



Ex 8 water application

→ A lake of 40 km^2 lake receives average water flow of $(0.56 \text{ m}^3/\text{s})$ for the month of January while delivers $(0.48 \text{ m}^3/\text{s})$ as out flow. The cumulative precipitation for January is (45 mm) , while the cumulative evaporation is (125 mm) and the cumulative infiltration from the lake bottom is (25 mm) rate. the change in the lake water level???

*** Sol 8 ***

→ The change in the storage = $\Delta S = (U_{in} - U_{out})$

area = 40 km^2 ...

average water flow = $0.56 \text{ m}^3/\text{s}$... inflow...

delivers = $0.48 \text{ m}^3/\text{s}$... outflow...

Precipitation = 45 mm ... inflow...

Evaporation = 125 mm ... outflow...

Infiltration = 25 mm ... outflow...

→ Volume inflow $\text{Bo} (\text{m}^3)$

→ $(1 \text{ km}^2 \rightarrow 10^6 \text{ m}^2)$

$$\textcircled{1} 0.56 \frac{\text{m}^3}{\text{s}} * (60 * 60 * 24 * 30) = 1451520 \text{ m}^3 \rightarrow \text{(average water flow)}$$

$$\textcircled{2} 45 \text{ mm} * 40 \text{ km}^2 * 10^6 * 10^{-3} = 1800000 \text{ m}^3 \rightarrow \text{(precipitation)}$$

$$\sum \text{inflow} = 1451520 + 1800000 = 3251520 \text{ m}^3$$

→ Volume outflow $\text{Bo} (\text{m}^3)$

$$\textcircled{1} 0.48 \frac{\text{m}^3}{\text{s}} * (60 * 60 * 24 * 30) = 1166400 \text{ m}^3 \dots$$

$$\textcircled{2} 125 * 10^{-3} * 40 * 10^6 = 5000000 \text{ m}^3 \dots$$

$$\textcircled{3} 25 * 10^{-3} * 40 * 10^6 = 1000000 \text{ m}^3 \dots$$

$$\sum \text{outflow} = 1166400 + 5000000 + 1000000 = 7166400 \text{ m}^3$$

$$\therefore \Delta S = 3251520 - 7166400 = -3914880 \text{ m}^3 \rightarrow \text{To find the depth (m)}$$

$$\Rightarrow \text{The depth (m)} = \frac{m^3}{m^2} = \frac{3914880}{40 \times 10^6}$$

$$\therefore \text{depth} = \text{drop} = -0.097 \text{ m}$$

$$\approx -9.78 \text{ cm} \approx \boxed{10 \text{ cm}} \neq$$

*** Exo (drainage density) *** $\Rightarrow D = \frac{\sum L}{A}$

$$\hookrightarrow w_A \Rightarrow \text{have } (D=7)$$

$$w_B \Rightarrow \text{have } (D=3)$$

which is correct???

(a) Slope A > Slope of B

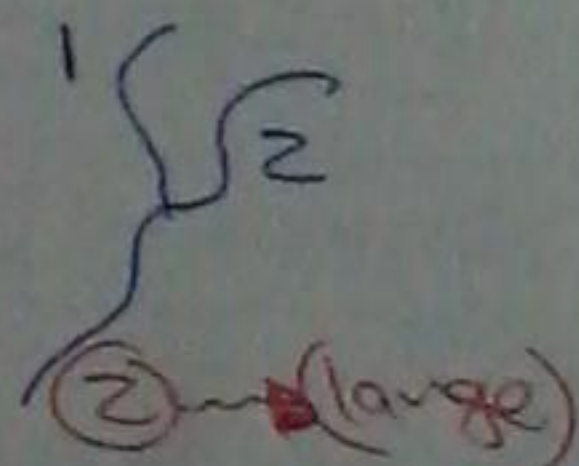
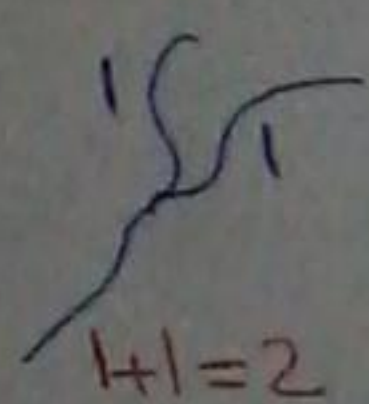
(b) Slope B > Slope of A

(c) Slope A = Slope of B

(d) No Relation...

*** Exo (stream order) ***

$$\hookrightarrow i+1 \Rightarrow \text{OR (large order) ...}$$



*** Exo (law of the stream number and the stream length) ***

$$\hookrightarrow \frac{N_i}{N_{i+1}} = R_n \Rightarrow N_i = R_n^{(K-i)} \Rightarrow (\text{Stream Number}) \dots$$

$$\frac{L_{i+1}}{L_i} = R_L \Rightarrow L_i = L_1 R_L^{(i-1)} \Rightarrow (\text{Stream length}) \dots$$

Ex (The expected value and the variance and standard deviation)...

Given a historical record of rainfall depth (x) for years (1995-2010) at a gauging station in Jordan. estimate the mean and the standard deviation of the rainfall depth

Year	Rainfall (x_i) (mm)	$x_i - \bar{x}$	$(x_i - \bar{x})^2$
1995	212	37.6875	1203.2
1996	123	54.2125	2949.8
1997	156	21.2125	454.2
1998	225	47.7875	2274.1
1999	134	43.2125	1876
2000	175	2.2125	5.3
2001	237	59.7875	3562.6
2002	249	71.7875	5139.1
2003	188	10.7875	114.2
2004	141	36.2125	1318.6
2005	197	19.7875	387.6
2006	180	2.7875	7.2
2007	96	81.2125	6611.7
2008	150	27.2125	746
2009	207	29.7875	881.3
2010	167	10.2125	106.3
$\sum x_i = 2837$		$\sum (x_i - \bar{x}) = 552.9$	$\sum (x_i - \bar{x})^2 = 27637.2$

$$\textcircled{1} \rightarrow \bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

$$\therefore \bar{x} = \frac{1}{n} \sum_{i=1}^{16} x_i$$

$$\bar{x} = \frac{1}{16} * (2837) = \boxed{177.2125 \text{ mm}}$$

$$\textcircled{2} \rightarrow U = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2$$

$$\therefore U = \frac{1}{16} (27637.2)$$

$$\therefore U = \boxed{1727.325}$$

$$\textcircled{3} \rightarrow S = \sqrt{U} = \boxed{41.57}$$

#

*** Ex 8 (weibull plotting position) ***

a) Annual rainfall at gauging station is recorded for year (1995-2010). Plot the distribution of the rainfall assuming that the (design storm is 210 mm), how frequent such rainfall storm will occur???

Year	Rainfall (mm) (X_i)	Rank (m)	Rainfall (mm) (design value)	$P(X \leq x) = \frac{m}{n+1}$
1995	212	1	96	0.059
1996	123	2	123	0.118
1997	156	3	134	0.176
1998	225	4	141	0.235
1999	134	5	150	0.294
2000	175	6	156	0.353
2001	237	7	167	0.412
2002	249	8	175	0.471
2003	188	9	180	0.529
2004	141	10	188	0.588
2005	197	11	197	0.647
2006	180	12	207	0.706
2007	96	13	212	0.765
2008	150	14	225	0.824
2009	207	15	237	0.882
2010	167	16	249	0.941

بترتيب تصاعدي (X_i) من الأصغر للأكبر

لح بعد ما أنزلنا هاد الجدول نرى العلاقة المتزايدة بين (X_i) وكل المعورد
النسبي والـ $(P(X \leq x))$ المعورد المتزايد ...

at (design storm $X_i = 210$ mm) graph $P(X \leq x) = 0.71$

$$\therefore P(X > x) = 1 - P(X \leq x) = 1 - 0.71 = 0.29$$

$$\therefore T = \frac{1}{P(X > x)} = \frac{1}{0.29} = 3.45 \approx 4 \text{ years} \quad \#$$

① estimate the design storm that being exceeded 10% or time ???

*** The exceedance probability $(P(x \geq x)) = 0.4$

$$P(x \geq x) = 1 - P(x \leq x)$$

$$0.4 = 1 - P(x \leq x)$$

$$P(x \leq x) = 1 - 0.4$$

$$P(x \leq x) = 0.6$$

→ Room graph at $P(x \leq x) = 0.6$
the value of $x_i = 190 \text{ mm}$ //

*** Ex 80 (intensity duration frequency) ***

② Plot the theoretical distribution for the following (15-minute extreme rainfall depths)

Year	15-min extreme rainfall depth (mm)	x_i (mm)	$(x_i - \bar{x})^2$
2000	12	7	45.1584
2001	17	8	32.72
2002	7	9	22.28
2003	14	11	7.3984
2007	27	12	2.9584
2005	9	13	0.5184
2006	13	14	0.0784
2007	18	15	1.6384
2008	8	17	10.76
2009	15	18	18.32
2010	11	27	176.35

$$\sum x_i = 151$$

$$\sum (x_i - \bar{x})^2 = 318.2$$

$$\bar{x} = \frac{151}{11} = 13.72$$

$$*** S = \sqrt{U} = \sqrt{\frac{1}{10} * 318.2} = 5.64$$

$$\therefore \alpha = \frac{\sqrt{6} * 5.64}{\pi} = (4.4) \rightarrow u = 13.72 - (0.5772 * 4.4)$$

$$\therefore u = 11.18$$

x_i	$P(X \leq x) = e^{-e^{-\left(\frac{x-u}{\alpha}\right)}} = e^{-e^{-\left(\frac{x-11.8}{-9.4}\right)}}$
7	0.08
8	0.13
9	0.14
11	0.35
12	0.44
13	0.52
14	0.59
15	0.66
17	0.77
18	0.81
27	0.97

ترجم العلاقة المقامة

بييت ال (X) ك شور

السيناريات وقمة ال

$P(X \leq x)$ ك شور الصاد است ...

⑥ what is the amount of extreme rainfall depth ($X_{15, \min}$, 10 years) that is associated to ($T_{\min}$) and return period of (10 years). (duration)

xxx The value of ($T=10$ years) ...

$$T = \frac{1}{P(X > x)} \Rightarrow P(X > x) = \frac{1}{T} = \frac{1}{10} = 0.1$$

$$\Rightarrow P(X > x) = 1 - P(X \leq x)$$

$$0.1 = 1 - P(X \leq x) \Rightarrow P(X \leq x) = 1 - 0.1$$

$$P(X \leq x) = 0.9$$

لعمرك الزمعة لما كانت قيمة ال $P(X \leq x)$ متساوية ال (0.9)

فأبت قيمة ال ($X = 22.5$)

لعمرك يمكن إيجاد قيمة ال (extreme rainfall depth)

ملاحظة: قانون مباشرة "دور ال اكاد ال ترتيبا

المعروف بـ العلاقة بين ال (X) وال $P(X \leq x)$ دور ال

.....

Q2 → To calc. The extreme rainfall depth at duration ($d = 15 \text{ min}$) and return period ($T = 10 \text{ year}$)...

$$* X_{(15,10)} = \bar{X}_d + K_T S_d$$

$$\Rightarrow K_T = \frac{-\sqrt{6}}{\pi} \left[0.5772 + \ln \left(\ln \left(\frac{T}{T-1} \right) \right) \right]$$

$$\therefore K_T = \frac{-\sqrt{6}}{\pi} \left[0.5772 + \ln \left(\ln \left(\frac{10}{10-1} \right) \right) \right]$$

$$\boxed{\therefore K_T = 1.3}$$

→ The value of $\bar{X}_{(15-\text{min})} = 13.72$

The value of $S_{(15-\text{min})} = 5.64$

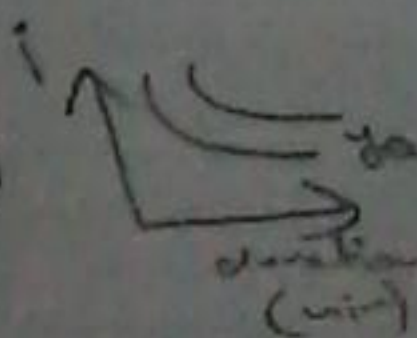
$$\therefore X_{(15,10)} = 13.72 + (1.3 \times 5.64)$$

$$\boxed{X_{(15,10)} = 21.052 \text{ mm}}$$

← قربة في إجابة فرغ (b) ...

→ To find the value of intensity Rainfall (i in mm/hr)

$$i = \frac{X_{d,T}}{d} = \frac{21.052}{\left(\frac{15 \text{ min}}{60} \right)} = \boxed{84.21 \text{ mm/hr}}$$

← أدنى أو بحدود 84 (أفروقة في القواسم) 

at ($d = 15 \text{ min}$) → ($T = 10 \text{ year}$)

→ The value of (i) from graph

$$\boxed{i = 84 \text{ mm/hr}}$$

*** Exo (To find the value of intensity) ***

Return Period (T)

Construct the (5-year) IDF curve for the following max. rainfall depth of (15-min) and (60-min) duration ...

Year	15-min. max rainfall	60-min. max rainfall
2000	24	45
2001	30	75
2002	20	34

① at (15-min. max rainfall) ...

$$X_{(15,5)} = \bar{X}_d + K_T S_d$$

$$X_{(15,5)} = \bar{X}_{15} + K_T S_{15}$$

$$\bar{X} = \frac{24+30+20}{3}$$

$$\therefore \bar{X} = 24.67$$

$$S = \sqrt{\frac{(24-24.67)^2 + (30-24.67)^2 + (20-24.67)^2}{2}} = 5.033$$

$$K_T = -\frac{\sqrt{6}}{T} \left[0.5772 + \ln \left(\ln \left(\frac{5}{5-1} \right) \right) \right] = 0.72$$

$$X_{(15,5)} = 24.67 + (0.72 * 5.033) = 28.3 \text{ mm}$$

$$\therefore \text{correct } (X_{15,5}) = 28.3 * (0.96) = 27.2 \text{ mm}$$

$$\therefore i = \frac{27.2}{\left(\frac{15}{60}\right)} = 108.8 \text{ mm/hr}$$

② at (60-min. max rainfall) ...

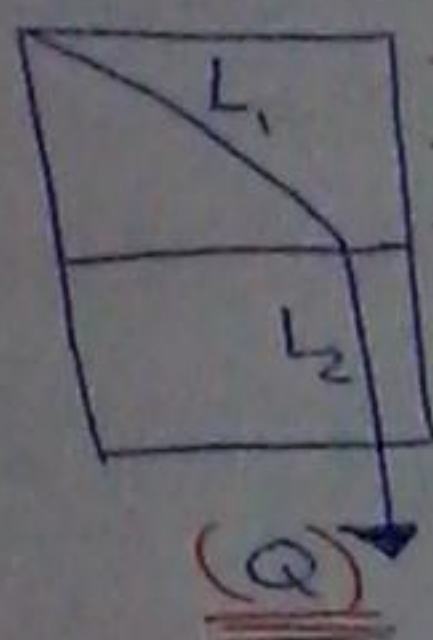
$$\bar{X} = \frac{(45+75+34)}{3} = 51.33 \text{ mm}$$

$$S = \sqrt{\frac{(45-51.33)^2 + (75-51.33)^2 + (34-51.33)^2}{2}} = 21.22$$

$$\therefore X_{(60,5)} = 51.33 + (0.72 * 21.22 * 0.96) = 64 \text{ mm} \rightarrow i = \frac{64}{\frac{60}{60}} = 64 \text{ mm/hr}$$

Ex 10 (To find the value of Peak Flow)

Q. For the watershed shown below, estimate the peak flow from a storm of (2-year) return period that lasts for (20 min)...



$*C_1 = 0.8$
 $*A_1 = 40000 \text{ m}^2$
 $*S_1 = 1\%$
 $*u_1 = 0.025$
 $*L_1 = 220 \text{ m}$

$*C_2 = 0.9$
 $*A_2 = 50000 \text{ m}^2$
 $*S_2 = 1.5\%$
 $*u_2 = 0.03$
 $*L_2 = 280 \text{ m}$

Q. Find the value of duration should be less than the duration (20 min)...

$$*t_{c1} = \frac{0.828 (L * u)^{0.467}}{S^{0.235}} = \frac{0.828 (220 * 0.025)^{0.467}}{\left(\frac{1}{100}\right)^{0.235}}$$

$$\therefore t_{c1} = 5.42 \text{ min}$$

$$*t_{c2} = \frac{0.828 ((280)(0.03))^{0.467}}{\left(\frac{1.5}{100}\right)^{0.235}} = 5.7 \text{ min}$$

$$t_c = (t_{c1} + t_{c2}) = (5.42 + 5.7) = 11.1 \text{ min} < 20 \text{ min}$$

$\therefore$ use the value of duration = 11.1 min

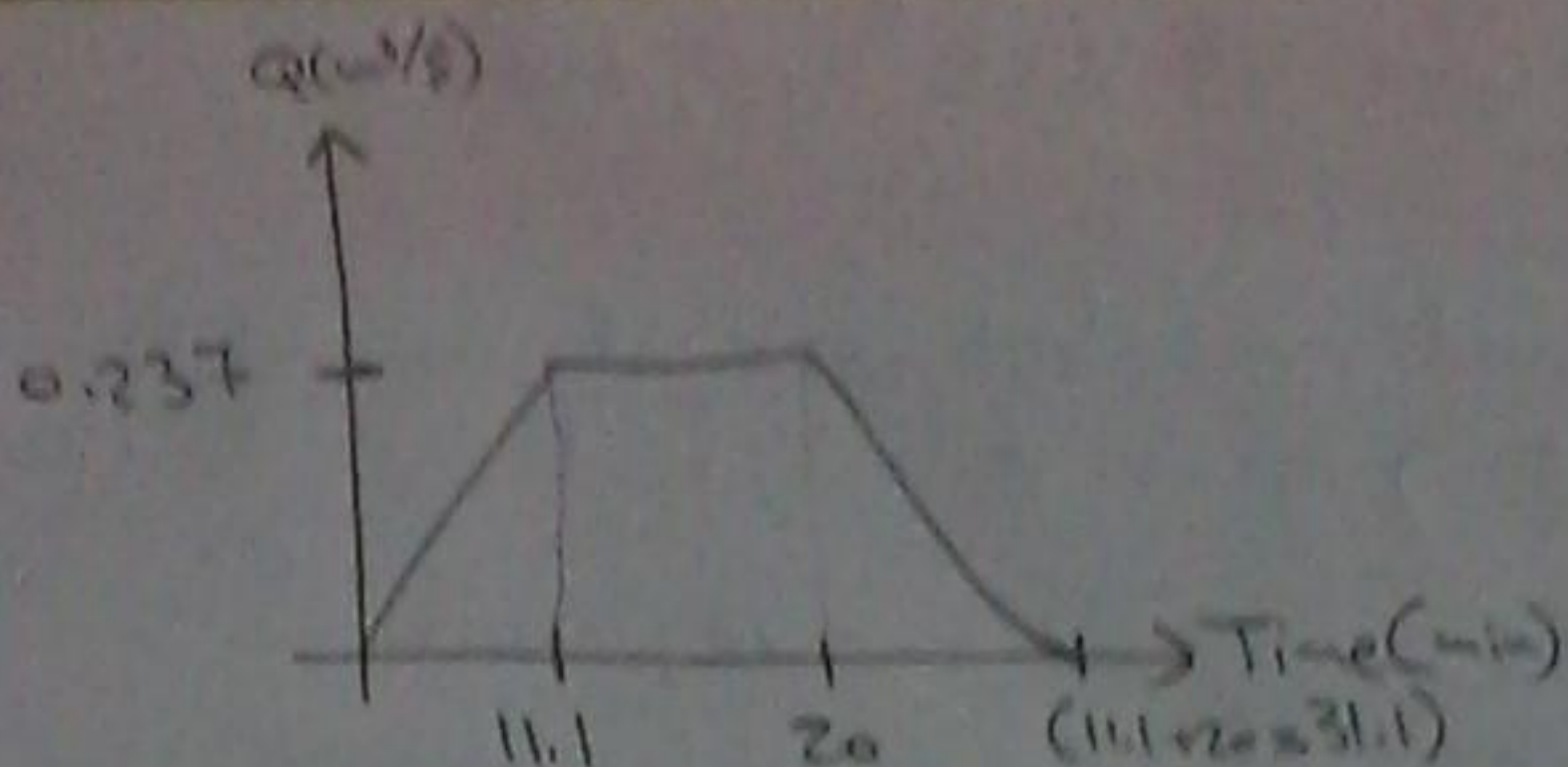
at $d = 11.1 \text{ min}$ and $T = 2 \text{ year}$
from graph $(i(\text{mm/hr}) = 11 \text{ mm/hr})$

$$\text{The value of } C_{\text{avg}} = \frac{C_1 A_1 + C_2 A_2}{\Sigma A} = \frac{(0.8 * 40,000) + (0.9 * 50,000)}{(40,000 + 50,000)}$$

$$\therefore C_{\text{avg}} = 0.86$$

$$\therefore Q = 0.278 * 0.86 * 11 * (40,000 + 50,000) * 10^{-6} \Rightarrow$$

$$\therefore Q = 0.237 \text{ m}^3/\text{s}$$



⑥ estimate the max. potential water volume that can be harvested from the storm given...

- Volume (m^3) = $Q \times \text{time}$ = area under the curve

$$\begin{aligned} \text{Volume } (m^3) = & \left(\frac{1}{2} \times 11.1 \times 0.237 \right) + \\ & \left(\frac{1}{2} \times (31.1 - 20) \times 0.237 \right) + \\ & ((20 - 11.1) \times 0.237) \end{aligned}$$

$$\therefore U (m^3) = 4.74 \times \frac{60}{1} \rightarrow \text{from (min} \rightarrow \text{sec)}$$

$$\therefore U (m^3) = 284.4 \text{ } m^3$$

$\begin{matrix} a & t(\text{sec}) \\ (0.237 \times 20 \times 60) \end{matrix}$

#

usually flat watershed would have drainage density that is low

watershed of high slope value would result in bifurcation ratio that is high

Elongated watershed usually discharge peak flow that appears after

short time

when two stream of order (3) and (4) are joined, the resultant stream has the order

7

In the rational method, the (C) coefficient represents net flow

watershed with little storage capacity discharge peak flow that appears early

The watershed stream ordering is used to classify watershed

Considered two watershed (A and B). The drainage density of watershed A = 2.5, having stream length ratio for watershed A (R_L) as 2.2. if watershed B has area of 26 km² having total streams length as 59 km. Estimate the length of length of streams of order (3) in watershed (B) when the (length of streams of order (1) is 8 km)

Solution

A	B
$D = 2.5$	$A_B = 26 \text{ km}^2$
$R_L = 2.2$	$\sum L = 59 \text{ km}$
$L_1 = 8 \text{ km}$	order = <u>3</u>
$L_3 = ???$	

$\Rightarrow D_A = 2.5$

$\Rightarrow D_B = \frac{\sum L}{A} = \frac{59 \text{ km}}{26 \text{ km}^2} = 2.26$

$\Rightarrow (D_A \approx D_B)$ (same characteristic)

$\Rightarrow L_3 = L_1 (R_L)^{3-1}$
 $L_3 = (8)(2.2)^{3-1}$

$L_3 = 38.72 \text{ km}$ #

② Small water shed area = 0.5 km^2 , runoff coefficient = $C = 0.8$... discharge flow of $(2.224 \text{ m}^3/\text{s})$ at 2-years return period, calc. the flow rate when the return period is (10-year) assume the rational is applied.

*** Solution ***

$$Q = 2.224 \text{ m}^3/\text{s}$$

$$Q = 0.278 \times C_{\text{total}} \times i \times A_{\text{total}}$$

$$2.224 = 0.278 \times 0.8 \times i \times 0.5$$

$$\therefore i = 20 \rightarrow \text{at } (T = 2\text{-year})$$

$$\therefore Q = 0.278 \times 0.8 \times i \times 0.5$$

$$Q = 0.278 \times 0.8 \times 60 \times 0.5$$

$$Q = 6.672 \text{ m}^3/\text{s} \quad \#$$

$$2\text{ year} \rightarrow 20$$

$$10\text{ year} \rightarrow ???$$

$$\frac{10 \times 20}{2} = 100$$

$$100 - (2 \times 2) =$$

$$100 - 4 =$$

$$96$$

$$i = ?$$

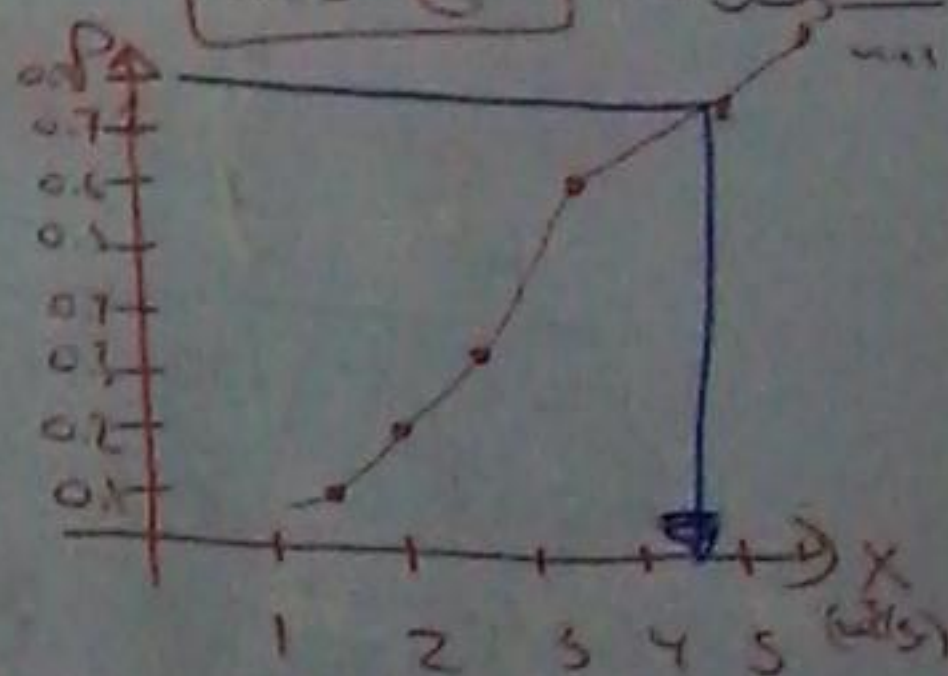
③ according to flow value listed below, a culvert has been designed such that a failure occurs on average once in (5 year). Estimate the value of the design flow? Estimate the frequency of a flow that is a half of the design flow.

Flow (m^3/s)

* 2.5	Rank	X	P(X ≤ x)
* 3.5	1	1.5	0.111
* 7.0	2	2	0.222
* 1.5	3	2.5	0.333
* 2.0	4	3.5	0.444
* 3.5	5	3.5	0.555
* 5	6	3.5	0.666
* 3.5	7	5	0.777
	8	7	0.888

* The value of

$$u = 8$$



The value

$$\text{of } X = 4.5$$

$$= 0.555 \text{ m}^3/\text{s}$$

$$T = \frac{1}{P(X > x)} \rightarrow P(X > x) = \frac{1}{T} = \frac{1}{5} = 0.2$$

$$P(X \leq x) = 1 - P(X > x) = 1 - 0.2 = 0.8$$

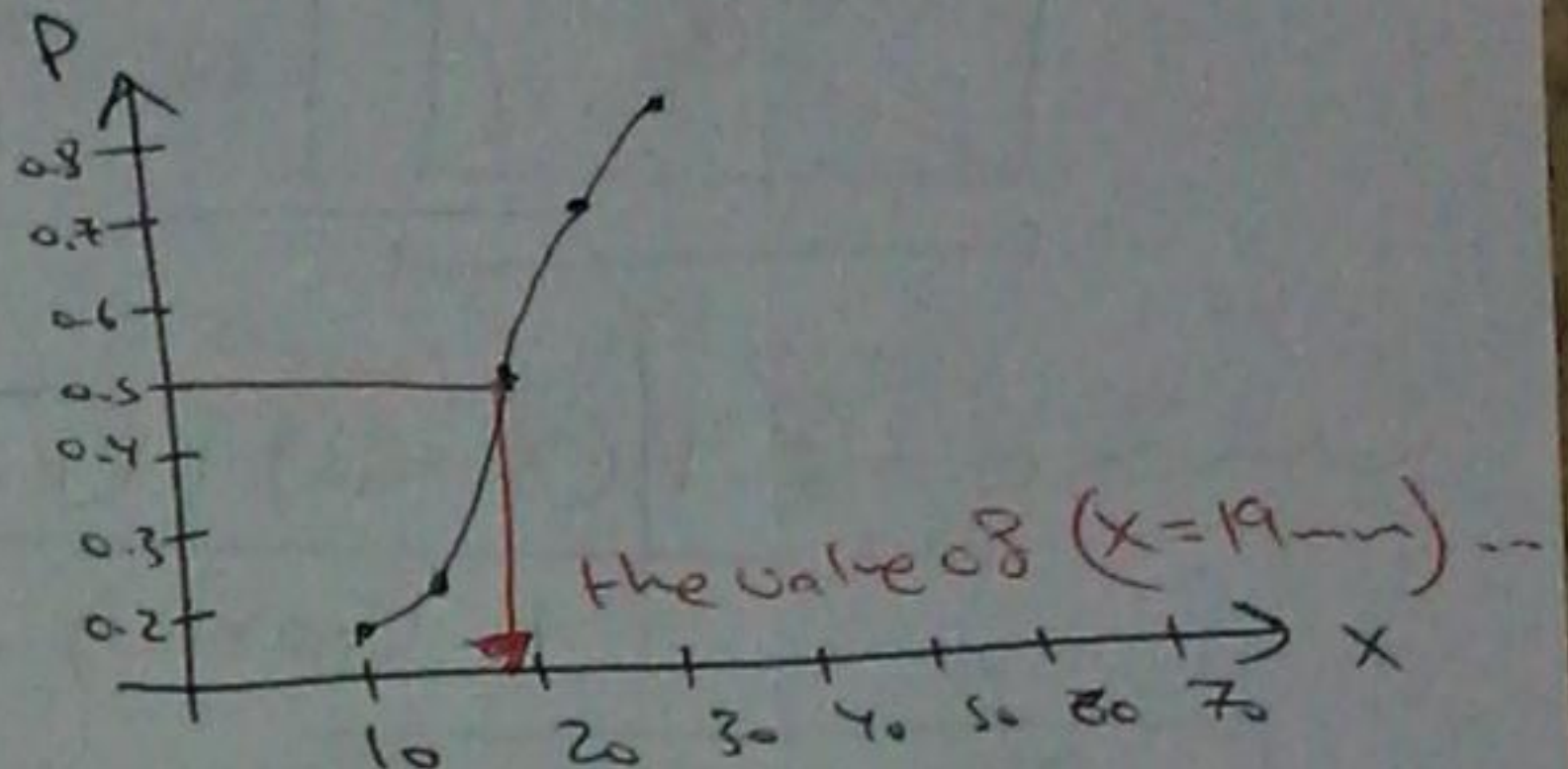
total rainfall depth (mm) over a watershed are as follows (30, 20, 15, 25, 20, 10) and ^① what is the mean rainfall depth that is associated to return period of (2 year)
^② what rainfall intensity that, being exceeded 70% of the time???

Solution

rank	x	P(X ≤ x)
1	10	0.1428
2	15	0.2857
3	20	—
4	20	0.5714
5	25	0.7143
6	30	0.8571

the value of $u = 6$

$$P(X \leq x) = \frac{u}{u+1}$$



$$\textcircled{1} \rightarrow T = \frac{1}{P(X > x)} \rightarrow P(X > x) = \frac{1}{T} = \frac{1}{2} = \textcircled{0.5}$$

$$P(X \leq x) = 1 - 0.5 = \textcircled{0.5}$$

$$\textcircled{2} \rightarrow P(X > x) = 0.7 \rightarrow \therefore T = \frac{1}{0.7} = \boxed{1.43 \text{ year}}$$

$$\therefore K = \frac{-\sqrt{6}}{\pi} \left(0.5772 + \ln \left(\ln \left(\frac{1.43}{1.43+1} \right) \right) \right)$$

$$\therefore K = -0.594$$

$$\rightarrow X_{d,T} = \bar{X}_{d1} + K_T \cdot \sigma_{d1} \rightarrow T = 2 \text{ year } i = \frac{X_{d,T}}{d}$$

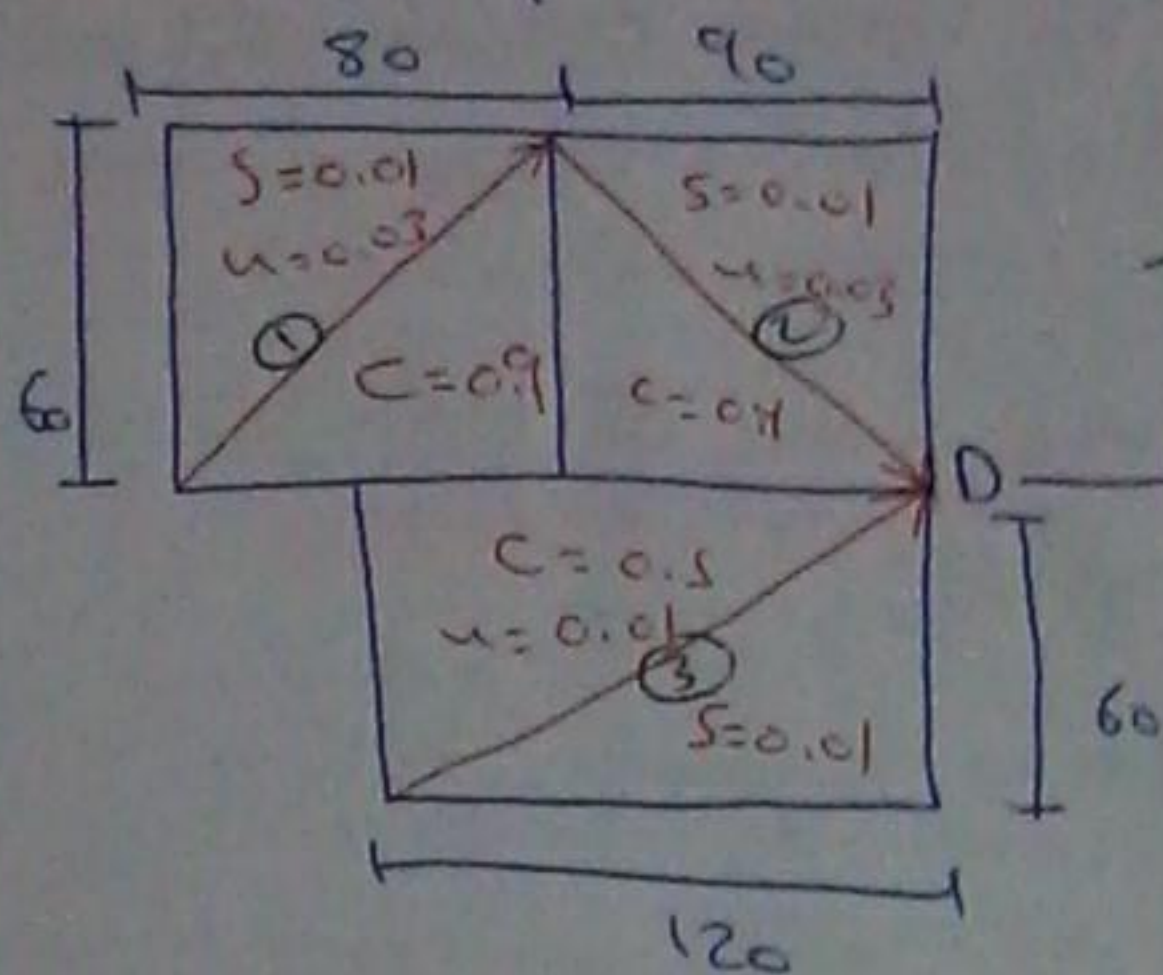
$$\textcircled{20} = \frac{10+15+20+25+30}{5}$$

$$\textcircled{7.905}$$

$$\therefore X_{d,T} = 15.3$$

$$\therefore i = \frac{15.3}{2} \rightarrow (\text{mm/hr}) \neq$$

using return period = 10 year...
Calc. Peak flow at the point (D)???



Solution 50

$$Q = 0.278 \times C \times I \times A_{\text{Total}}$$

$$A_{\text{Total}} = (80 \times 60) + (90 \times 60) + (120 \times 60)$$

$$\therefore A_{\text{Total}} = 17400 \text{ m}^2$$

$$C_{\text{Total}} = \frac{(0.9)(80 \times 60) + (0.7)(90 \times 60) + (0.5)(120 \times 60)}{(80 \times 60) + (90 \times 60) + (120 \times 60)}$$

$$\therefore C_{\text{Total}} = 0.579$$

$$t_c = \frac{0.828 \times (L \times u)^{0.464}}{S^{0.235}} \rightarrow \sqrt{(x)^2 + (y)^2}$$

$$\therefore t_{c1} = 36.86 \text{ min}$$

$$\therefore t_{c2} = 12.607 \text{ min}$$

$$\therefore t_{c3} = 13.536 \text{ min}$$

check
in

$$t_{cT} = 36.86 + 12.607 = 49.5$$

from curve the value of

$$i = 20$$

$$\therefore Q = 0.278(0.579)(20)(0.0174)$$

$$= 0.056 \text{ m}^3/\text{s}$$

$$\frac{0.162}{\text{m}^3/\text{s}}$$

#

$$P(x) = 1 - P(y) = 1 - 0.01 = 0.99$$

duration = 30 min

acceptance Probability = 10% $\rightarrow$ 26.5

acceptance probability = 5% $\rightarrow$ 29.35

acceptance probability = 50% $\rightarrow$???

*** Solution ***

$$*K_{T_1} = \frac{\sqrt{6}}{\pi} \left(0.5772 + \ln \left(\ln \left(\frac{10}{10-1} \right) \right) \right) = \boxed{1.305} \#$$

$$\rightarrow T = \frac{1}{0.1} = 10 \text{ year}$$

$$*K_{T_2} = \frac{\sqrt{6}}{\pi} \left(0.5772 + \ln \left(\ln \left(\frac{20}{20-1} \right) \right) \right) = \boxed{1.867} \#$$

$$\rightarrow T = \frac{1}{0.05} = 20 \text{ y}$$

$$*K_{T_3} = \frac{\sqrt{6}}{\pi} \left(0.5772 + \ln \left(\ln \left(\frac{2}{2-1} \right) \right) \right) = \boxed{-0.164} \#$$

$$\rightarrow T = \frac{1}{0.5} = 2 \text{ year}$$

$$*** X_{30,10} = \bar{X} + K_1 S_{30}$$
$$X_{30,20} = \bar{X} + K_2 S_{30}$$

$$26.5 = \bar{X} + 1.305 S_{30}$$

$$29.35 = \bar{X} + 1.867 S_{30} \ominus$$

$$\therefore S_{30} = 5.33$$

$$\text{بقريب} \rightarrow \bar{X} = 19.57$$

$$\therefore X_{30,2} = \bar{X} + K_3 S_{30}$$

$$X_{30,2} = 19.57 + (-0.164 \times 5.33)$$

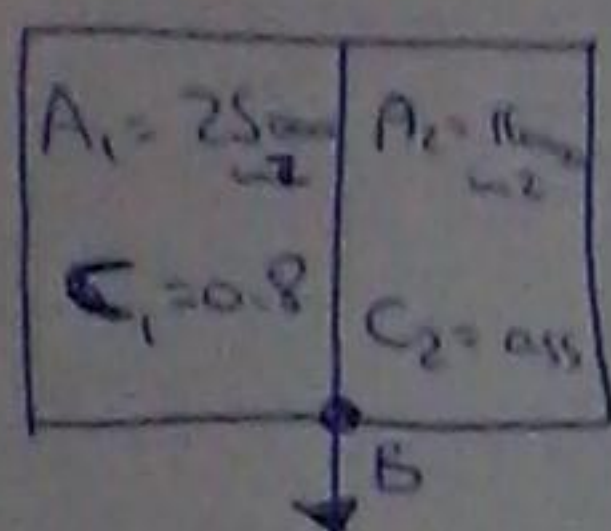
$$\therefore X_{30,2} = 18.66$$

$$\rightarrow \therefore i = \frac{18.66}{\frac{30}{60}} = \boxed{37.32} \#$$

max(DoR(V))

- *** The intercepted 2m precipitation depth nearly the soil moisture. (F)
 - *** The SCS method is used to estimate the excess rain from large watershed of steep slopes. (F)
 - *** The 2-hr UH represent the watershed response to 2-hr rainfall of 2cm depth excess rainfall. (F)
 - *** watershed of high storage capacity are characterized by large base long time. (T)
 - *** Equal watershed produce runoff hydro-graph that is flat with low peak flow. (T)
 - *** The peak flow estimated using the unit hydrograph is usually less accurate than estimate using the UH method. (T)
 - *** in elongated watershed the peak flow occurs at time shorter than the time of concentration. (F)
 - *** The ground water max. is 0.7 times of the peak only the property of the aquifer. (F)
-

The watershed shown consists of area A_1 and A_2 is the 2-year recurrent peak flow for $A_1 = 0.85 \text{ m}^3/\text{s}$ and $A_2 = 0.7 \text{ m}^3/\text{s}$



① Estimate the 2-year recurrent peak flow from the whole watershed that will be along at Point (B)???

*** Solution ***

$$\rightarrow C_{avg} = \frac{250000(0.8) + 160000(0.55)}{250000 + 160000} = \boxed{0.695}$$

$$Area = 250000 + 160000 = 410000 = \boxed{0.41 \text{ km}^2}$$

$$Q = 0.278 C_i A \rightarrow i = ???$$

$$Q_1 = 0.278 C_1 A_1 i_1 \rightarrow 0.85 = 0.278(0.8)(0.25)i_1$$

$$\boxed{i_1 = 15.278} \quad \checkmark$$

$$Q_2 = 0.278 C_2 A_2 i_2 \rightarrow 0.70 = 0.278(0.55)(0.16)i_2$$

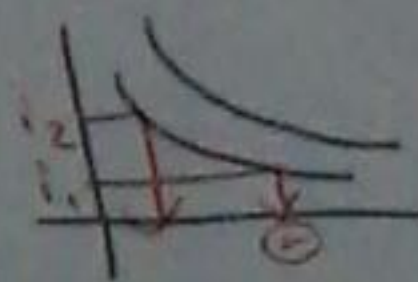
$$\boxed{i_2 = 22.48}$$

$\rightarrow i_1 \rightarrow$ storm curve $\rightarrow$ Give long time of concentration.

Assuming $\therefore Q = 0.278 * C_{avg} * A * i$

$$Q = 0.278 * 0.695 * 0.41 * 15.278$$

$$\boxed{Q = 1.211 \text{ m}^3/\text{s}}$$



② is the whole watershed (2 hr) duration calc. peak flow for (10 year) at point B???

*** Solution *** storm graph (2 hr $\rightarrow$ 120 min)
at 120 min $\rightarrow i = 14$

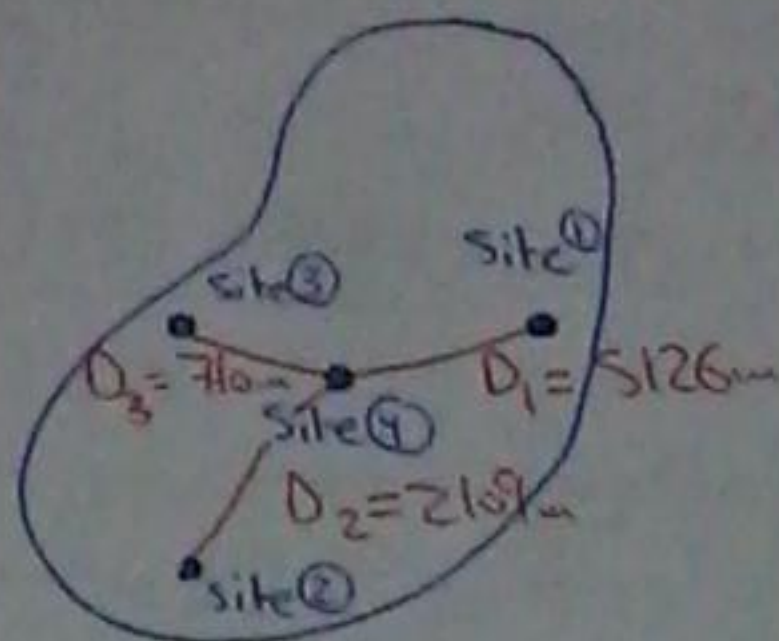
$$\therefore Q = 0.278(0.695)(14)(0.41) = \boxed{1.145 \text{ m}^3/\text{s}}$$

* second exam *

Exo (un-gauged site precipitation) ***

estimate the rainfall at the un-gauged site #4, based on the rainfall at the following gauged sites...

Site	rainfall (mm)
1	14
2	21
3	11



$$P_{\text{un-gauged}} = \frac{\sum P * w}{\sum w}$$

$$w = \frac{1}{D^2} \Rightarrow w_1 = \frac{1}{D_1^2} = \frac{1}{(5126)^2} = 3.8 * 10^{-8} * 10^6 \rightarrow D(Km)$$

$$w_2 = \frac{1}{D_2^2} = \frac{1}{(2109)^2} = 2.24 * 10^{-7} * 10^6$$

$$w_3 = \frac{1}{D_3^2} = \frac{1}{(710)^2} = 1.98 * 10^{-6} * 10^6$$

$$\sum w = 2.245 * 10^{-6} * 10^6$$

$$\therefore \sum w = 2.245$$

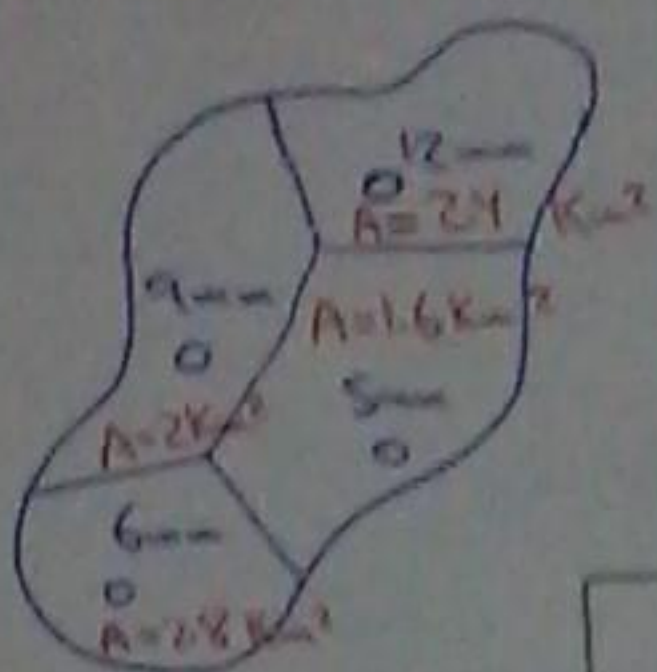
$$\therefore P_{\text{un-gauged}} = \frac{(3.8 * 10^{-8} * 10^6 * 14) + (2.24 * 10^{-7} * 10^6 * 21) + (1.98 * 10^{-6} * 10^6 * 11)}{2.245}$$

$$\therefore P_{\text{un-gauged}} = 12.033$$

#

Exo (areal precipitation)

Estimate the areal rainfall for the following watershed.



$$\bar{P} = \frac{\sum PA}{\sum A}$$

$$\frac{(12 \times 24) + (5 \times 1.6) + (6 \times 28) + (9 \times 2)}{(24 + 1.6 + 28 + 2)}$$

$$\therefore \bar{P} = 8.14 \text{ mm}$$

#

Exo (The evaporation rate)

Calculate the evaporation rate under net solar radiation of 200 W/m^2 and air temperature of 25°C . Assume completely wet soil ($K_s = 1$) and in arid region ($K_c = 1$).

$$*E_r = \frac{R_n}{l_v * \rho} * K_g * K_c \quad \rightarrow l_v = 2500 - 2.36T$$

$$l_v = 2500 - (2.36 * 25)$$

$$l_v = 2441 \text{ (KJ/Kg)}$$

$$\therefore E_r = \frac{200}{(2441 * 10^3 * 1000)} * 1 * 1 = 8.22 * 10^{-8} \text{ m/s}$$

$$\therefore E_r = 8.22 * 10^{-8} * 24 * 60 * 60 * 10^3 = 7.1 \text{ (mm/day)}$$

$$\therefore E_r = 8.22 * 10^{-8} * 60 * 60 * 10^3 = 0.295 \text{ (mm/hr)}$$

#

Ex (infiltration rate and depression storage) ans

→ a (2-hr) rainfall storm with pattern as shown below. Given the soil equilibrium infiltration capacity of (0.75 mm/hr), an initial infiltration of (5 mm/hr), and the infiltration constant is (0.29) (what is the net rain available for runoff) assuming that depression storage is for the first hour with total storage capacity of (2 mm/hr) assume completely wet soil in ariel region under air temperature of (10°C) and solar radiation of (150 W/m²) neglect interception losses.

hour	Total rainfall intensity P_{Total} (mm/hr)
1	10.3
2	12.5

$$\Rightarrow f_c = 0.75 \text{ mm/hr}$$

$$\Rightarrow f_0 = 5 \text{ mm/hr}$$

$$\Rightarrow K = 0.29$$

$$\Rightarrow P_u = ???$$

$$\Rightarrow S_c = 2 \text{ mm/hr} \text{ (at first hour)}$$

$$\Rightarrow T = 10^\circ\text{C}$$

$$\Rightarrow R_u = 150 \text{ W/m}^2$$

$$\text{at (2-hr)} \Rightarrow f = 0.75 + (5 - 0.75)e^{-(0.29 \times 2)}$$

$$\boxed{f = 3.13 \text{ mm/hr}}$$

$$\Rightarrow E_n = 0.22 \text{ mm/hr}$$

$$\Rightarrow P_u = 12.5 - 0.22 - 3.13$$

$$\boxed{P_u = 9.15 \text{ mm/hr}}$$

$$\Rightarrow D_s = 0 \text{ mm/hr}$$

$$\Rightarrow \text{Net} = 9.15 \text{ mm/hr} \quad \#$$

$$\left(\begin{array}{l} \text{at} \\ \text{1 hr} \end{array} \right) \Rightarrow f = f_c + (f_0 - f_c)e^{-Kt}$$

$$f = 0.75 + (5 - 0.75)e^{-(0.29 \times 1)}$$

$$\boxed{f = 3.93 \text{ mm/hr}}$$

$$\Rightarrow E_n = \frac{150}{2476.4 \times 10^3 \times 10^3} \times 1 \times 1$$

$$I_0 = 2800 - (2.36 \times I_0)$$

$$\boxed{I_0 = 2476.4}$$

$$\therefore E_n = 0.22 \text{ mm/hr}$$

$$\therefore P_u = 10.3 - 0.22 - 3.93$$

$$\boxed{P_u = 6.15 \text{ mm/hr}}$$

$$\therefore D_s = S_c (1 - e^{-P_u/S_c})$$

$$D_s = 2 (1 - e^{-6.15/2})$$

$$\boxed{D_s = 1.9 \text{ mm/hr}}$$

$$\Rightarrow \text{Net} = 6.15 - 1.9$$

$$\boxed{\text{Net} = 4.25 \text{ mm/hr}} \quad \#$$

Ex 8 (Hydrology Numericals) (The effects of irrigation)

→ determine the excess water the (3 inches) total water in soil clay loam intercalated at (18 Kwt) under dry soil condition along the (18 Kwt) (1 Kwt) is range level, while the rest is cultivated land.

→ Given → The value of $CN(7 Kwt) = 71$

The value of $CN(11 Kwt) = 98$

$$\therefore CN_{avg} = \frac{(CN_1 \times A_1) + (CN_2 \times A_2)}{\sum A} = \frac{(71 \times 7) + (98 \times 11)}{(7 + 11)}$$

$$\therefore CN_{avg} = 82.5 \rightarrow CN(II)$$

$$\rightarrow CN(I) = \frac{4.2 \times 82.5}{10 - (6.058 \times 82.5)} = \boxed{66.5}$$

$$\rightarrow CN(III) = \frac{23 \times 82.5}{10 + 0.13(82.5)} = \boxed{91.55}$$

$$\rightarrow \therefore d = \frac{1000}{66.5} - 10 = \boxed{5.03 \text{ inches}}$$

$$\rightarrow \therefore P_e = \frac{(P - 0.2d)^2}{(P + 0.8d)} = \frac{(3 - 0.2 \times 5.03)^2}{(3 + 0.8 \times 5.03)} = \boxed{0.56 \text{ inch}} \neq$$

$$\rightarrow \therefore d = \frac{1000}{91.55} - 10 = \boxed{0.92 \text{ inches}}$$

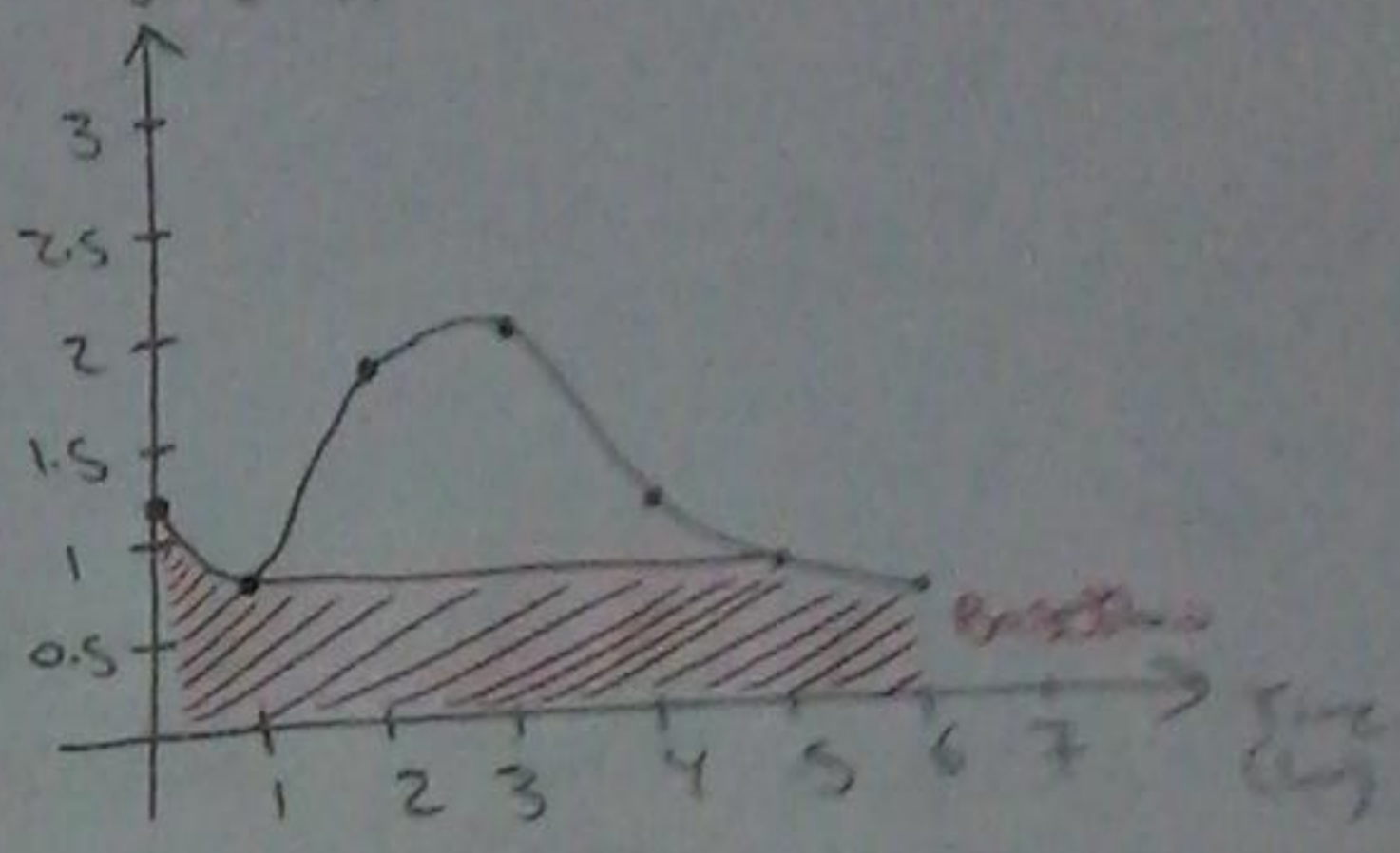
$$\rightarrow \therefore P_e = \frac{(3 - 0.2 \times 0.92)^2}{(3 + 0.8 \times 0.92)} = \boxed{2.12 \text{ inches}} \neq$$

Exo (hydrograph)

During a large watershed discharge runoff to its outlet the measured total runoff is shown in the table below. estimate the direct runoff (surface runoff)???

(P)

Time(hr)	Total Runoff (m ³ /s)	Base (m ³ /s)
0	1.2	
1	0.86	
2	1.57	
3	1.92	
4	1.21	
5	0.94	
6	0.77	



*** Sol ***

* دالة قمية ال
(Total Runoff)
كيب ان كويل
لقيمة ال
(direct runoff)
وذلك من طريق طرح
قيمة ال (Baseflow)
من قمية ال
الاعلا قمية بيا ال
(Time - Total Runoff)

Time	Total Runoff	Baseflow	direct runoff
0	1.2	1.2	0
1	0.86	0.86	0
2	1.57	0.86	0.71
3	1.92	0.86	1.06
4	1.21	0.86	0.35
5	0.94	0.86	0.08
6	0.77	0.77	0

* Direct Runoff = Total Runoff - Baseflow

④

$\begin{matrix} 20 & \textcircled{1} \\ 15 & \textcircled{2} \end{matrix} \rightarrow M$

ملاحظة (P) لا تسمى (excess value) ملاحظة ال (Q) فلازم
تسمى (direct value) إذا كانت (Total value) فلازم أن نخرج
منها ملاحظة (Base value) عن طريق (direct value)

$$* Q_n = P_1 U_n + P_2 U_{n-1} + P_3 U_{n-2} + \dots$$

$$\text{at } (u=1) \rightarrow Q_1 = P_1 U_1$$

$$z_3 = 200,$$

لازم ہو گا
④ قاعدہ ⑤
(4, 4, 4, 4, 4)

$$12.1 = 20(v_2) + 15(1.15)$$

$$\therefore V_2 = 5.19 \text{ cm}$$

$$26.7 = (2)(0.3) + (1.5)(5.19) + 0$$

$$\text{at } (u=4) \rightarrow Q_4 = P_1 U_4 + P_2 U_3 + 0$$

$$U_4 = 1.51 \text{ cm}$$

Shown below...

(*) إدار العلاقة بيناد (9)

⑦ 515

excess rainfall (mm) measured (P)

1	8
2	10
3	5

*** Time	excess rainfall	direct runoff	v (cm)
1	20	2.3	1.15
2	15	12.1	5.19
3	0	26.7	9.46
4	0	17.2	1.51
5	0	2.3	0

لے بیٹھیں وہاں ان کو لے کر ایک جگہ پر (۵) فتح اور (۶) فقط ایجاد مہمہ اور
(۷) ایک مہمہ ...

$$\therefore M=3 \Rightarrow N=5 \Rightarrow u=5-3+1$$

$u=3$

at $(u=1) \Rightarrow Q_1 = P_1 V_1 \Rightarrow Q_1 = 0.8 \times 1.15 = \boxed{0.92 \text{ m}^3/\text{s}}$

$$\text{at } (u=2) \rightarrow Q_2 = P_1 V_2 + P_2 V_1 \rightarrow Q_2 = (0.8)(5.19) + (1)(1.15) = \boxed{5.3 \text{ m}^3/\text{s}}$$

at $(u=3) \rightarrow Q_3 = P_1 Q_3 + P_2 Q_2 + P_3 Q_1 = (0.8)(9.46) + (1)(5.19) + (0.5)(1.15)$
 $\therefore Q_3 = 13.33 \text{ m}^3/\text{s}$

$$\text{at } (u=4) \rightarrow Q_4 = P_1 U_4 + P_2 U_3 + P_3 U_2$$

$$Q_1 = (0.8)(1.51) + (1)(9.46) + (0.5)(5.19) = \boxed{13.26 \text{ m/s}}$$

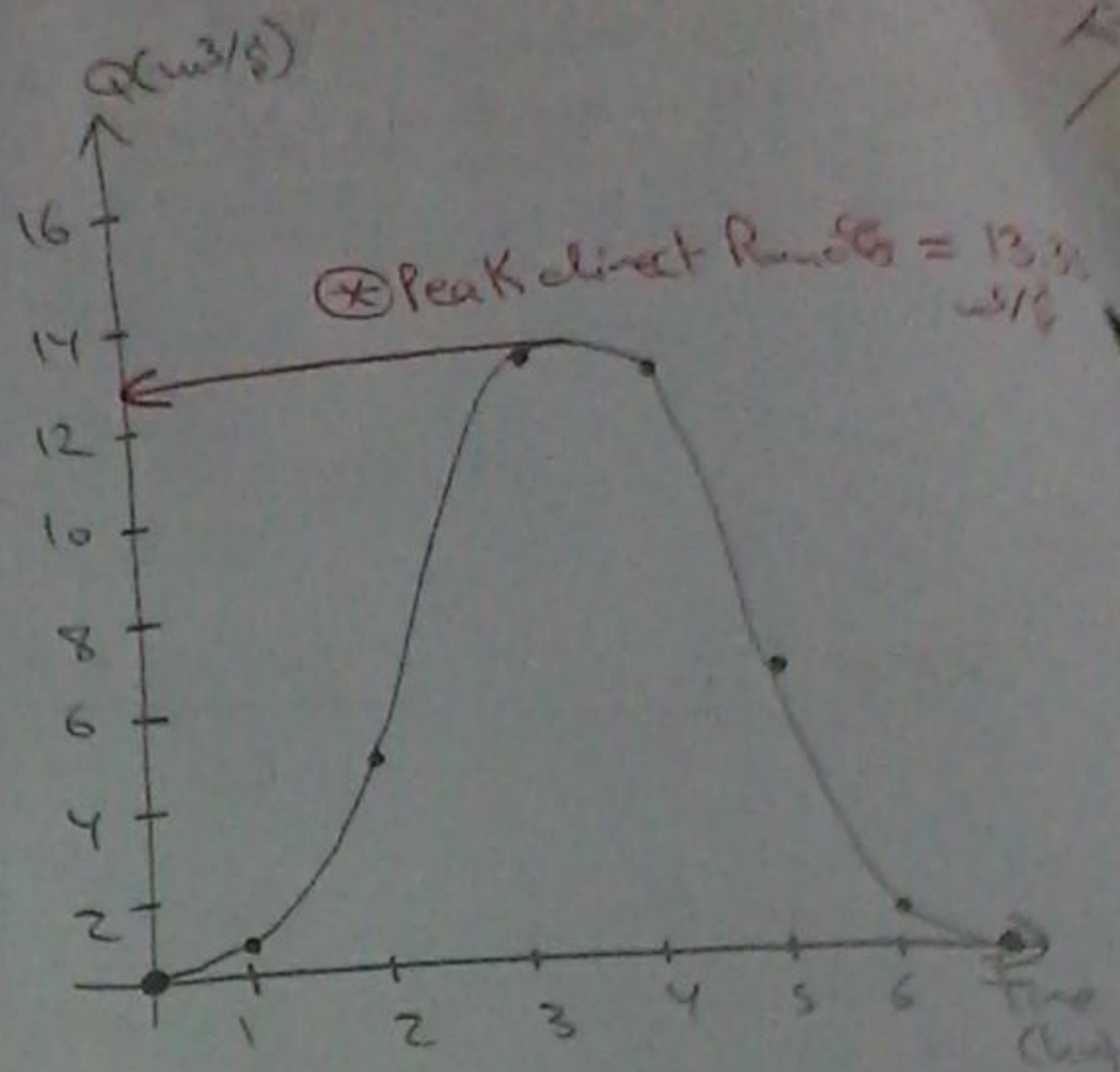
$$\text{at } (u=5) \rightarrow Q_5 = P_1 U_5 + P_2 U_4 + P_3 U_3 = (1)(1.51) + (0.5)(9.46) = \underline{6.24 \text{ W}}$$

$$\text{at } (u=6) \rightarrow Q_6 = P_1 U_6 + P_2 U_5 + P_3 U_4 = (0.5)(1.51) = \boxed{0.755 \text{ m}^3/\text{s}}$$

$$\text{at } (u=7) \rightarrow Q_1 = P_1 U_1 + P_2 U_8 + P_3 U_5 = \textcircled{0}$$

at $(u=0) \rightarrow Q=0$

Time (hr)	Q (m ³ /s)
0	0
1	0.92
2	5.30
3	13.33
4	13.26
5	6.24
6	0.76
7	0



Ex 80 (Singh's 11)

Develop a (2-hr) unit hydrograph for the watershed shown. The basin area is (280 km²), and the distance along the main stream to the basin centroid nearest point is (20 km). Use C_f of (1.5), and C_p of (0.8) as of the nearest gauged basin. main stream = 35 km...

$$*** T_L = C_f (L + L_c)^{0.3} = (1.5)(20 + 35)^{0.3} = \boxed{10.7 \text{ hr}}$$

$$*** D = \frac{T_L}{S.S} = \frac{10.7}{5.5} = \boxed{1.95 \text{ hr}}$$

$$*** T'_L = T_L + 0.25(D' - D) = 10.7 + 0.25(2 - 1.95) = \boxed{10.72 \text{ hr}}$$

$$*** T_b = 3 + \frac{T'_L}{8} = 3 + \frac{10.72}{8} = 4.34 \text{ day} \times 24 = \boxed{104 \text{ hr}} \checkmark$$

$$*** T_b = 4 T_L = 4 \times 10.7 = 42.8 \dots \text{ (for small basins)}$$

$$*** Q_p = \frac{2.78 C_p A}{T'_L} = \frac{2.78 \times 0.8 \times 280}{10.72} = \boxed{58.1 \text{ m}^3/\text{s/cm}}$$

$$*** T_p = \frac{D'}{2} + T'_L = \frac{2}{2} + 10.72 = 10.72 + 1 = \boxed{11.72 \text{ hrs}}$$

$$*** \omega_{50} = 5.87 \left(\frac{Q_p}{A} \right)^{-1.08} = 5.87 \left(\frac{58.1}{280} \right)^{-1.08} = \boxed{32.1 \text{ hr}} \#$$

$$*** \omega_{75} = \frac{\omega_{50}}{1.75} = \frac{32.1}{1.75} = \boxed{18.3 \text{ hr}} \#$$

Time(hr)	Runoff ($m^3/s/a$)
0	0
$T_p - \frac{1}{3} \omega_{50}$	$\frac{1}{2} Q_p$
$T_p - \frac{1}{3} \omega_{75}$	$0.75 Q_p$
T_p	Q_p
$T_p + \frac{2}{3} \omega_{75}$	$0.75 Q_p$
$T_p + \frac{2}{3} \omega_{50}$	$0.5 Q_p$
T_b	0

Time(hr)	Runoff ($m^3/s/a$)
0	0
1.02	29.05
5.62	43.57
11.72	58.1
23.92	43.57
33.12	29.05
104.02	0

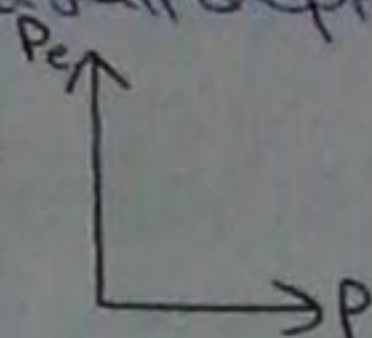
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ال (Time-Q)

Question (1)

answer the following using the abbreviation of (CBD) ^{in can not be determined}
 2. ① Given total rainfall of (5") at watershed of (CN=70) would retain rainfall depth (will not flow) as _____

*Solve from graph



at $P = 5$ inches and $CN = 70$ the value of $P_e = 2$ inches

$$\therefore S = \frac{1000}{CN} - 10$$

$$\therefore S = \frac{1000}{70} - 10$$

$$\rightarrow S = 4.3$$

The value of $P_e = \frac{(P - 0.2S)^2}{(P + 0.8S)}$

$$2 = \frac{(P - (0.2 \times 4.3))^2}{(P + (0.8 \times 4.3))}$$

$$\therefore P = 4.95 \approx \underline{\underline{5}}$$

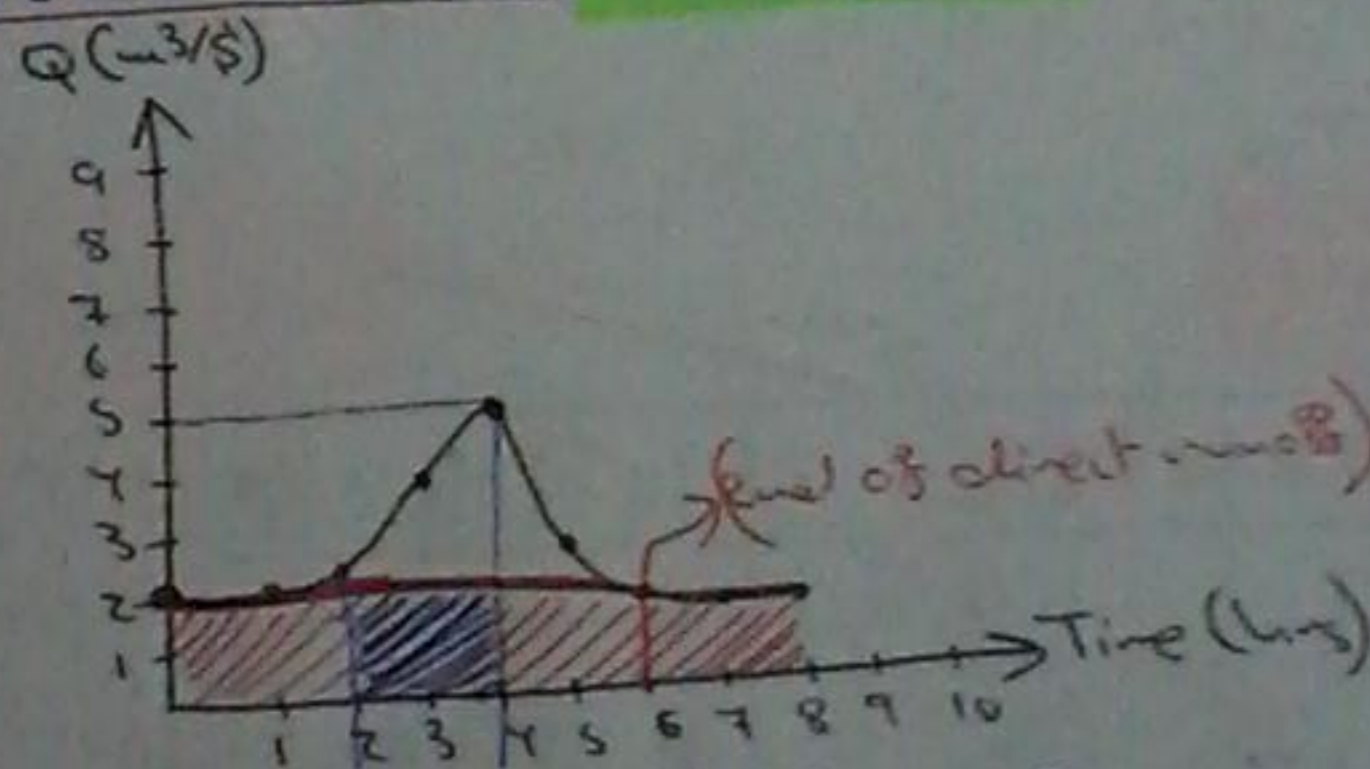
$$CN(I) = \frac{(4.2)(70)}{10 - (0.058(70))}$$

$$\therefore CN(I) = 49.49$$

$$CN(III) = \frac{23(70)}{10 + (0.13(70))}$$

$$CN(III) = 84.29$$

② From the hydrograph shown, the direct runoff due to the excess rainfall ends at the time (6) ...



③ From the hydrograph shown, the base flow is nearly (2) ...

④ From the hydrograph shown, the rainfall duration is can be determined ...

⑤ From the hydrograph shown, the watershed time of concentration is nearly 4-2=2 ...

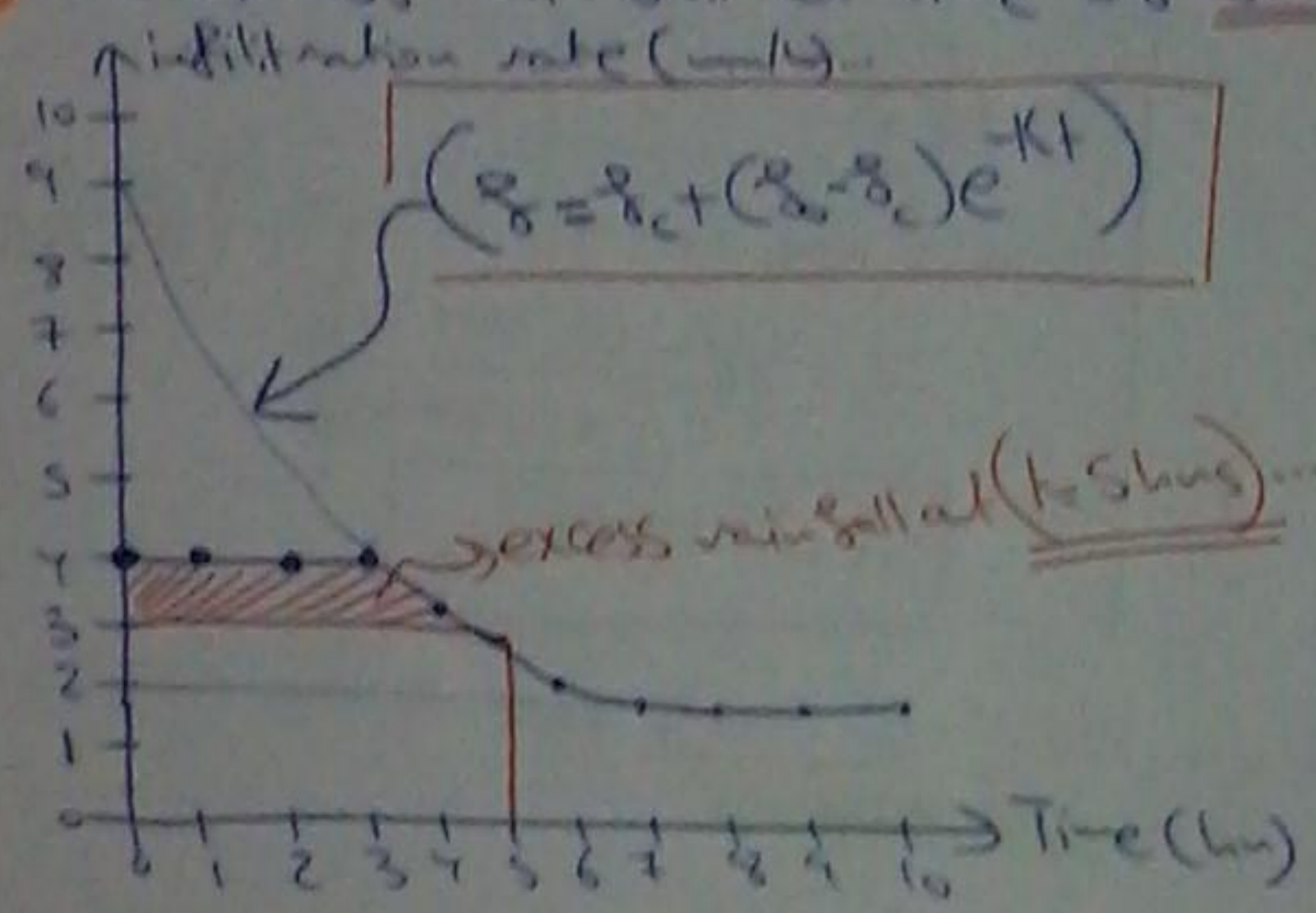
⑥ From the hydrograph shown, the peak flow due to the excess rainfall is (3) m³/s $\rightarrow (5-2)$...

⑦ For the same watershed, as the rainfall amount increases, the UH values The same ... (depend on watershed characteristics) $\rightarrow$ (stay constant)

Question 2

A watershed is exposed to rainfall of constant intensity and long duration. The graph below describes the infiltration rate of that watershed. Neglecting the evaporation interception and storage rates, answer the following short statement and give proper units:

- The equilibrium infiltration rate (2) mm/hr...
- The actual infiltration rate at time of (1 hr) (4) mm/hr...
- The rainfall intensity (4) mm/hr...
- The excess rainfall at time of 5 hrs $4 - 3 = (1)$ mm/hr...



Question 3

Total runoff

Time	*P(mm)*	*Q*	*Q _{res} ???
1	1.7	1.6	1.6 - 1 = 0.6
2	0.6	Q ₂	Q ₂ - 1 = Q ₂ *
3	1.5	Q ₃	Q ₃ - 1 = Q ₃ *
4	0	2.5	2.5 - 1 = 1.5
5	0	1	1 - 1 = 0

* Base flow = 1 m³/s
 * determine (Q₂) and (Q₃) ...
 كما نلاحظ قيمة 1 (Base flow = 1 m³/s)
 فلا نأخذ المربع الذي القيمة
 من الـ (Q) يجب مطبقه
 ... يا صا

$N=4$
 $M=3 \rightarrow u = 4 - 3 + 1 = (2)$

* at (u=1) $\rightarrow Q_1 = \sum_{i=1}^1 P_i U_i \rightarrow Q_1 = P_1 U_1 \rightarrow 0.6 = 1 * u_1$
 $u_1 = 0.6$

* at (u=2) $\rightarrow Q_2 = P_1 U_2 + P_2 U_1$

$Q_2 = 1 * U_2 + (0.6 * 0.6)$

$Q_2 = U_2 + 0.36 \rightarrow (1)$

* at (u=3) $\rightarrow Q_3 = P_1 U_3 + P_2 U_2 + P_3 U_1$

$Q_3 = U_3 + (0.6 U_2) + (1.5 * 0.6)$

$Q_3 = U_3 + 0.6 U_2 + 0.9 \rightarrow (2)$

* at (u=4) $\rightarrow Q_4 = P_1 U_4 + P_2 U_3 + P_3 U_2 + P_4 U_1$

$1.5 = (1) U_4 + (0.6) U_3 + (1.5) U_2 + P_4 (0.6)$

$1.5 = (1) U_4 + (0.6) U_3 + (1.5) U_2$

$1.5 = U_4 + 0.6 U_3 + 1.5 U_2 \rightarrow (3)$

$\therefore U_2 = 1$

$\therefore Q_2 = 1 + 0.36 = 1.36 \rightarrow (2.36)$

$\therefore Q_3 = (0.6 * 1) + 0.9 = 1.5 \rightarrow (2.5)$

*** Question 4 ***

The following table shows the total runoff from a watershed.
estimate the excess rainfall value (P_i)...

Time	excess rainfall (mm)	Total runoff (mm)	* Q * 8.45 - 8.45 = 0
0	0	8.45	22.13 - 8.45 = 13.68
1	P ???	22.13	18.29 - 8.45 = 9.84
2	0	18.29	32.39 - 8.45 = 23.94
3	14	32.39	25.67 - 8.45 = 17.22
4	0	25.67	8.45 - 8.45 = 0
5	0	8.45	8.45 - 8.45 = 0
6	0	8.45	

→ The value of $N=4$
The value of $M=2$...

$$u = N - M + 1$$

$$u = 4 - 2 + 1$$

$$u = 3 \rightarrow \begin{pmatrix} u_1, u_2, u_3 \\ \text{basis} \end{pmatrix}$$

$$u=1 \rightarrow Q_1 = P_1 U_1 \rightarrow 13.6 = P_1 U_1 \rightarrow \textcircled{1}$$

$$u=2 \rightarrow Q_2 = P_1 U_2 + P_2 U_1 \rightarrow 9.87 = P_1 U_2 + 0$$

$$9.87 = P_1 U_2 \rightarrow \textcircled{2}$$

$$u=3 \rightarrow Q_3 = P_1 U_3 + P_2 U_2 + P_3 U_1$$

$$23.94 = P_1 U_3 + 0 + 14 U_1$$

$$23.94 = 14 U_1$$

$$U_1 = \frac{23.94}{(14 \times 10^1)} \rightarrow U_1 = 17.1$$

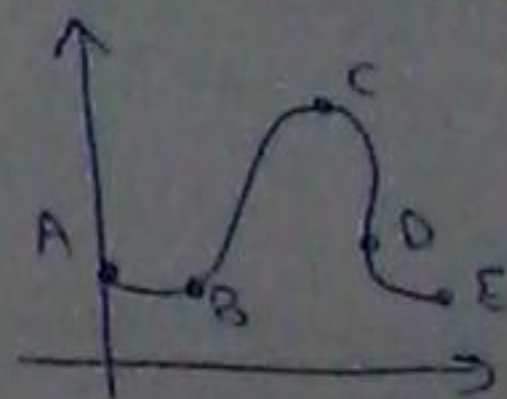
cm ←

$$\therefore 13.6 = P_1 \times 17.1 \rightarrow P_1 = 0.8 \quad \#$$

*** Question 5 ***

→ Shortly answer the following Sub-questions:

- ① The hantonic overland flow occurs when $i > (S, E, U, \text{intercept})$
- ② The depression storage highly affects storms that have ↓ duration
- ③ The sub-surface flow occurs due to groundwater
- ④ In the hydrograph shown, the surface runoff starts at point B
- ⑤ The UH is a characteristics of the watersheds
- ⑥ The S-hydrograph is used to Y-hr UH from X-hr
- ⑦ The watershed surface roughness ↑ then the excess rainfall ↓ (T)...
- ⑧ CN ↑ then the excess rainfall ↑ (T)...



Question 680 ***

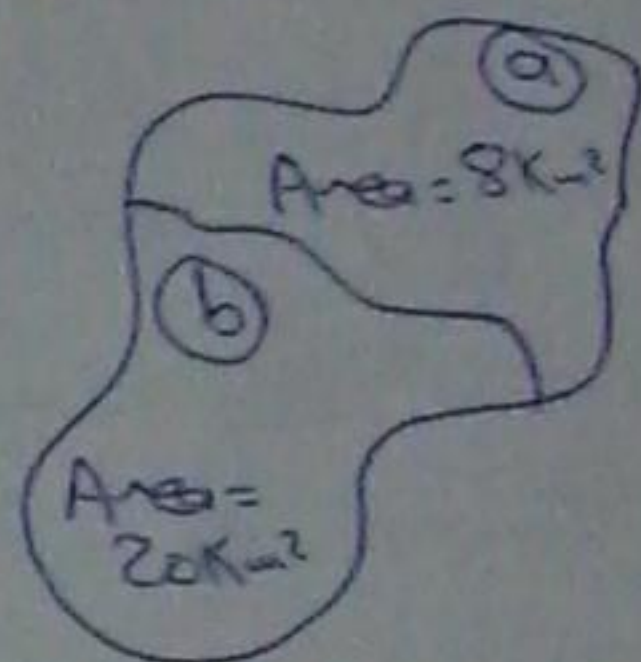
① The watershed shown consists of regions (a) and (b). Region (a) has (CN=50), while region (b) has (CN=70)...

① is the whole watershed faces a complete wet condition (AMC III). estimate the amount of the excess rainfall resulted from (25.4mm) total rainfall. (Hint: 25.4mm = 1 inches)
 $\rightarrow P = 1 \text{ inches}$

*** Solution ***

$$\rightarrow CN(II)_{avg} = \frac{(50 \times 8) + (70 \times 20)}{(8 + 20)}$$

$$CN(II)_{avg} = 64.28$$



$$\rightarrow CN(III) = \frac{23 \times CN(II)}{10 + 0.13 \times CN(II)}$$

$$\therefore CN(III) = \frac{23 \times 64.28}{10 + (0.13 \times 64.28)} = 80.54$$

$$\therefore S = \frac{1000}{CN} - 10 = \frac{1000}{80.54} - 10 = 2.41 \text{ inches}$$

$$\therefore P_e = \frac{(P - 0.2S)^2}{(P + 0.8S)} = \frac{(1 - 0.2 \times 2.41)^2}{(1 + 0.8 \times 2.41)} = 0.0916 \text{ inches} = 2.314 \text{ mm}$$

② Estimate the volume expected (m³) from the direct runoff resulted from such watershed?

*** Solution ***

$$U = P_e \times \text{area}$$

$$U = \frac{0.0916 \times 25.4}{1000} \times 28 \times 10^6$$

$$U = 65174.87 \text{ m}^3 \quad \#$$

*** Question 7 ***

$u = 3 - 1 + 1$
 $u = 3$
 (u_1, u_2, u_3)
 $\#$

* For (1-hr) *

Time	P	Q
1	2	1
2	0	2
3	0	1
4	0	0
5	0	0

* For (2-hrs) *

Time	P	U	Q
1	0.5	0.5	0.25
2	1	1	1
3	0.5	0.5	2
4	0	0	2
5	0	0	0.75

* Solution *

- For (1-hr) -

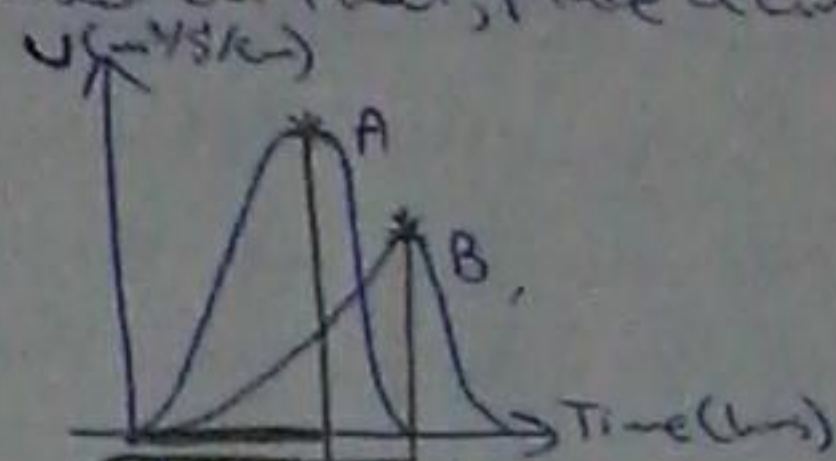
$$\begin{aligned} \rightarrow Q_1 &= P_1 u_1 \rightarrow 1 = 2 u_1 \\ \therefore u_1 &= 0.5 \\ \rightarrow Q_2 &= P_1 u_2 + P_2 u_1 \\ 2 &= 2(u_2) + 0 \\ \therefore u_2 &= 1 \\ \rightarrow Q_3 &= P_1 u_3 + P_2 u_2 + P_3 u_1 \\ 1 &= 2 u_3 + 0 + 0 \\ \therefore u_3 &= 0.5 \\ \therefore u_4 &= 0 \rightarrow Q_4 = 0 \\ \therefore u_5 &= 0 \rightarrow Q_5 = 0 \end{aligned}$$

- For (2-hr) -

$$\begin{aligned} Q_1 &= P_1 u_1 \rightarrow Q_1 = 0.5 * 0.5 \\ \therefore Q_1 &= 0.25 \\ Q_2 &= P_1 u_2 + P_2 u_1 \rightarrow Q_2 = 0.5 * 1 + 0.5 * 1 \\ \therefore Q_2 &= 1 \\ Q_3 &= P_1 u_3 + P_2 u_2 + P_3 u_1 \rightarrow \\ Q_3 &= (0.5 * 0.5) + (1 * 1) + (1.5 * 0.5) \\ \therefore Q_3 &= 2 \\ Q_4 &= P_1 u_4 + P_2 u_3 + P_3 u_2 + P_4 u_1 \\ Q_4 &= 1(0.5) + 1.5(1) + 0 \\ \therefore Q_4 &= 2 \\ Q_5 &= P_1 u_5 + P_2 u_4 + P_3 u_3 + P_4 u_2 + P_5 u_1 \\ Q_5 &= 0 + 0 + 1.5(0.5) + 0 + 0 \\ \therefore Q_5 &= 0.75 \end{aligned}$$

Question 8

The graph shows describes the unit hydrographs for two watershed (A and B). Both watershed have the same soil type and land cover. Based on that, place a circle around the most correct answer:



1 Compared to watershed (B), watershed (A) has an area that is:

- a) larger b) smaller c) the same ☒ d) can not be determined

2 Compared to watershed (B), watershed (A) has a slope that is:

- ☒ a) higher b) lower c) the same d) can not be determined

3 Compared to watershed (B), watershed (A) has a time of concentration that is:

- a) longer ☒ b) shorter c) the same d) can not be determined

4 Compared to watershed (B), watershed (A) receives precipitation that is:

- a) higher b) lower c) the same ☒ d) can not be determined

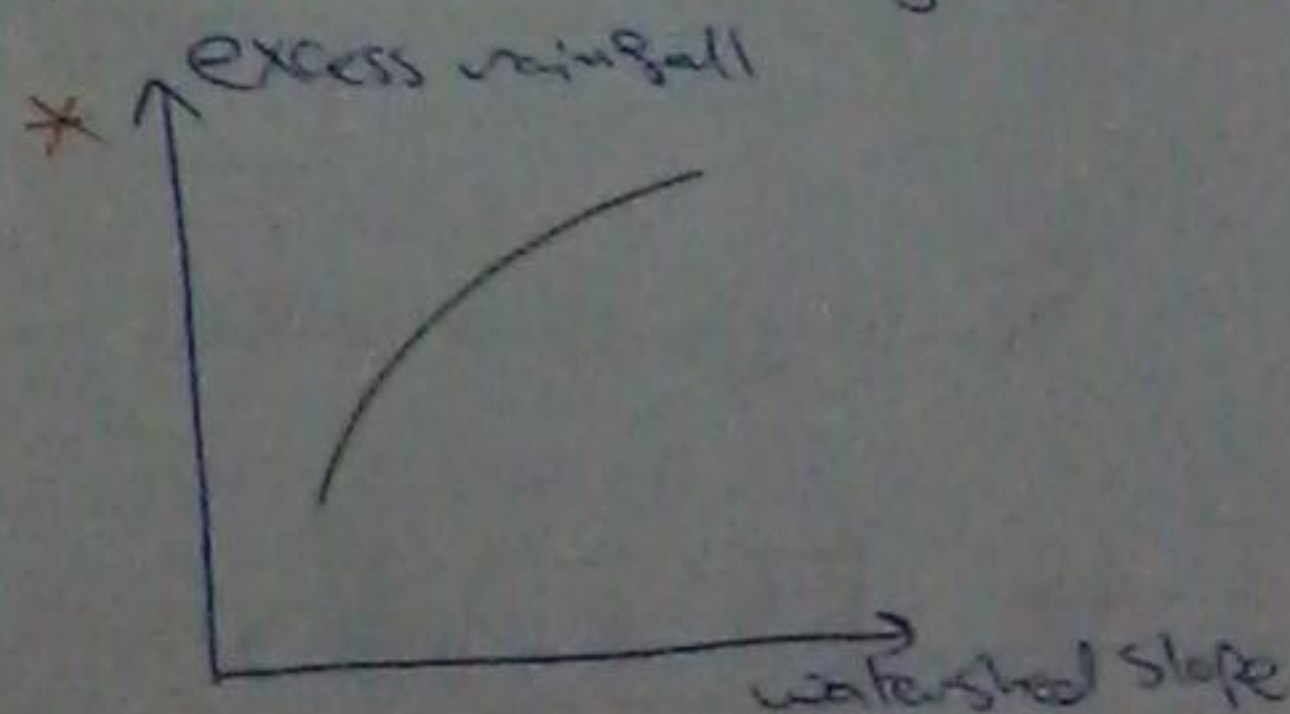
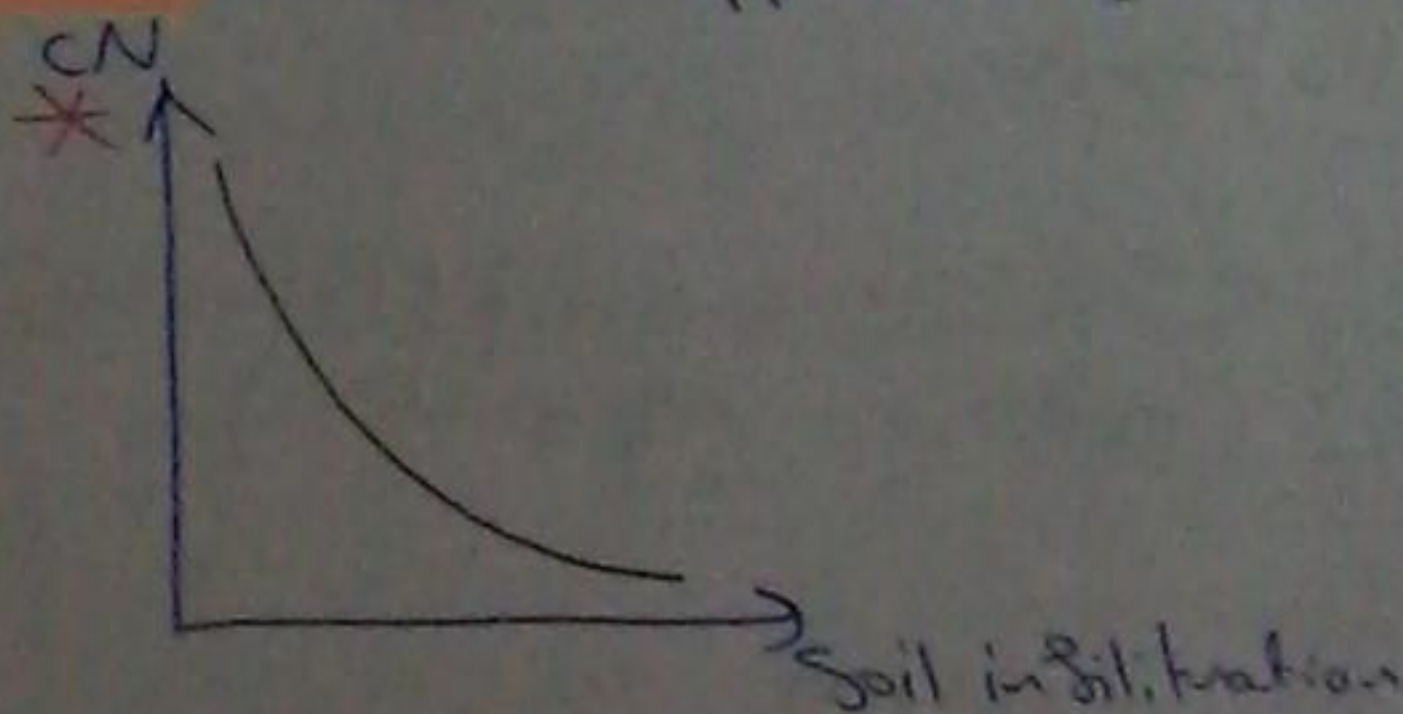
5 For watershed (A), as the precipitation amount increase, (UH) values:

- a) increase b) decrease ☒ c) remain the same d) slightly increase

6 If the surface roughness of watershed (B) has increased, then it's (UH) values:

- a) increase ☒ b) decrease c) remain the same d) can not be determined

7 Draw an approximate relationship between the following:



*** Question 9 ***

Watershed in arid region ($K_s = 0.7$ and $K_e = 1$) Soils an average air temperature of 30°C and solar radiation of 350 W/m^2 . The watershed soil equilibrium infiltration capacity is 0.7 mm/hr and the initial infiltration capacity is 9 mm/hr with infiltration constant (K) as $0.2/\text{hr}$. compute the excess rainfall at times $(t=1)$ and $(t=4 \text{ hrs})$ from the beginning of (5 hr) storm that has constant rainfall intensity of 6 mm/hr . neglect the depression storage and the interception losses.

→ DS

*** Solution ***

$$K_s = 0.7 \rightarrow K_e = 1 \rightarrow T = 30^\circ\text{C} \rightarrow R_n = 350 \text{ W/m}^2$$

$$f_c = 0.7 \text{ mm/hr} \rightarrow f_0 = 9 \text{ mm/hr} \rightarrow K = 0.2/\text{hr}$$

The excess rainfall ??? → beginning (5 hr)

- at $t=1 \text{ hr}$

- at $t=4 \text{ hr}$

$$\begin{aligned} \text{***} \rightarrow \text{at } t=1 & \rightarrow I_0 = 2500 - (2.36 \times T) \\ & I_0 = 2500 - (2.36 \times 30) \\ & I_0 = 2429.2 \text{ mm} \end{aligned}$$

$$\therefore E_r = \frac{R_n}{I_0} K_s K_e = \frac{350}{2429.2 \times 1000} \times 0.7 \times 1 \times 60 \times 60 \times 10^3$$

$$\therefore E_r = 0.36 \text{ mm/hr}$$

$$\therefore f = f_c + (f_0 - f_c) e^{-(Kt)} \rightarrow f = 0.7 + (9 - 0.7) e^{-(0.2 \times 1)} \rightarrow \underline{\underline{f = 7.495 \text{ mm/hr}}}$$

∴ The net rainfall available for runoff = $6 - 7.495 - 0.36$
(excess runoff = -1.855)...

$$\begin{aligned} \text{***} \rightarrow \text{at } t=4 & \rightarrow E_r = 0.36 \text{ mm/hr} \\ & f = 0.7 + (9 - 0.7) e^{-(0.2 \times 4)} \\ & \therefore \underline{\underline{f = 4.43 \text{ mm/hr}}} \end{aligned}$$

∴ The net rainfall available for runoff = $6 - 4.43 - 0.36$
(excess runoff = 1.21)...

→ The following table shows the direct runoff from a watershed considering its L-in $UH(m^3/s/cm)$...
compute the direct runoff (Q) and the excess rainfall (P)...

Times	excess rainfall (mm)	direct runoff $Q(m^3/s)$
0	0	0
1	P_1	Q_1
2	0	3.525
3	7	2.802
4	—	1.645
5	—	0.798
6	—	0

*** Solution *** The value of $(M=2)$ → The value of $(N=5)$...

$$\therefore M = 5 - 2 + 1 = \underline{\underline{4}} \dots \rightarrow \begin{matrix} U_1 \\ U_2 \\ U_3 \\ U_4 \end{matrix}$$

Time	excess rainfall (mm)	direct runoff $Q(m^3/s)$
1	P_1	Q_1
2	0	3.525
3	0.7	2.802
4	—	1.645
5	—	0.798

→ at $(u=1)$ → $Q_1 = P_1 U_1$ → ①

→ at $(u=2)$ → $Q_2 = P_1 U_2 + P_2 U_1$ → $3.525 = P_1 U_2$ → ②

→ at $(u=3)$ → $Q_3 = P_1 U_3 + P_2 U_2 + P_3 U_1$
 $2.802 = P_1 U_3 + P_3 U_1$

$2.802 = P_1 U_3 + 0.7 U_1$ → ③

→ at $(u=4)$ → $Q_4 = P_1 U_4 + P_2 U_3 + P_3 U_2 + P_4 U_1$
 $1.645 = 0.7 U_2$ → $U_2 = 2.35$

→ in (eq 2) → $3.525 = P_1 \times 2.35$ → $P_1 = 1.5 \text{ cm} = 15 \text{ mm}$

→ at $(u=5)$ → $Q_5 = P_1 U_5 + P_2 U_4 + P_3 U_3 + P_4 U_2 + P_5 U_1$
 $0.798 = 0.7 \times U_3$ → $U_3 = 1.14$

using eq (3) →

$$2.802 = P_1 U_1 + 0.7 U_1$$

$$2.802 = (1.5)(1.14) + 0.7 U_1$$

$$\therefore U_1 = 1.56$$

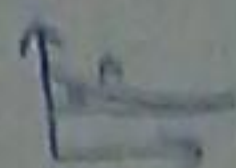
using eq (1) →

$$Q = P_1 U_1$$

$$Q = 1.56 \times 1.5$$

$$Q = 2.34 \text{ m}^3/\text{s} \quad \#$$

*** Question 11 ***



*** The curve below represents the infiltration rate for a soil type under different moisture conditions (condition A and B). Study the curve and shortly answer the following sub-questions placing proper units where applicable.

- ① The soil equilibrium infiltration capacity is about 3 mm/hr
- ② In terms of dry and wet expressions the soil under condition (A) is dry
- ③ The soil infiltration constant is $K = 8 + (8 - 8)e^{-Kt}$ (at 2 hrs)
 $7 = 8 + (12 - 8)e^{-K(2)}$ $K = 0.405$
- ④ at rainfall intensity of 6 mm/hr, the actual infiltration rate at time = 2 hrs is about (7 - 6 = 1 mm/hr) for soil under condition A, while (6 - 5 = 1 mm/hr) for soil under condition B.
- ⑤ in term of soil material (sand or clay), the soil under condition A behaves like sand while the soil under condition B behaves like clay.
- ⑥ at rainfall intensity of 12 mm/hr the excess rainfall rate at time = 2 hr is about 12 - 7 = 5 for soil under condition A, while 12 - 5 = 7 for soil under condition B.
- ⑦ Explain why as the storm duration increases, the infiltration rate changes
 ↑ duration ↓ infiltration rate ↓ velocity of water ↓ temperature and the relative humidity ↓ and the type of the soil effect on this ... ↑ evaporation ... (Type of the soil become more dry).

- ① The flow from a main well in a confined aquifer of (15m thick) is $\frac{Q}{25L}$ is the phreatic surface elevation at two observation wells (50m) and (20m) away of the main well and (114.6) and (112.5m) respectively, find the transmissivity of the aquifer ???

$$Q = \frac{2\pi K D (h_2 - h_1)}{\ln\left(\frac{r_2}{r_1}\right)}$$

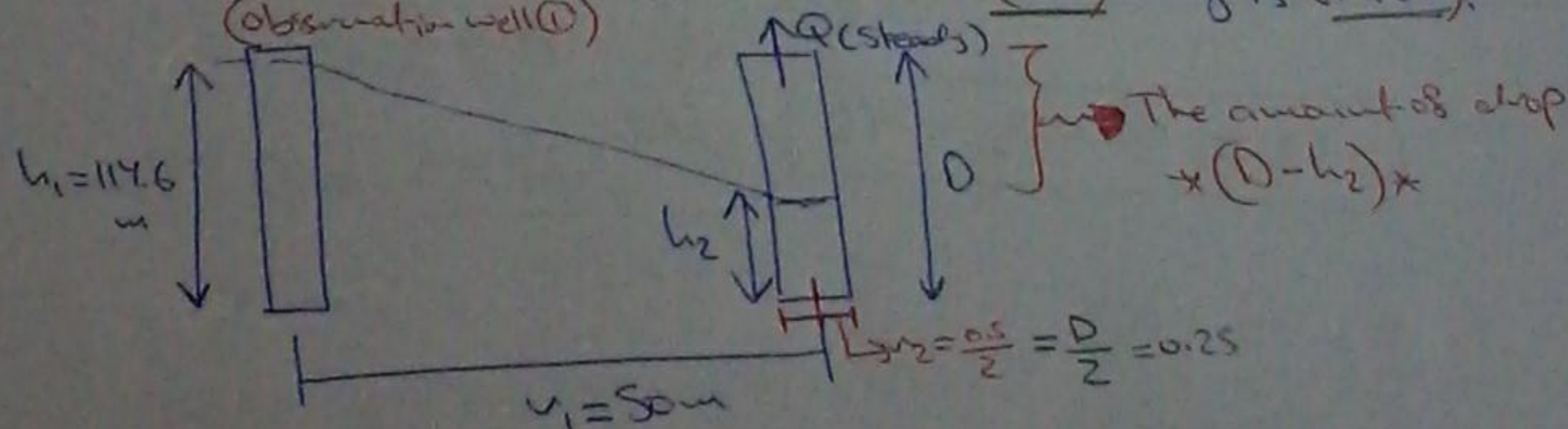
$$\frac{25}{1000} = \frac{2\pi (K) (15) (112.5 - 114.6)}{\ln\left(\frac{20}{50}\right)}$$

$$\therefore K = 1.6 \times 10^{-4} (\text{m/s})$$

$$\therefore K \approx 10 \text{ m/day}$$

$$T = 10 \times 15 = 150 \text{ m}^2/\text{day} \Rightarrow (KD)$$

- ② a main well has diameter of (0.5m) and transmissivity of (150 m²/day), what is the height of the phreatic surface (water table head) at the main well if the phreatic surface at an observation well (50m) away is (114.6m)?



$$Q = \frac{2\pi K D (h_2 - h_1)}{\ln\left(\frac{r_2}{r_1}\right)} \Rightarrow 0.025 = \frac{2\pi \left(\frac{150}{60 \times 60 \times 24}\right) (h_2 - 114.6)}{\ln\left(\frac{0.25}{50}\right)}$$

$$\therefore h_2 = 102.5\text{m}$$

$$\# \text{ drop} = 114.6 - 102.5 = 12.1\text{m}$$

③ A main well of (0.5m) diameter penetrates a (confined) aquifer of ($K=20\text{ m/day}$) and thickness of (35m). The flow is pumped from the main well such that its water table is maintained at drawdown (drop) of (5m) below the water table of an observation well that is (600m) from the main well, what is the discharge from the main well??

→ The value of ($r_2 = \frac{0.5}{2} = 0.25$)

→ The value of ($KD = (20\text{ m/day} \times 35)$)

$\therefore KD = 700\text{ m}^2/\text{day}$

$\therefore KD = \frac{700}{60 \times 60 \times 24} = \boxed{8.1 \times 10^{-3}}$

→ $D = 600\text{m}$ → The drop = 5m

$600 - 5\text{m} = \boxed{595\text{m}} \rightarrow h_2$

$\boxed{h_1 = 600\text{m}}$

→ $Q = \frac{2\pi KD(h_2 - h_1)}{\ln\left(\frac{r_2}{r_1}\right)}$

$Q = \frac{2\pi (8.1 \times 10^{-3})(595 - 600)}{\ln\left(\frac{0.25}{600}\right)}$

$\therefore Q = \boxed{0.055\text{ m}^3/\text{s}}$

→ From (2) → $\frac{\text{المجال}}{\text{المجال}}$
#

A groundwater well of (40 cm) diameter is confined aquifer
 of (25 m) thickness having $(K = 5 \text{ m/day})$ at steady state
 the piezometric surface elevation at two observation well that
 are (80 m) and (52 m) away from the ground water well
 are (42 m) and (28 m) respectively. estimate the piezometric
surface elevation at the ground water well???

$\Rightarrow \text{① } r = \frac{40}{2} = \frac{20}{100} = 0.2 \text{ m} = (r_1)$

Thickness = 25 m

$K = 5 \text{ m/day}$

$\therefore T = KD = \frac{5 \times 25}{60 \times 60 \times 24} = \boxed{1.75 \times 10^{-3}}$

$\Rightarrow Q = \frac{2\pi KD(h_2 - h_1)}{\ln\left(\frac{r_2}{r_1}\right)}$

$\therefore Q = \frac{2\pi(1.75 \times 10^{-3})(42 - 28)}{\ln\left(\frac{80}{52}\right)}$

$\therefore Q = 0.296 \text{ m}^3/\text{s}$

$\rightarrow \left(\frac{2\pi(1.75 \times 10^{-3})(28 - h)}{\ln\left(\frac{r}{80}\right)} \right)$
 ← بطلح ذلک اگواست

$\rightarrow \frac{h_2}{r_2} \rightarrow \frac{42}{0.2}$

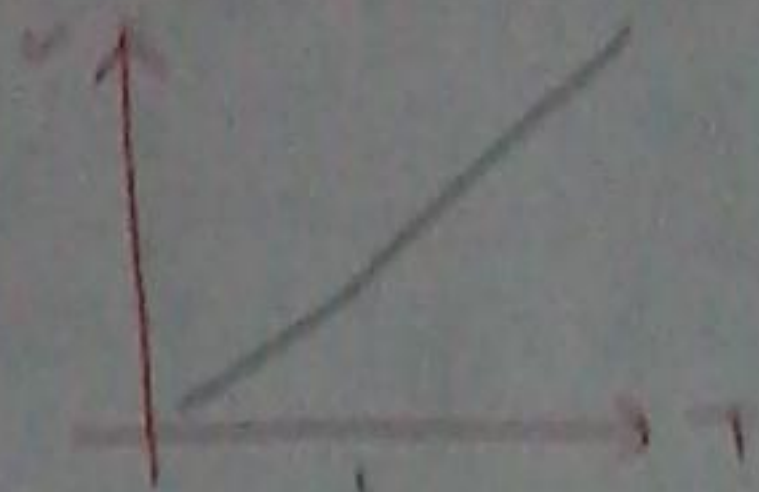
$\Rightarrow \text{② } Q = \frac{2\pi KD(h_2 - h_1)}{\ln\left(\frac{r_2}{r_1}\right)}$

$0.296 = \frac{2\pi(1.75 \times 10^{-3})(28 - h)}{\ln\left(\frac{0.2}{80}\right)} \Rightarrow \boxed{h = 222.66 \text{ m}}$

$0.296 = \frac{2\pi(1.75 \times 10^{-3})(h - 42)}{\ln\left(\frac{0.2}{80}\right)} \Rightarrow \boxed{h = 152.66 \text{ m}} \quad \text{OK} \quad \checkmark$

Problem 10

① The relationship between the T and u



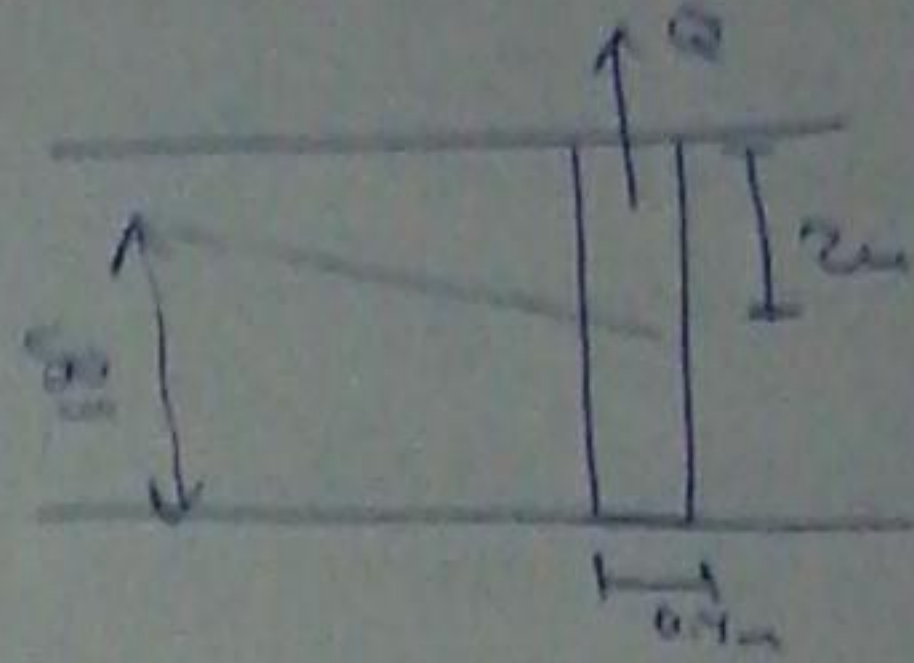
u (direct relationship)

Q1, Q2 also arranged

② unconfined
 $K = 10 \text{ m/day}$
 $D = 0.7 \text{ m}$

determine $v_1 = ???$

$Q = 1420 \text{ m}^3/\text{d}$



$\Delta h = d - q = 2 \text{ m}$

$h_1 = 5 \text{ m}$

$h_2 = 48 \text{ m}$

$v_2 = \frac{Q}{2} = 0.2 \text{ m}$

$v_1 = ???$

$$Q = \frac{2\pi K (h_2^2 - h_1^2)}{\ln\left(\frac{v_2}{v_1}\right)} \Rightarrow$$

$$1420 = \frac{2\pi \left(\frac{10}{\text{m} \cdot \text{d} \cdot 24}\right) ((48)^2 - (5)^2)}{\ln\left(\frac{0.2}{v_1}\right)}$$

$$1420 = \frac{0.143}{\ln\left(\frac{0.2}{v_1}\right)} \rightarrow 1420 \ln\left(\frac{0.2}{v_1}\right) = 0.143$$

$$\ln\left(\frac{0.2}{v_1}\right) = 1 \times 10^{-3}$$

$$\frac{0.2}{v_1} = 1$$

$$v_1 = 0.20 \text{ m} \quad \#$$

Exo

→ an aquifer of $(T = 150 \text{ m}^2/\text{day})$ ($S = 10^{-4}$) provides flow of (25 L/s) to a main well. Find the drop (S_d) at an observation well (20 m) away from the main well after (1 day) and (30 day) of pumping???

$$S_d = \frac{Q}{4\pi T} \ln\left(\frac{2.25 T t}{r^2 S}\right)$$

$$Q = \frac{25}{1000} = 0.025 \text{ m}^3/\text{s}$$

$$T = 150 \text{ m}^2/\text{day} = 150$$

$$S = \frac{150}{60 \times 60 \times 24} = 1.74 \times 10^{-3}$$

$$t = \begin{cases} 1 \text{ day} \\ 30 \text{ day} \end{cases}$$

$$S = 10^{-4}$$

$$r = 20 \text{ m}$$

$$S_d(\text{at } t=1 \text{ day}) = \frac{0.025}{4\pi(1.74 \times 10^{-3})} \ln\left(\frac{2.25(150)(1)}{(20)^2 \times 10^{-4}}\right)$$

$$S_d(\text{at } t=1 \text{ day}) = 10.36 \text{ m}$$

$$S_d(\text{at } t=30 \text{ day}) = \frac{0.025}{4\pi(1.74 \times 10^{-3})} \ln\left(\frac{2.25(150)(30)}{(20)^2 \times 10^{-4}}\right)$$

$$S_d(\text{at } t=30 \text{ day}) = 14.22 \text{ m}$$

$$S_d(\text{at } 30) - S_d(\text{at } 1) = S_d(\text{at } 29 \text{ day})$$

*** 180 ***

→ confined well produces flow through an aquifer of $T = 200 \text{ m}^2/\text{d}$.
The volume released per unit volume of aquifer per unit drop
in the water table is (0.008) calculate the (2 day) drop at an
observation well (40m) away from the main well when the
flow for the first day is $(100 \frac{\text{L}}{\text{s}})$ while for the second day
is $(80 \frac{\text{L}}{\text{s}})$.

$$*** \underline{\underline{S_{d1}}} * S_{d1} = \frac{Q}{4\pi T} \ln \left(\frac{2.25 T t}{r^2 S} \right)$$

$$\rightarrow S_{d1} = \frac{(100/1000)}{4\pi \left(\frac{200}{60 \times 60 \times 24} \right)} \cdot \ln \left(\frac{2.25 (200) (1)}{(40)^2 (0.008)} \right)$$

$$\boxed{S_{d1} = 12.238 \text{ m}}$$

$$\rightarrow S_{d2} = \frac{(80/1000)}{4\pi \left(\frac{200}{60 \times 60 \times 24} \right)} \cdot \ln \left(\frac{2.25 (200) (2)}{(40)^2 (0.008)} \right) -$$

$$\frac{(80/1000)}{4\pi \left(\frac{200}{60 \times 60 \times 24} \right)} \cdot \ln \left(\frac{2.25 (200) (1)}{(40)^2 (0.008)} \right)$$

$$\boxed{S_{d2} = 1.906 \text{ m}}$$

⊕ S_{d1} و S_{d2} دو روز اول و دوم افت
نسبت (S_d) نسبت اول و دوم
دقیقه ۲ و ۱ افت (نسبت)
نسبت (1) و (2)

∴ The Total accumulative drop over the whole (2 day)
equal $(12.238 + 1.906 = \underline{\underline{14.144 \text{ m}}})$

*** Problem ***

$\rightarrow T = 120 \text{ m}^2/\text{day}$ and $v = 50$

$S = 0.006$

$S_{d \text{ total}} = 18$

$Q_1 = 100 \text{ L/s}$

$Q_2 = 50 \text{ L/s}$

Calc. time???

*** $S_{d1} = \frac{(100/1000)}{4\pi \left(\frac{120}{60 \times 60 \times 24} \right)} \cdot \ln \left(\frac{2.25(120)(1)}{(50)^2(0.006)} \right)$

$S_{d1} = 16.57$

*** $S_{d2} = \frac{(50/1000)}{4\pi \left(\frac{120}{60 \times 60 \times 24} \right)} \cdot \ln \left(\frac{2.25(120)(t)}{(50)^2(0.006)} \right) -$

$\frac{(50/1000)}{4\pi \left(\frac{120}{60 \times 60 \times 24} \right)} \cdot \ln \left(\frac{2.25(120)(1)}{(50)^2(0.006)} \right)$

$\rightarrow S_{d \text{ total}} = S_{d1} + S_{d2}$

$18 = 16.57 + (2.86 \cdot \ln(18t)) - 8.28$

$18 = 8.289 + 2.86 \ln(18t)$

$\ln(18t) = \frac{18 - 8.289}{2.86} = 3.395$

$\therefore t = 1.65 \text{ day}$ #

Given table ...

complete the table...

t	I_{OH}	$S(t)$	$S(t - \Delta t_y)$	$2I_{OH} - OH$
0	0	0	0	0
1	0.3	0.3 + 0 = 0.3	0	0.15
2	2.6	0.3 + 2.6 = 2.9	0	1.75
3	6.2	2.9 + 6.2 = 9.1	0.3	4.4
4	4.7	9.1 + 4.7 = 13.8	2.9	5.75
5	0.4	13.8 + 0.4 = 14.2	9.1	2.55
6	0	14.2 + 0 = 14.2	13.8	0.2

← ١. عبادة الرباعي

$$\left(\frac{1}{\Delta t_j} (S(t) - S(t - \Delta t_j)) \right) \leftarrow$$

✱ ✱ ✱ ✱ ✱ ✱