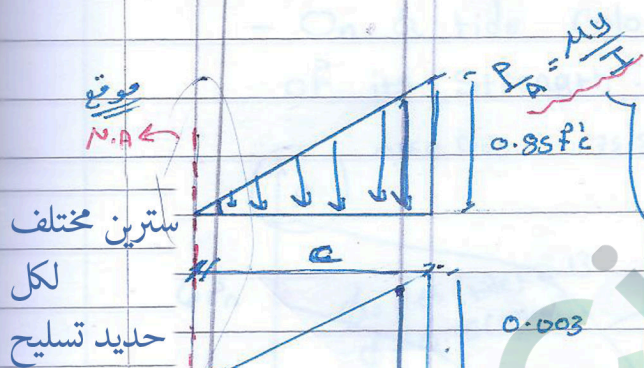
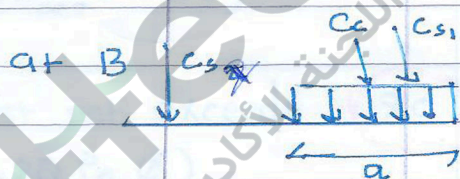
\* Interaction Diagram for Concrete Columns:





مقدار السترين بالحديد في حالة الـ pure load هو : (أجا فاينل)

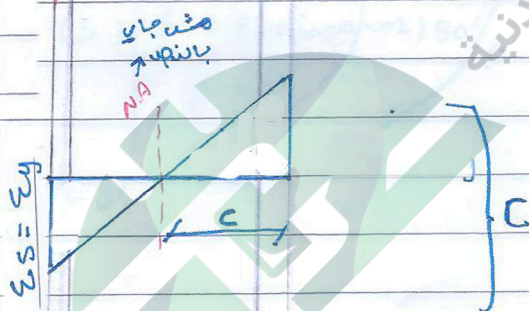
هو 0.003



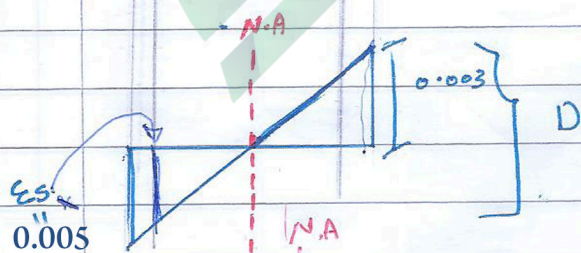
Comp تباد

(zero tension)

لجدهاي، لنقطة يبدأ القنشة



توضيح كل نقطة من النقاط في الصفحة الجاي

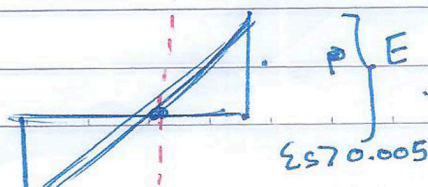


معلومة جدا هامة ..

كيف تميز بين h و b للعمود :

h : عمودي على axis of bending

أو يفرد الحديد دائماً باتجاه b



# Calculation of Interaction Diagram \*<sub>-</sub>

Point A (Pure axial load)  $A_g$ : cross sectional area (bh)

$$P_n = 0.85 f'_c (A_g - A_s) + A_s f_y \quad M_n = 0.0$$

Point B

①  $C = h$     ②  $a = c \beta$

③ نجد  $\epsilon_{s2}$  و  $\epsilon_{s1}$  من  $\epsilon_{s1} > \epsilon_{s2}$  بالانتشار

④ نشك في  $\epsilon_y$   $\epsilon_{s2} > \epsilon_y$   $f_s = f_y$

⑤  $C_c = 0.85 f'_c \times a \times b$

$C_{s1} = f_s \times \frac{A_s}{2}$  نعم إذا  $\epsilon_{s2} < \epsilon_y$   $f_s = f_y$

(Comp block واقع داخل)  $C_{s2} = \frac{A_s}{2} (f_s \text{ or } f_y - 0.85 f'_c)$

طرحنا لأنه يدي السترس تاع الحديد دون الكونكرت عشانه داخل بالبلوك يكونو مع بعض

\*  $P_n = C_c + C_{s1} + C_{s2}$

\*  $M_n = C_c \left(\frac{h}{2} - \frac{a}{2}\right) + C_{s1} \left(\frac{h}{2} - d'\right) + C_{s2} \left(\frac{h}{2} - d'\right)$

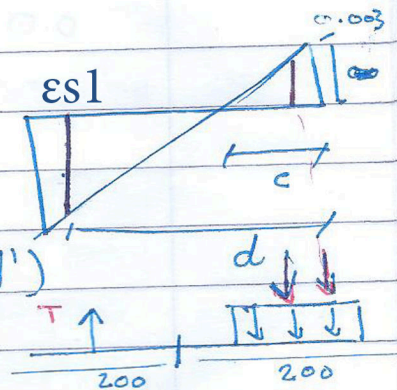
Point C (Balanced condition)

$\frac{\epsilon_{s1}}{d-c} = \frac{0.003}{c}$  find c  $\epsilon_{s1} = \epsilon_u$

$\frac{\epsilon_{s2}}{c-6s} = \frac{0.003}{c}$  find  $\epsilon_2$

$P_n = C_c + C_{s2} \ominus T_{s1}$

$M_n = C_c \left(\frac{h}{2} - \frac{a}{2}\right) + C_{s1} \left(\frac{h}{2} - d'\right) \oplus T_{s1} \left(\frac{h}{2} - d'\right)$



Point D

Tension Controlled limit :

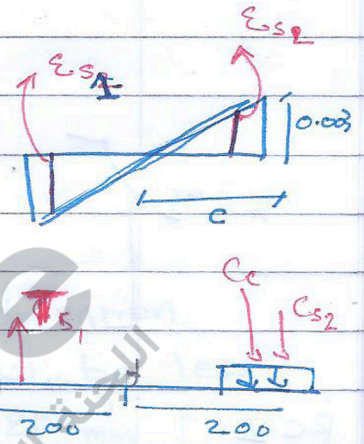
$$\epsilon_{s1} = 0.005$$

$$\frac{\epsilon_{s1}}{d-c} = \frac{0.003}{c} \quad (\text{نسبة } c)$$

$$\frac{\epsilon_{s2}}{c-65} = \frac{0.003}{c}$$

$$P_n = C_c + C_{s2} - T_{s1}$$

$$M_n = \epsilon M_\phi = C_c (200 - \frac{a}{2}) + C_{s2} (200 - 65) + T_{s1} (200 - 65)$$

Point E

Pure Bending (Ignore Comp reinforcement)

①

$$T = C$$

$$0.85 f'_c \cdot a \cdot b = \left(\frac{A_s}{2}\right) F_y$$

$A_s$  (تأخرت، لتتشنه) أو  $A_s$

$$a = \quad c =$$

$$\textcircled{2} \quad \epsilon_s = ? > \epsilon_y$$

$$\textcircled{3} \quad M_n = A_s F_y (d - \frac{a}{2})$$

$$P_n = 0.0$$

أنواع الأعمدة (تسميات)

Pure axial eccentricity تتعرض للود بدون مومنت مفي

uni axial eccentricity تتعرض لمومنت نتيجة eccentricity حول محور واحد إما X وإما y

bei axial eccentricity يتعرض لمومنت حول محورين X و Y

## Point E pure bending

ignore compression reinforcement

T=C

$$0.85f'_c ab = \frac{A_s \text{ total}}{2} f_y$$

دائماً هون

أس2 أو تاع التنشن

then find a= and c=

2-check  $\epsilon_s \geq \epsilon_y$  ?

$$3-M_n = A_s f_y (d - 0.5a)$$

$P_n = 0.0$

As total/2

Maximum axial load :

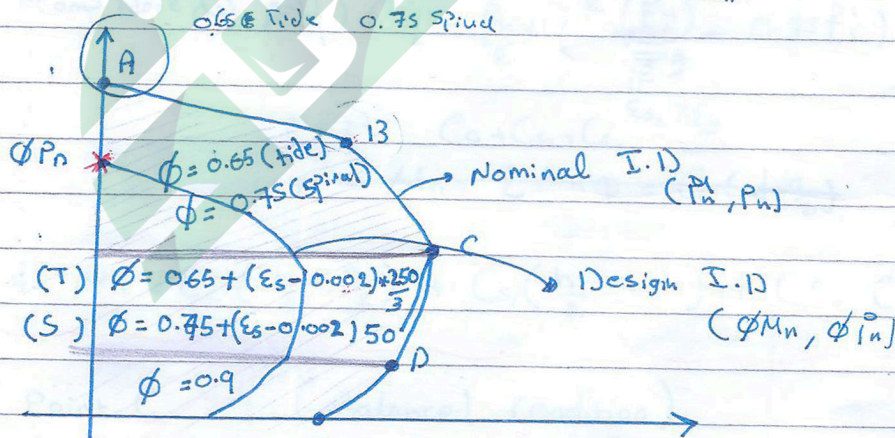
$$\phi P_n = \phi P_{n_{max}} = \phi [0.85 F'_c (A_g - A_s) + A_s f_y]$$

$A_g$ : cross sectional area (bh)

\* In Order to account the effect of accidental Moments :  
the ACI specifies that the max load on :

- On a spiral column must not exceeds **85%**  
of its strength. ( $\phi P_{n_{max}} * 0.85$ )

- On a tide column must not exceeds **80%**  
of its strength. ( $0.8 P_n \phi$ )



مهم جدا جدا بالامتحان إذا طلب منك maximum axial load اتبع الخطوات الاتية

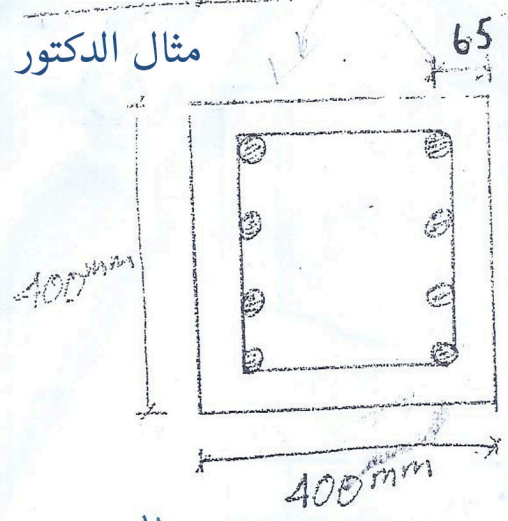
(1) جد  $\phi P_n$  من المعادلة فوق

(2) حدد هو tide ولا spiral

(3) قلّه  $0.8 \phi P_n$  or  $0.85 \phi P_n$  but it must not exceeds

واحسبه  $0.85 \phi P_n$  أو  $0.8 \phi P_n$  حسب نوع العمود

Example: - Calculation of Interaction Diagram.



مثال الدكتور

$f_c = 35 \text{ MPa}, f_y = 420 \text{ MPa}$

$A_s = 8 \text{ NO. } 29 \text{ M} = 5160 \text{ mm}^2$

Point A: Pure Axial load.

$P_n = 0.85 f_c' (A_g - A_s) + A_s f_y$

$P_n = 0.85 \times 35 \times (400 \times 400 - 5160) + 5160 \times 420$

$P_n = 6773.69 \text{ kN}$   
 $M_n = 0.0$

العمود  
 axis of bending

Point B: - zero Tension

$c = 400 \text{ mm} \Rightarrow a = \beta_1 c$

$\beta_1 = 1.09 - (0.008 \times 35)$

$\beta_1 = 0.81$

$\Rightarrow a = 0.81 \times 400$

$a = 324 \text{ mm}$

\*  $\frac{0.003}{400} = \frac{\epsilon_{s1}}{65} = \frac{\epsilon_{s2}}{400 - 65}$

$\Rightarrow \epsilon_{s1} = 4.875 \times 10^{-4} < \epsilon_y$   
 ( $f_{s1} \neq f_y$ )

$\epsilon_{s2} = 0.0025 > \epsilon_y$

$f_{s1} = 4.875 \times 10^{-4} \times 200,000 = 97.5 \text{ MPa}$

( $f_{s2} = f_y$ )

$C_c = 0.85 \times 35 \times (324 \times 400) = 3855.6 \text{ kN}$

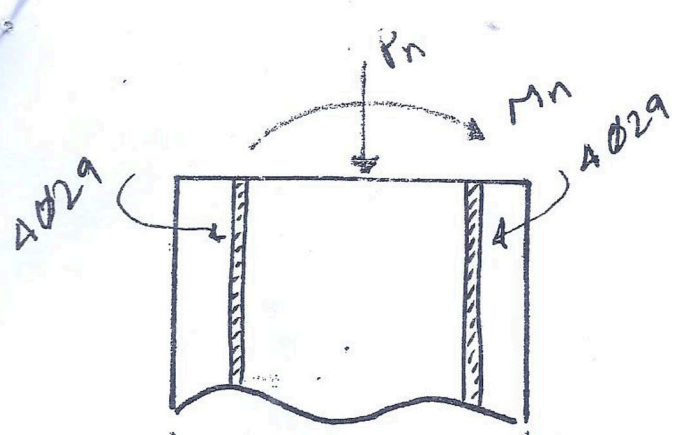
$C_{s1} = 2580 \times 97.5 = 251.55 \text{ kN}$

com  
 stress

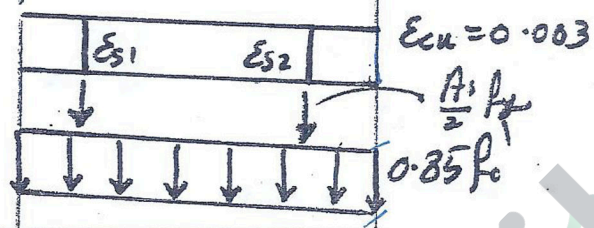
$C_{s2} = \frac{2580}{A_{s2}} (420 - 0.85 \times 35) = 1006.8 \text{ kN}$

\*  $P_n = C_c + C_{s1} + C_{s2} = 5114 \text{ kN}$

$M_n = \sum M_i = C_c \left( \frac{200}{2} - \frac{a}{2} \right) + C_{s1} \left( \frac{200}{2} - d' \right) + C_{s2} (200 - d)$   
 $= 3855.6 \times (200 - \frac{324}{2}) + 251.55 \times (200 - 65) + 1006.8 \times (200 - 65)$   
 $= 1.125 \text{ kN.m}$

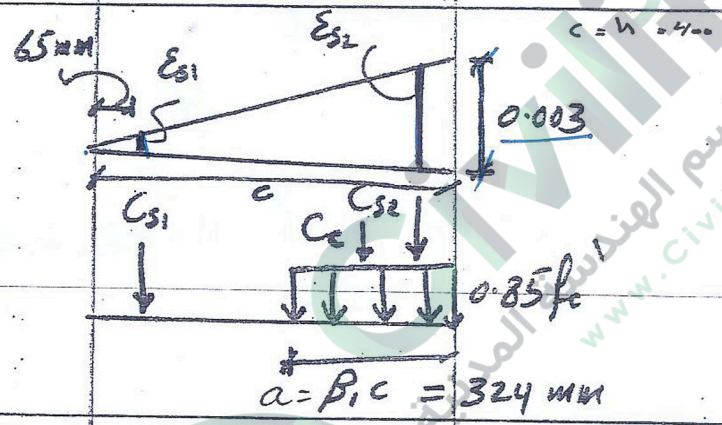


Point A



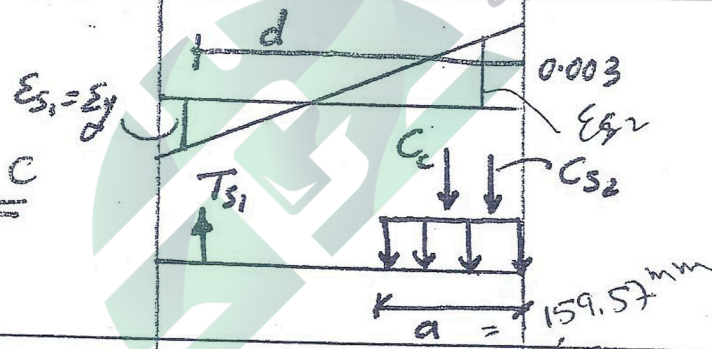
$P_n = 6773.69$   
 $M_n = 0.0$

Point B



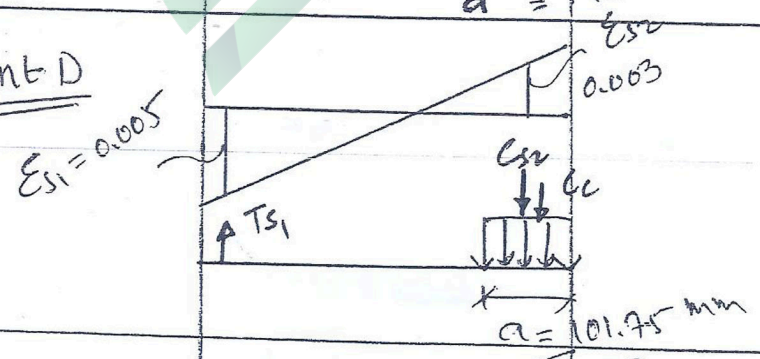
$P_n = 5114 \text{ kN}$   
 $M_n = 248.5 \text{ kN.m}$

Point C



$P_n = 1775.8 \text{ kN}$   
 $M_n = 504 \text{ kN.m}$

Point D



$P_n = 797.36 \text{ kN}$   
 $M_n = 417.32 \text{ kN.m}$

$\epsilon_{s1} > 0.005$

$P_n = 0.0$   
 $M_n = 313.67 \text{ kN.m}$

Point C - Balanced Condition

$$\frac{\epsilon_{s1}}{d-c} = \frac{0.003}{c} \quad \epsilon_{s1} = 0.0021$$

$$\Rightarrow c = 197 \text{ mm}$$

$$a = 0.81 \times 197 = 159.57 \text{ mm}$$

$$\frac{\epsilon_{s2}}{c-65} = \frac{0.003}{c} \Rightarrow \epsilon_{s2} = 0.00201 < \epsilon_y$$

$$\Rightarrow f_{s2} = 0.00201 \times 200,000 = 402 \text{ MPa}$$

$$C_c = 0.85 f'_c a b = 0.85 \times 35 \times 159.57 \times 400 = 1899 \text{ kN}$$

$$C_{s2} = 2580 (402 - 0.85 \times 35) = 960.4 \text{ kN}$$

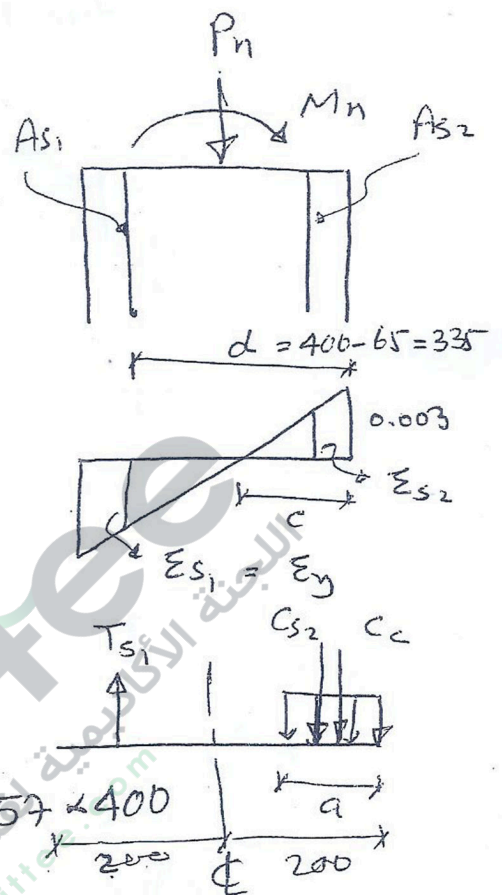
$$T_{s1} = 2580 + 420 = 1083.6 \text{ kN}$$

$$P_n = C_c + C_{s2} - T_{s1} = 1775.8 \text{ kN}$$

$$M_n = \sum M \phi$$

$$= 1899 \left( 200 - \frac{159.57}{2} \right) + 960.4 \times (200 - 65)$$

$$+ 1083.6 \times (200 - 65) = 504 \text{ kN.m}$$



Point D: Tension Controlled - limit.

$$\frac{\epsilon_{s1}}{335-c} = \frac{0.003}{c} \quad ; \quad \epsilon_{s1} = 0.005$$

$$\Rightarrow c = 125.6 \text{ mm}$$

$$a = 0.81 \times 125.6 = 101.75 \text{ mm}$$

$A_{s2}$  (within  $a$ )

$$\frac{\epsilon_{s2}}{c-65} = \frac{0.003}{c} \Rightarrow \epsilon_{s2} = 0.001447 < \epsilon_y$$

$$\Rightarrow f_{s2} = 0.001447 \times 200,000 = 289.5 \text{ Mpa.}$$

$$C_c = 0.85 \times 35 \times 101.75 \times 400 = 1210.8 \text{ kn.}$$

$$C_{s2} = 2580 \times (289.5 - 35 \times 0.85) = 670.16 \text{ kn.}$$

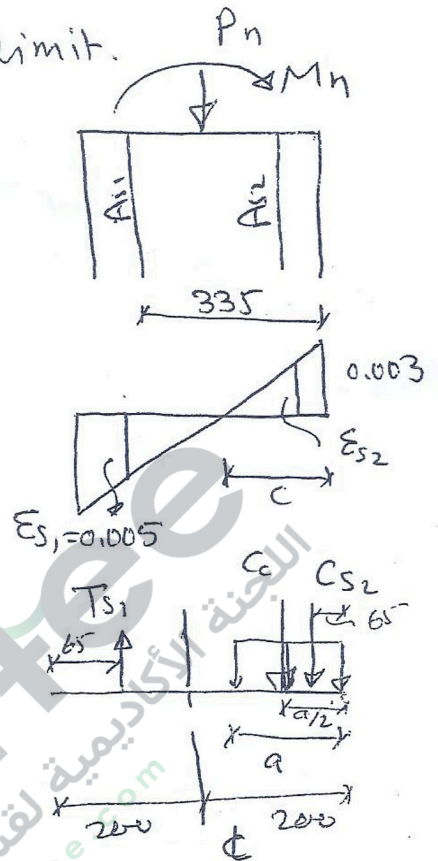
$$T_{s1} = 2580 \times 420 = 1083.6 \text{ kn.}$$

$$P_n = C_c + C_{s2} - T_{s1} = \cancel{2914.56} \text{ kn. } 797.36$$

$$M_n = \sum M \phi$$

$$= 1210.8 \times \left(200 - \frac{101.75}{2}\right) + 670.16 \times (200 - 65) + 1083.6 \times (200 - 65)$$

$$= 417.32 \text{ kn.m/}$$



Point E: Pure Bending. (Beams)

Ignore Comp. reinforcement ( $A_s2$ )

$c = T$

$0.85 \times 35 \times a \times 400 = 2580 \times 420$

$a = 91.05 \text{ mm}$

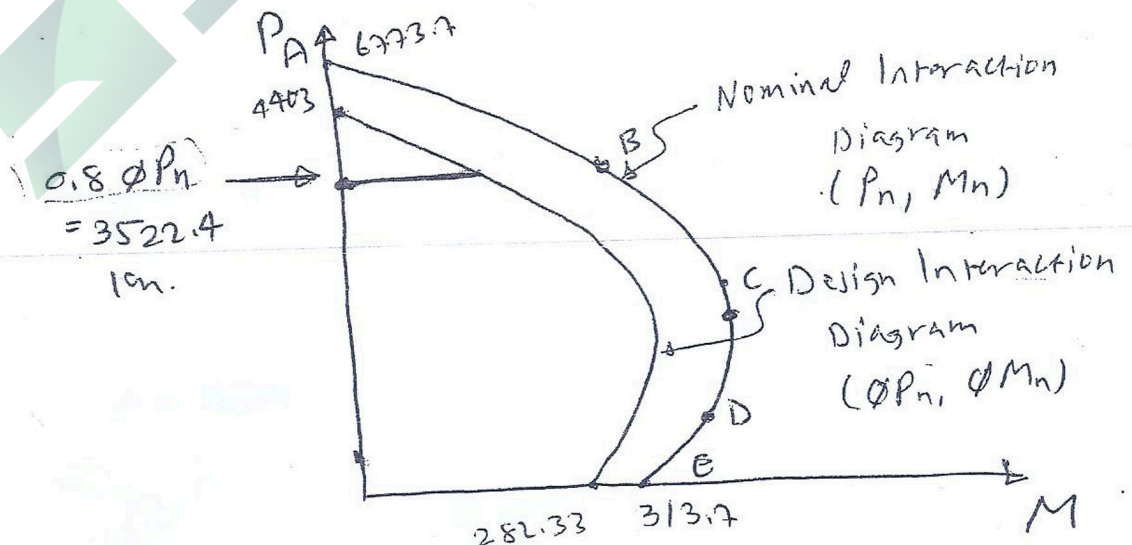
$c = \frac{91.05}{0.81} = 112.41 \text{ mm}$

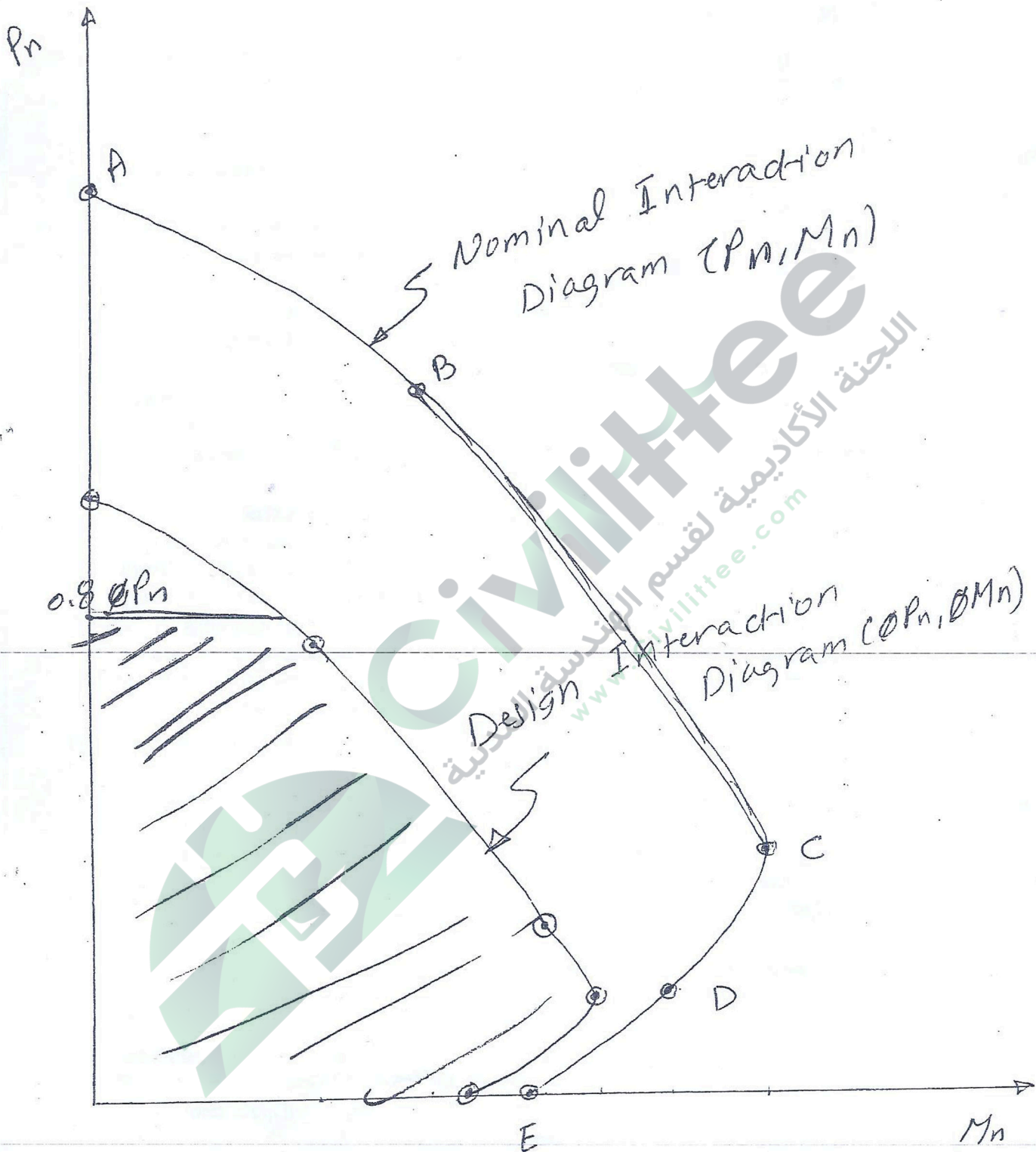
$\epsilon_s = 0.003 \left( \frac{335 - 112.41}{112.41} \right) = 0.00594 > \epsilon_y$

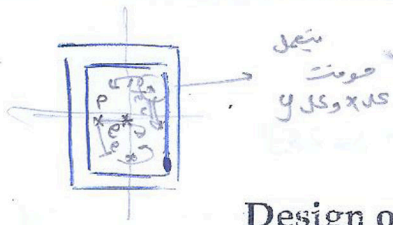
$M_n = A_s1 \cdot f_y \left( d - \frac{a}{2} \right)$   
 $= 2580 \times 420 \left( 335 - \frac{91.05}{2} \right) = 313.67 \text{ kNm}$

$P_n = 0.0$

Point	$\epsilon_t$	$\phi$	$P_n$ (kn)	$M_n$ (kn.m)	$\phi P_n$ (kn)	$\phi M_n$ (kn.m)
A	—	0.65	6773.7	0.0	4403	0.0
B	0.0004875	0.65	5114	248.5	3324.1	161.5
C	0.0021	0.65	1775.8	504	1154.3	327.7
D	0.005	0.9	797.36	477.32	717.62	375.59
E	0.00594	0.9	0.0	313.67	0.0	282.3







## Design of Short Columns:

-Slender or Long Columns and Short Columns

$$M @ \text{ends} = Pe$$

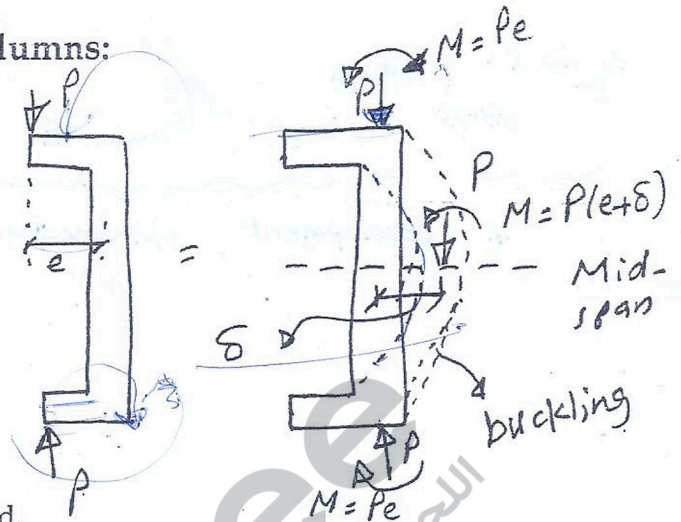
$$M @ \text{midheight} = P(e + \delta)$$

-The deflection increases the moment for which the column must be designed.

- Because of the increase in the maximum moment due to deflections, the axial-load capacity is reduced.

This reduction in the axial-load capacity results from what are referred to as slenderness effects.

A slender column is defined as a column that has a significant reduction (>5%) in its axial-load capacity due to moments resulting from lateral deflections of the column.



### Choice of materials properties and reinforcement ratios :

-In small buildings,  $f'_c$  in columns  $\approx f'_c$  in floors  $\approx 28 - 31$  MPa.

-In tall buildings,  $f'_c$  in columns  $> f'_c$  in floors, to reduce the column size.

-Per ACI code section  $0.01 \leq \rho_{st} \leq 0.08$

Although the code allows  $\rho_{max} = 0.08$  it is generally very difficult to place this amount of steel in a column, particularly if lapped splices are used.

Example: 400mm X 400mm column,  $A_{st} = 0.08 \times 400 \times 400 = 12,800 \text{ mm}^2$

If No. 25M used  $\rightarrow$  25 bars are required.

It will be difficult to place 25 bars in a 400X400 mm column.

- Tables A-10 and A-11 give  $\rho_{max}$  for various column sizes for square and circular columns. (3-5 or 6%).
- Most economical tied-column sections  $\rightarrow \rho_{st}$  (1-2)%.
- For Spiral columns  $\rho_{st}$  (2.5-5)%, because they resist higher axial loads.
- Per ACI code: Min. No. of bars in a tied column is 4. and Min. No. of bars in a spiral column is 6.
- Almost universally: an even No. of bars is used in a rectangular column maintain symmetry about the axis of bending. All bars are the same size.

### Estimating the column size:

For very small values of moment, the column size is governed by the maximum axial load capacity

-For tied columns

$$A_g(\text{trial}) \geq \frac{P_u}{0.4(f'_c + \rho F_y)}$$

$\rho \approx 0.015$

-For spiral columns

$$A_g(\text{trial}) \geq \frac{P_u}{0.5(f'_c + \rho F_y)}$$

$\rho \approx \frac{\pi}{4} \delta^2$

axial load

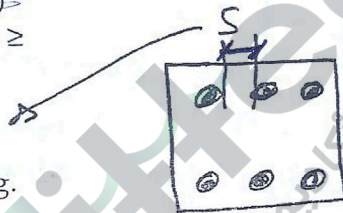
Both of these equations will tend to under estimate the column size if there are moments present, because they correspond roughly to the horizontal line portion of the  $\phi P_n, \phi M_n$  interaction diagram.

Although the ACI - Code does not specify a minimum column size, the min. dimension of a cast-in-place tied column should not be less than 8 in (200mm) and preferably not less than 10 in (250mm). The diameter of spiral column should not be less than 12 in (300mm).

**Bar spacing requirements and cover requirements:**

- Per ACI code, the clear cover  $\geq 1.5$  in (40 mm)
- Min clear distance between longitudinal bars  $\geq$

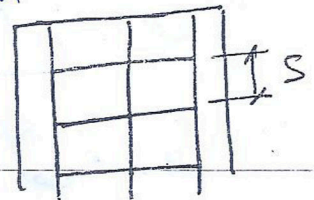
Larger of { 1.5 db  
1.5 in (40mm)  
 $1\frac{1}{2}$  Max. size of coarse Agg.



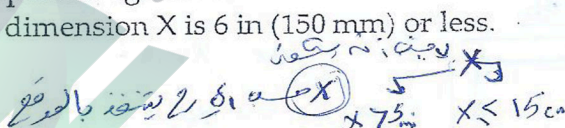
Clear distance limitation also apply to lap-spliced bars.

**Spacing for Ties:**

$S_{max}$  shall not exceed (smaller of) maximum { 16 db  
48  $d_t$  }  $\rightarrow$  dia of tie  
Least dimension of the column (b)



A bar is adequately supported against lateral movements if it is located at a corner of a tie and if the dimension X is 6 in (150 mm) or less.



**Choice of Column Type:**

$e/h$  = Eccentricity Ratio

$\frac{M}{P} = e$

$e/h < 0.10$   
Small eccentricity  
small moment

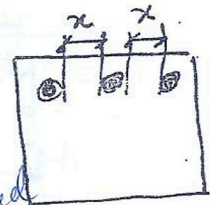
Spiral column is more efficient; in terms of load capacity,  $\phi = 0.70$  (S) and  $0.65$  (T). In terms of maximum axial load capacity,  $0.85\phi P_n$  (S) and  $0.8\phi P_n$  (T)

$e/h > 0.20$   
Large eccentricity  
Large Moment

A tied column with bars in the faces farthest from the axis of bending is most efficient. Even more efficiency can be obtained by using a rectangular column to increase the depth perpendicular to the axis of bending.

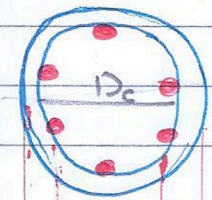
$e/h < 0.20$  and M exists about both axes

A Tied column with bars in four faces are used.



$$A_g = \frac{\pi}{4} D^2$$

مشاهدة



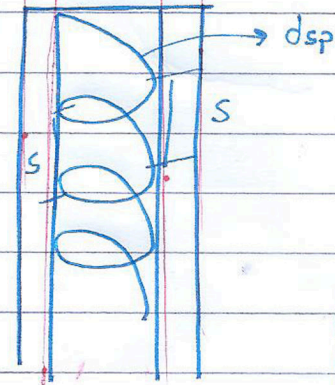
$$S_{max} = \frac{\pi d_{sp}^2 f_y}{0.45 D_c P_c' \left( \frac{A_g}{A_c} - 1 \right)}$$

$$A_g = \frac{\pi}{4} D^2$$

$$A_c = \frac{\pi}{4} D_c^2$$

$D_c$ : diameter of Core

لعمري يقرب لا أقل



$$S_{max} = 75 \text{ mm}$$

$$S_{min} = \text{larger of } \begin{cases} 25 \text{ mm} \\ 1.33 \text{ Max Core Agg} \end{cases}$$

مهم سبب استخدام الـ min

to avoid problems in Concrete placing

طبع أقل من min

Use min

طبع أكبر من max

Use max

بعد ما تطلع S من المعادلة فوق

شيك على الماكس 75mm و الـ min

وإنتبه بالامتحان إن أعطاك الـ diameter كامل اطرح منه  $2 \times \text{cover}$  عشان يعطيك  $D_c$

خطوات تصميم tide colomun

(1) جد  $A_g$  ثم إما بعطيك  $h$  أو  $b$  وإما بقلك square عندها  $h=b$  والان نجيب الابعاد من  $A_g=bh$

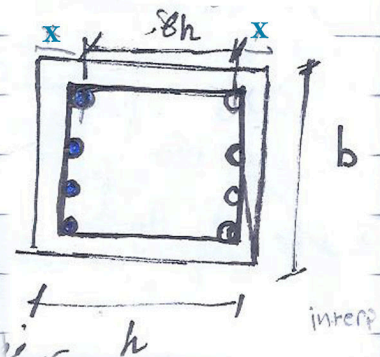
(2) تستطيع التقريب للأكبر بالابعاد... بمحدد لك بالامتحان قطر الحديد والمطلوب الان جد  $\gamma$  كالتالي

$$h = \gamma * h + 2 X$$

حيث  $X = \text{cover} + d_s + d_b/2$

يا إما تطلع معك  $\gamma$  عدد موجود بالجدول أو بينهم

بينهم لازم تستخدم الرسمتين نسوي interpolation



$$\Phi M_n = M_u$$

$$\Phi P_n = P_u$$

(3) استخدام الرسومات أول شي جد  $\frac{\Phi M_n}{f_c b h^2}$  و  $\frac{\Phi P_n}{f_c b h}$  مهم جدا تعرف إنه

تابع الصفحة

الجاي

بتوجد  $\rho$  أو 2 من  $\rho$  وبتعمل interpolation إذا أكثر من غاما

(4) تشييك على  $\rho$  لازم  $0.01 \leq \rho_{st} \leq 0.08$  لكن برضه ما لازم تطلع عن 0.04 إذا أكثر استخدم 0.04

(5) الان نجد  $As$  حيث  $As = \rho bh$  ثم جيب الprovided من الجدول (اختر عدد قضبان حديد زوجي)

(7) الان تحديد spacing of bars

(6) الان تحديد spacing of ties ولازم تحفظ الاتي

احفظ برضه  
Larger of

1.5 db  
1.5 in (40mm)  
1 1/2 Max. size of course Agg.

Spacing for Ties:

$S_{max}$  shall not exceed

(smaller of)

maximum

16 db

48 (dt)

Least dimension of the column (b)

(8) check  $S_{min}$  value of X أوجد X من قانون ال  $b_{min}$  حيث  $x$  نفسه  $S_{min}$

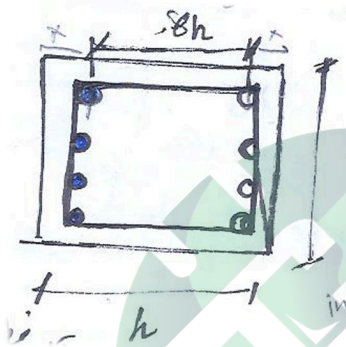
ويجب أن يكون  $S_{min} \leq X \leq 15 \text{ cm}$

Design the colomun which  $P_u=1550\text{Kn}$  square colomun

$M_u=150\text{Kn}$   $f'_c=20\text{Mpa}$   $f_y=420\text{Mpa}$

$$A_g = P_u / 0.4(f'_c + \rho f_y) \quad A_g = 1550 \cdot 1000 / 0.4(20 + 0.015 \cdot 420) \quad A_g = 147338 \text{mm}^2$$

$$b=h \quad b \cdot b = h \cdot h = 147338 \quad b=h \quad 384 \text{ mm} \quad \text{تقريب } b=h=400 \text{mm}$$



$$X = 40 + 10 + 25/2 = 62.5 \text{mm}$$

$$h = \gamma \cdot h + 2x \quad \gamma = 0.69$$

القيمة بين الرسمتين لذلك بدنا تستخدم الرسمتين ونسوي انتربوليش

$$\frac{\phi P_n}{F'_c b h} = \frac{1550 \times 10^3}{20 \times 400 \times 400} = 0.48 \quad \frac{\phi M_u}{F'_c b h^2} = \frac{150 \times 10^6}{20 \times 400 \times 400^2} = 0.12$$

$$\gamma = 0.6 \quad \rho = 0.033$$

$$\gamma = 0.65 \quad \rho = ??$$

$$\gamma = 0.75 \quad \rho = 0.28$$

$$\rho = 0.03$$

$$P = 0.3 < P_{max} \quad \left. \begin{array}{l} P_{min} = 0.01 \\ \rho = 0.03 > P_{min} \\ o.k \end{array} \right\}$$

لازم تختار عدد قضبان الحديد زوجي حتى يكون سممترك

$$As = \rho bh = 4800 \text{mm} \quad \text{use } 10 \text{ No } 25 \text{M } As = 5100 \text{mm}$$

حسب القانون فوق  
now we get Spacing of ties (400mm or 488mm or 400mm) take 400mm

now find Spacing of bars ( $S_{min}$ ) then check X  $S_{min} = 40 \text{mm}$

$$X \cdot 4 + 2 \cdot (2ds - 0.5db) + 25 \cdot 5 + 2 \cdot 10 + 40 \cdot 2 = 400$$

$$S_{min} \leq X \leq 150 \text{mm}$$

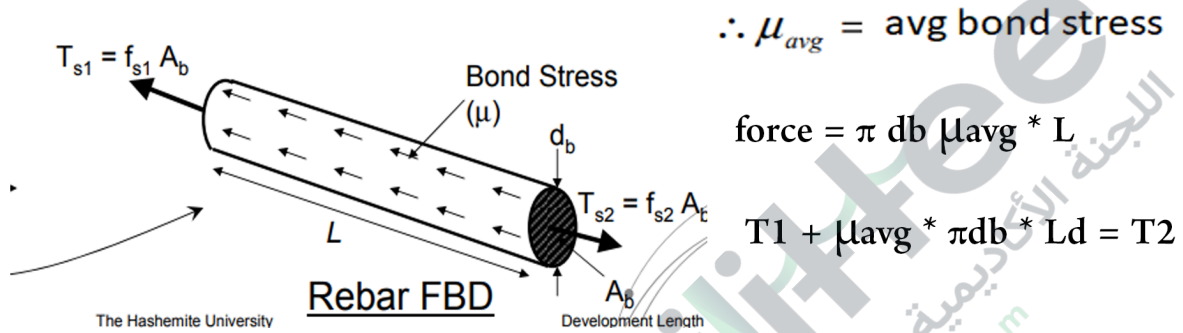
then ok

مهم جدا أوع تضربلي ب 10 بارز لأن نحن هون بنستخدم  
قضبان الي بمنطقة التشن فقط والي هي نص القضبان

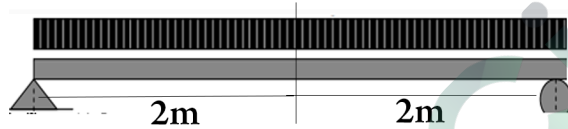
# Development length

Development length : is the shortest length in the bar in which bar stress can increase from zero to  $f_y$

if the distance from a point where the bar stress equal  $f_y$  to the end of the bar is less than  $(L_d)$  then the bar will pullout of the concrete because there is not enough bond stress to produce equilibrium



ينتقل ال bond stress باتجاه T الأقل



لازم أقارن  $L_d$  مع  $L$  حيث  
 $L$  من نقطة الماكس المومنت لنهاية الحديد حيث  
السترس صفر

هون مثلا : لو طلعت  $L_d = 1.5$  فهو ok أما لو طلعت  $L_d = 2.5$  إذا كان continuous بمد الحديد  
وإن لم يكن نستخدم hooks

2/c

Development length Anchoring

Reinforced Concrete Design I

Development Length of Straight Bars and Standard Hooks

For deformed bars, ACI318-05 Section 12.2.2 defines the development length  $l_d$  given in the table below. Note that  $l_d$  shall not be less than 300 mm.

Case	$\leq \phi 20$	$> \phi 20$
<p>Case 1: Clear spacing of bars being developed not less than <math>d_b</math>, clear cover not less than <math>d_b</math>, and stirrups throughout <math>l_d</math> not less than code minimum</p> <p>حدد الحالة بالأول بعدها اختر القانون المناسب</p> <p>or</p> <p>Case 2: Clear spacing of bars being developed not less than <math>2d_b</math> and clear cover not less than <math>d_b</math></p>	<p><math>S \geq d_b</math> <math>Cov \geq d_b</math></p> $l_d = \frac{f_y \alpha \beta \lambda}{2.1 \sqrt{f_c}} d_b$	$l_d = \frac{f_y \alpha \beta \lambda}{1.7 \sqrt{f_c}} d_b$
Other cases	$l_d = \frac{f_y \alpha \beta \lambda}{1.4 \sqrt{f_c}} d_b$	$l_d = \frac{f_y \alpha \beta \lambda}{1.1 \sqrt{f_c}} d_b$

The terms in the foregoing equations are as follows:

$\alpha$  = reinforcement location factor

- Horizontal reinforcement so placed that more than 300 mm of fresh concrete is cast in the member below the development length ..... 1.3
- Other reinforcement ..... 1.0

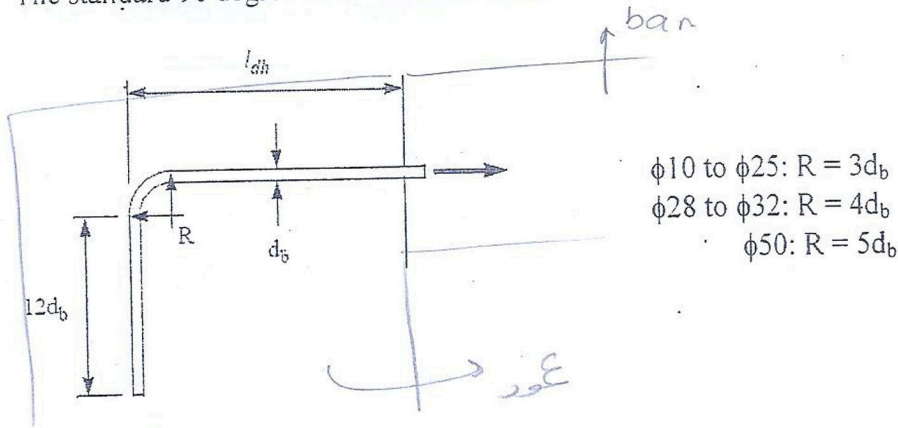
$\beta$  = coating factor

- Epoxy-coated bars with cover less than  $3d_b$ , or clear spacing less than  $6d_b$  ..... 1.5
- All other epoxy-coated bars ..... 1.2
- Uncoated reinforcement ..... 1.0

$\lambda$  = lightweight aggregate concrete factor

- When lightweight concrete is used ..... 1.3
- Normal weight concrete is used ..... 1.0

When there is insufficient length available to develop a straight bar, standard hooks are used. The standard 90 degree hook is shown below:

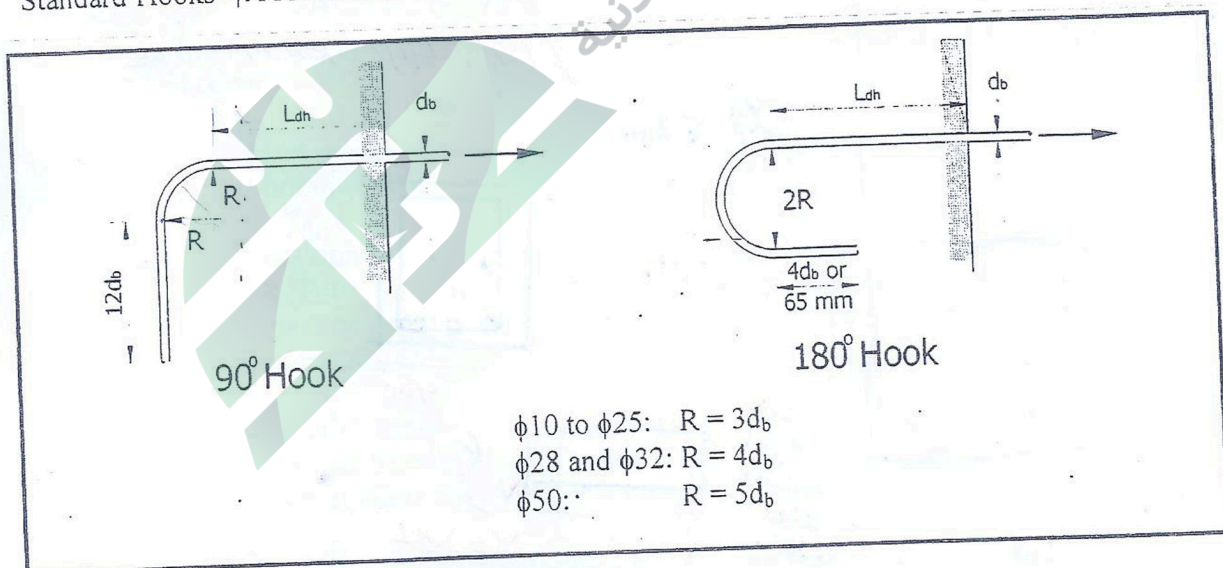


The development length of a hook,  $l_{dh}$ , is given by the following equation. Note that the development length shall not be less than  $8d_b$  nor less than 150mm:

$$l_{dh} = \frac{0.24 f_y \beta \lambda}{\sqrt{f_c}} d_b \geq \text{larger of } \begin{cases} 8d_b \\ 150\text{mm} \end{cases}$$

where  $\beta$  = the coating factor = 1.2 for epoxy coated bars and 1.0 for uncoated reinforcement, and  $\lambda$  is the lightweight aggregate factor = 1.3 for lightweight aggregate concrete. For other cases  $\beta$  and  $\lambda$ , shall be taken as 1.0

Standard Hooks - ACI sections 7.1 and 7.2.1

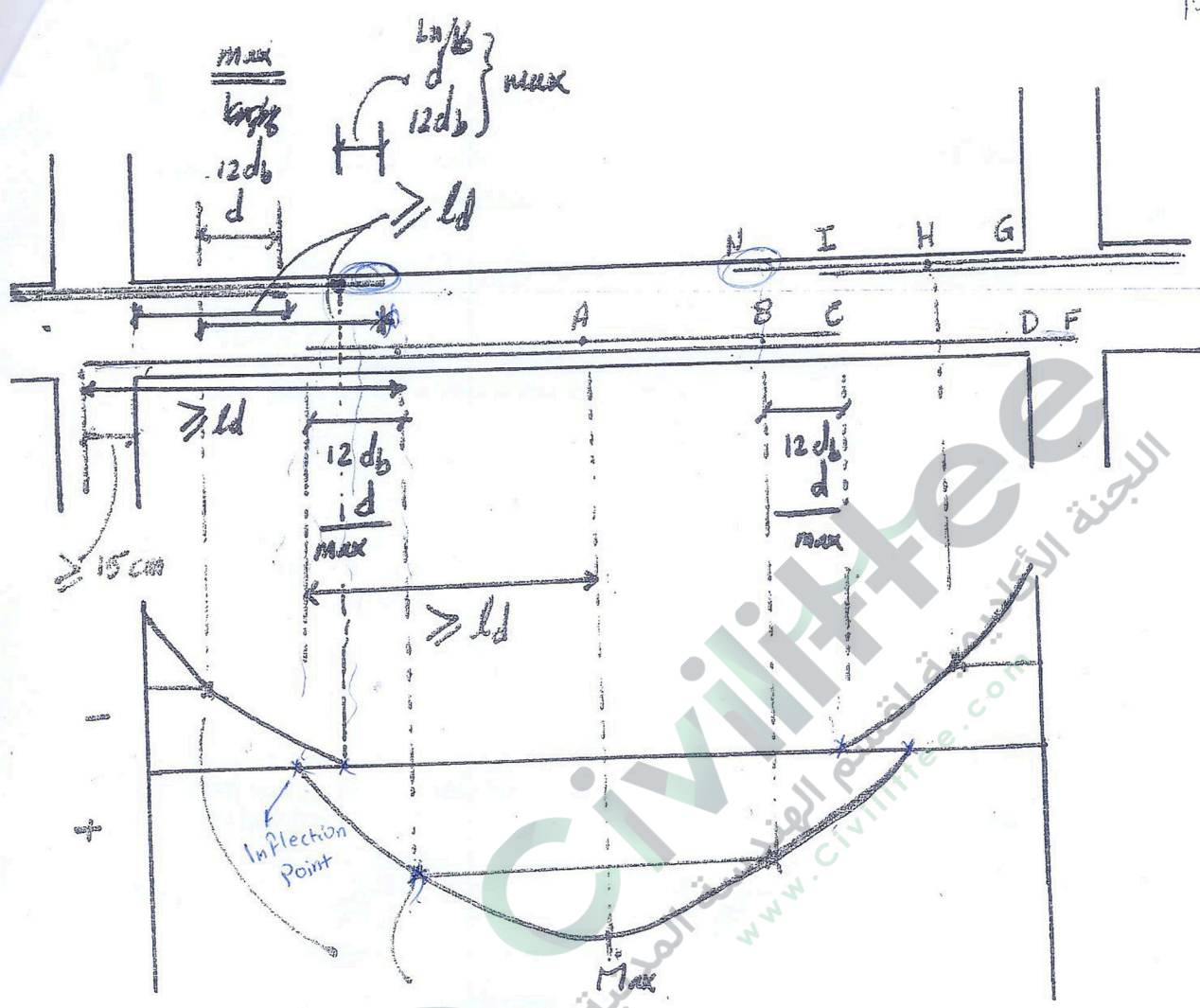


## Bar Cutoffs:

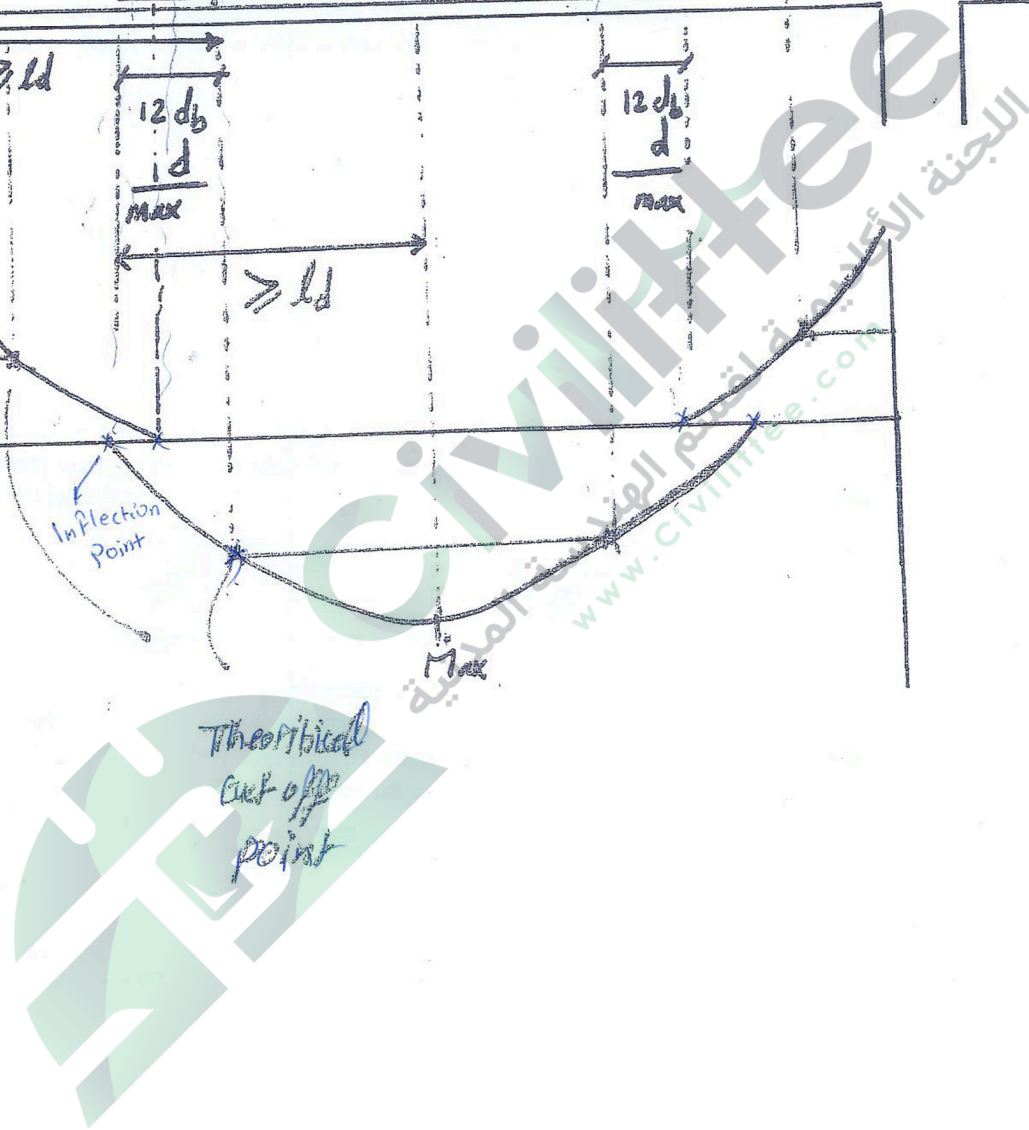
Bars can be cutoff where they are no longer needed to resist tensile forces or where the remaining bars are adequate to do so. The following rules apply per the ACI code:

مصنوع لوقوف الحديد فيها

1. Every bar must continue a distance ( $d$  or  $12d_b$ ) beyond the theoretical cutoff point. (B-C) & (H-I).
2. Full development length  $l_d$  must be provided beyond the critical sections (A-C) & (B-F). Critical sections include points of maximum positive and negative moments and points where reinforcing bars adjacent to the bar under consideration are cutoff or bent.
3. At least  $A_s^+/3$  (one – third of the positive moment reinforcement) but not less than two bars in simple spans or  $A_s^+/4$  in continuous spans must be continued at least 15cm into the supports. (D-F).
4. At least  $A_s^-/3$  must be extended beyond the point of zero moment a distance not less than  $d$  or  $12d_b$  or  $l_n/16$ .
5. Cutoff 50% of the positive moment steel and extend the other 50% into the support.
6. At least  $A_s^+/4$  at mid span, not less than two bars, shall be spliced at or near the mid span.
7. At least  $A_s^-/6$  shall be spliced at or near mid span.

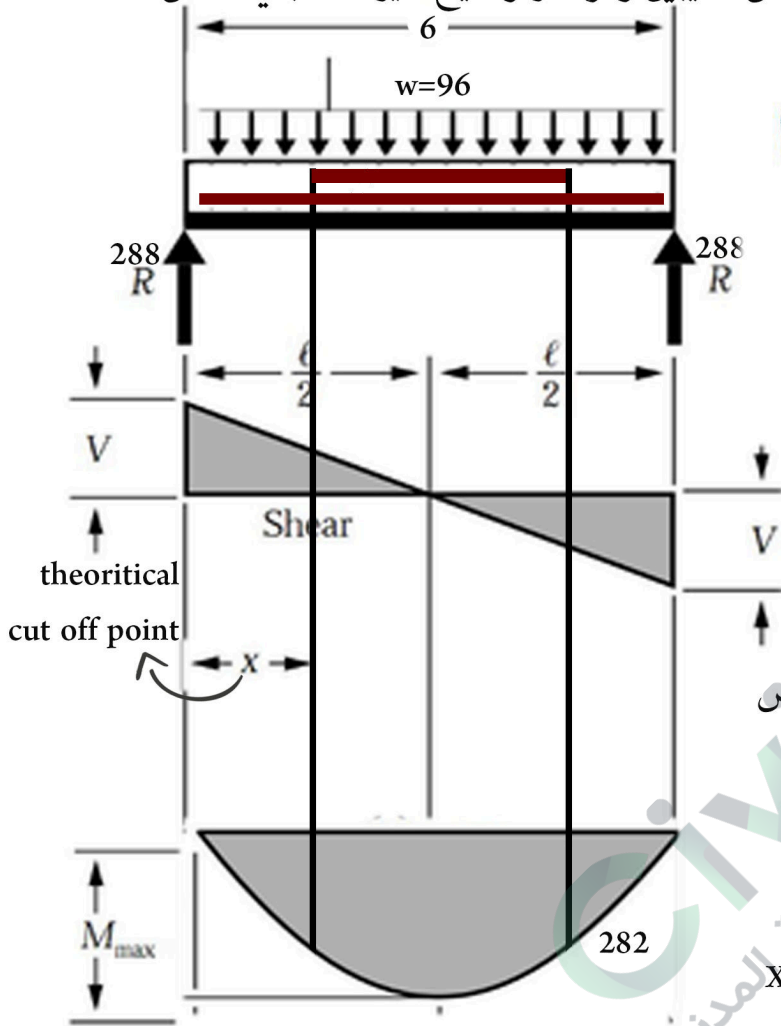


Theoretical  
cut off  
point

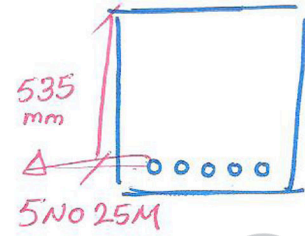


بيحي السؤال مثلا جد ال theoretical cut off point بعد قص قضيبين وهون ركن منيح كثير لان الباقي 3 مش تحط 2

الحديد الكلي 5 قضبان

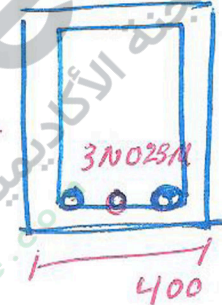


بعد التصميم



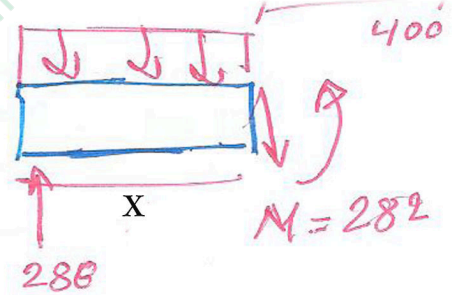
$\phi M_n = 440 \text{ kN.m}$

نحسب اسبب  $\phi M_n$  للقضبان بعد القص



$\phi M_n = 282$

نحسب X بأخذ سكتشن بطول X



$X = 1.23$

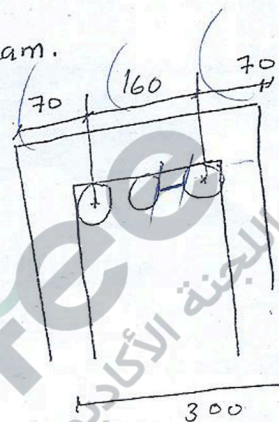
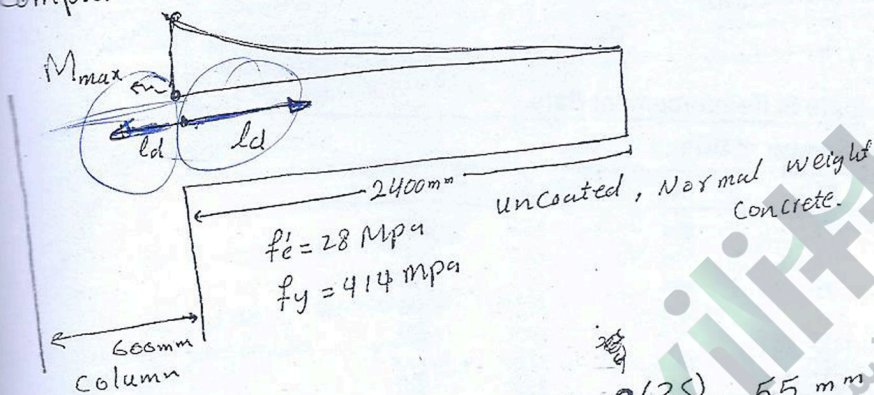
2 No 25  $L = 1.75 \text{ m}$   
3 No 25  $L = 3 \text{ m}$

both are ok

# مثال مهم من دوسية الطالب لطف الصباري

## Example

Comput  $l_d$  for the  $3\phi 25$  in the cantilever beam.



محور  
البيضاوي

Sol:-

clear spacing bet. bars =  $\frac{300 - 2(70) - 2(25)}{2} = 55 \text{ mm}$

$d_b = 25 \text{ mm}; 2d_b = 50 \text{ mm} \rightarrow 55 > 2d_b$  Case 2

table

طول اليبس في جهة  
اليمين المتأخر

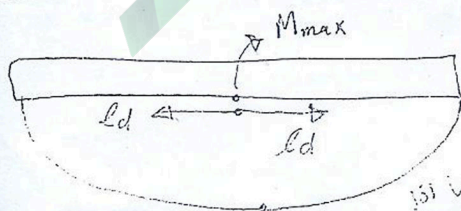
$l_d = \frac{f_y \phi_b \cdot 2}{1.7 \sqrt{f_c}} \cdot d_b = \frac{414 \cdot 1.3 \cdot 1 \cdot 1}{1.7 \sqrt{28}} \cdot 25 = 1495.74 \text{ mm}$

but  $l_d = 1495.74 > 600 \text{ mm} \rightarrow$  المسافة المتاحة  
داخلة اليبس  
في كل سبار  $M_{max}$

So, provide  $90^\circ$  hook

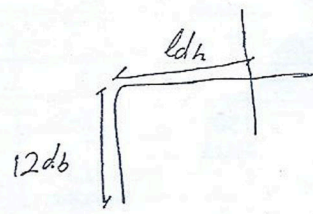
check  $l_{dh} = \frac{0.24 \cdot 414 \cdot 1 \cdot 1}{\sqrt{28}} \cdot 25 = 469 \text{ mm} < 600 \text{ mm}$

OK

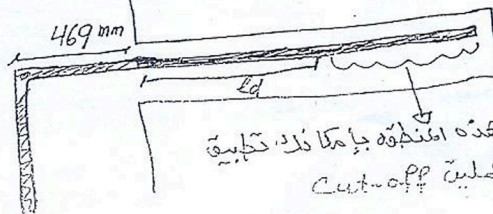


لو كان  $S \leq S$

نوجد  $l_d$   
ونضاد ذلك مع جدول  
طول اليبس في كل سبار  
لو كان  $S \leq S$  for work



التمساح النهائي لليبس



لهذه المنطقة بما كان ذلك تطبيقه  
كلية Cut-off

هنا تنتهي مادة RC one  
سأقوم بإرفاق ملف ملحق بأسئلة السنوات الفايصل محلولة قبيل الامتحان  
ياذن الله

وفي حال لاحظت أي خطأ أو عندك استفسار بالدوسية أو لطلب الملحق  
الالكترونياً

تواصل معي على الفيس:

<https://www.facebook.com/ezrawille>

بالتوفيق للجميع أتمنى أني لم أقصر في هذا الملخص  
سائلاً منكم الدعاء بالتوفيق ...  
ودعائي لكم بالموفقية والنجاح الدائم

عز الدين عاشور

TABLE A-4 Total Area (in.<sup>2</sup>) of Multiple U.S. Reinforcement Bars

Bar No.	Number of Bars					
	1	2	3	4	5	6
3	0.11	0.22	0.33	0.44	0.55	0.66
4	0.20	0.40	0.60	0.80	1.00	1.20
5	0.31	0.62	0.93	1.24	1.55	1.86
6	0.44	0.88	1.32	1.76	2.20	2.64
7	0.60	1.20	1.80	2.40	3.00	3.60
8	0.79	1.58	2.37	3.16	3.95	4.74
9	1.00	2.00	3.00	4.00	5.00	6.00
10	1.27	2.54	3.81	5.08	6.35	7.62
11	1.56	3.12	4.68	6.24	7.80	9.36

TABLE A-4M Total Area (mm<sup>2</sup>) of Multiple SI Reinforcement Bars

Bar No.	Number of Bars					
	1	2	3	4	5	6
10	71	142	213	284	355	426
13	129	258	387	516	645	774
16	199	398	597	796	995	1190
19	284	568	852	1140	1420	1700
22	387	774	1160	1550	1930	2320
25	510	1020	1530	2040	2550	3060
29	645	1290	1930	2580	3220	3870
32	819	1640	2460	3280	4090	4910
36	1010	2010	3020	4020	5030	6040

TABLE A-5 Minimum Beam Width (in.) for Multiple U.S. Bars per Layer; Interior Exposure<sup>a</sup>

Bar No.	Diameter (in.)	Number of bars in single layer				
		2	3	4	5	6
4	0.50	7.0	8.5	10.0	11.5	13.0
5	0.625	7.0	8.5	10.5	12.0	13.5
6	0.75	7.0	9.0	11.0	12.5	14.0
7	0.875	7.5	9.0	11.0	13.0	15.0
8	1.00	7.5	9.5	11.5	13.5	15.5
9	1.128	8.0	10.0	12.5	14.5	17.0
10	1.27	8.0	10.5	13.0	15.5	18.0
11	1.41	8.5	11.0	14.0	17.0	19.5

<sup>a</sup>Clear cover of 1.5 in.; No. 3 double-leg stirrup; 3/4 in. maximum-size aggregate.

7.7 — Concrete protection for reinforcement

7.7.1 — Cast-in-place concrete (nonprestressed)

The following minimum concrete cover shall be provided for reinforcement, but shall not be less than required by 7.7.5 and 7.7.7:

	Minimum cover, mm
(a) Concrete cast against and permanently exposed to earth	75
(b) Concrete exposed to earth or weather:	
No. 19 through No. 57 bars	50
No. 16 bar, MW200 or MD200 wire, and smaller	40
(c) Concrete not exposed to weather or in contact with ground:	
Slabs, walls, joists:	
No. 43 and No. 57 bars	40
No. 36 bar and smaller	20
Beams, columns:	
Primary reinforcement, ties, stirrups, spirals	40
Shells, folded plate members:	
No. 19 bar and larger	20
No. 16 bar, MW200 or MD200 wire, and smaller	15

9.5 — Control of deflections

9.5.1 — Reinforced concrete members subjected to flexure shall be designed to have adequate stiffness to limit deflections or any deformations that adversely affect strength or serviceability of a structure.

9.5.2 — One-way construction (nonprestressed)

9.5.2.1 — Minimum thickness stipulated in Table 9.5(a) shall apply for one-way construction not supporting or attached to partitions or other construction likely to be damaged by large deflections, unless computation of deflection indicates a lesser thickness can be used without adverse effects.

TABLE 9.5(a) — MINIMUM THICKNESS OF NONPRESTRESSED BEAMS OR ONE-WAY SLABS UNLESS DEFLECTIONS ARE COMPUTED

Member	Minimum thickness, <i>h</i>			
	Simply supported	One end continuous	Both ends continuous	Cantilever
Solid one-way slabs	$l/20$	$l/24$	$l/28$	$l/10$
Beams or ribbed one-way slabs	$l/16$	$l/18.5$	$l/21$	$l/8$

Notes:  
 1) Span length *l* is in mm.  
 2) Values given shall be used directly for members with normalweight concrete ( $w_c = 2300 \text{ kg/m}^3$ ) and Grade 60 reinforcement. For other conditions, the values shall be modified as follows:  
 a) For structural lightweight concrete having unit weight in the range 1500–2000  $\text{kg/m}^3$ , the values shall be multiplied by  $(1.65 - 0.0003 w_c)$  but not less than 1.09, where  $w_c$  is the unit weight in  $\text{kg/m}^3$ .  
 b) For  $f_c$  other than 420 MPa, the values shall be multiplied by  $(0.4 + f_c/700)$ .

TABLE 9.5(b) — MAXIMUM PERMISSIBLE COMPUTED DEFLECTIONS

Type of member	Deflection to be considered	Deflection limitation
Flat roofs not supporting or attached to nonstructural elements likely to be damaged by large deflections	Immediate deflection due to live load <i>L</i>	$l/180^a$
Floors not supporting or attached to nonstructural elements likely to be damaged by large deflections	Immediate deflection due to live load <i>L</i>	$l/360$
Roof or floor construction supporting or attached to nonstructural elements likely to be damaged by large deflections	That part of the total deflection occurring after attachment of nonstructural elements (sum of the long-term deflection due to all sustained loads and the immediate deflection due to any additional live load) <sup>†</sup>	$l/480^a$
Roof or floor construction supporting or attached to nonstructural elements not likely to be damaged by large deflections		$l/240^b$

<sup>a</sup> Limit not intended to safeguard against ponding. Ponding should be checked by suitable calculations of deflection, including added deflections due to ponded water, and considering long-term effects of all sustained loads, camber, construction tolerances, and reliability of provisions for drainage.  
<sup>†</sup> Long-term deflection shall be determined in accordance with 9.5.2.5 or 9.5.4.3, but may be reduced by amount of deflection calculated to occur before attachment of nonstructural elements. This amount shall be determined on basis of accepted engineering data relating to time-deflection characteristics of members similar to those being considered.  
<sup>b</sup> Limit may be exceeded if adequate measures are taken to prevent damage to supported or attached elements.  
<sup>c</sup> Limit shall not be greater than tolerance provided for nonstructural elements. Limit may be exceeded if camber is provided so that total deflection minus camber not exceed limit.