

الهيئة العامة للغذاء والدواء  
الهيئة العامة للغذاء والدواء

# Foundation engineering

Notebook

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# Foundation

هندسة أساسات

إعداد الطالب : عمر زياد أبو زياد

\* هذه إدوسية لا تغني عن شرح الدكتور  
وانما هي وسيلة مساعدة \*

# Civilitee

اللجنة الأكاديمية  
لقسم الهندسة المدنية

# المحتوى

\* لفيرست ولسكند ولفاينيل :

- شرح بكارة مع تفصيل الأفكار المهمة

- الجداول ورسومات المطلوبة

- حلول أمثلة للكتاب المقترحة

- امتحان بفضل مع حله

\* First: ch. 4

- Terzaghi's Bearing Capacity.

- General Bearing Capacity.

- Eccentricity Loaded Footing.

- Bearing Capacity For Two Layers.

\* Second: ch. 6, 7, 12

- stress increment.

- settlement

- Lateral Earth Pressure.

\* Final: Ch. 13

- Tensile Crack

- Retaining Wall

- Piles.

\*\* تذكروا ان هذا العمل هو جهد بشري ، فإن اصبحت من الله ، وان اخطأت فمن نفسي  
في حال وجود اي خطأ او ملاحظة يرجى التواصل معي .

\* هذا العمل اهداء الى دفعة 2014

مع تمنياتي للجميع بالتوفيق

لا تنسوني ووالدي من صالح الدعاء

... أخوكم عمر

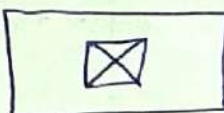

- Footing : Structure element "member" carry the loads from column to underground soil.

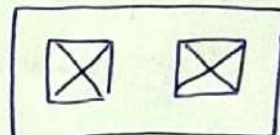
- Types of Footing :

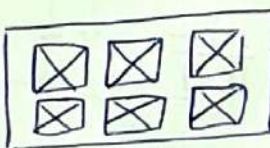
- <1> Shallow Footings
- <2> Deep Footings → Piles "فانيل"

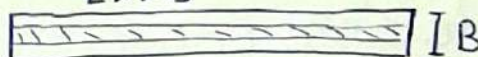
- Footing shape :

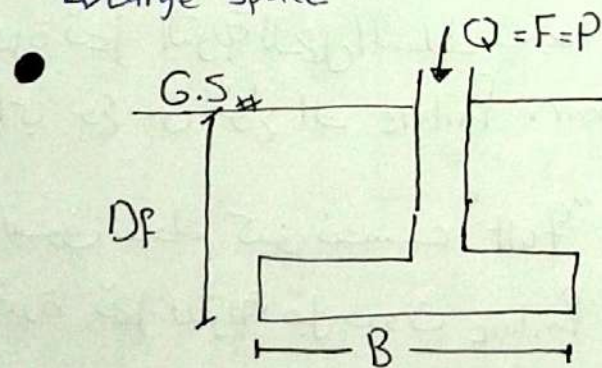
1- Square  2- Circular 

3- Rectangular  4- Ring Footing 

5- Combined : carry max 3 column (general 2) 

6- Mat (Raft) :   
 ↳ weak soil.  
 ↳ Large Load.  
 ↳ Large Space.

7- strip, continuous, wall   
 $L \gg B$



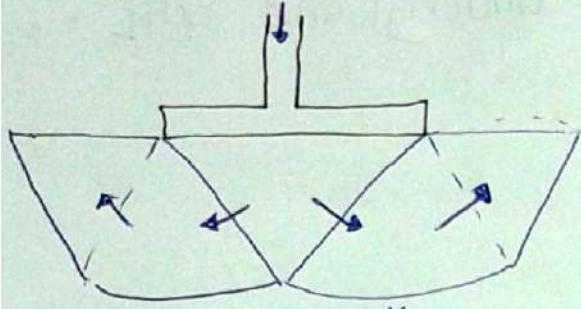
- \* B : width of footing " must be the shortest dimension on the plan "
- \* Df : Depth of footing .
- \* Q : Load .

• Type of failure : " The footing must be safe against " :

- <1> Shear failure in soil
- <2> excessive vertical displacement " Settlement " } المواضع بالتفصيل في المادة
- <3> excessive lateral movement .

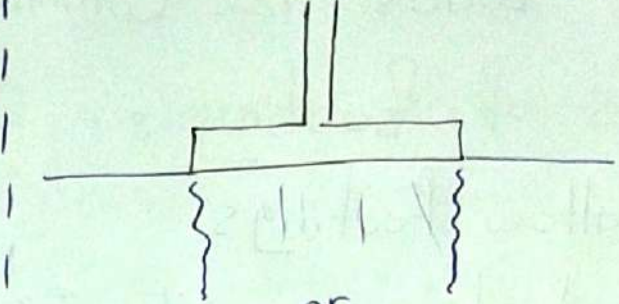
# • Type of Shear Failure :

## 1] General shear failure



- Stiff clay or dense sand
- Shallow Depth

## 2] punching shear failure

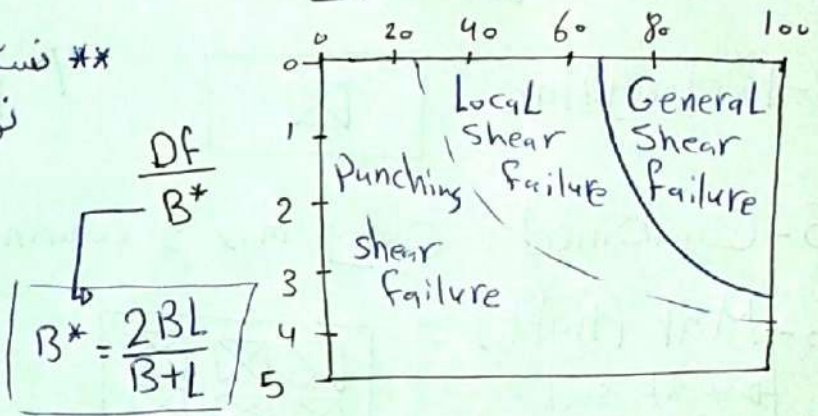


- Soft clay or loose sand
- great depth

## 3] Local shear failure : medium clay . (Dr) "relative density"

\*\* نستطيع من خلال (B, L, Dr) معرفة نوع ال failure وهو مهم جداً في الحل . " فكرة سنوات "

\*  $B^*$  for square = B



# • Bearing Capacity : قدرة تحمل التربة للحمل المبدل عليها قيد حدوث اي نوع من انواع ال shear failure .

$$F.S = \frac{q_{ult}}{q_{all}}$$

$$Q_{all} = (q_{all})(Area)$$

\* سوف نتعلم كيف نحسب "  $q_{ult}$  " وهي اكبر قدرة تحمل للتربة قبل حدوث failure ، ولكن التصميم لا يكون عليها از نأخذ معامل امان وهو " F.S " تحسب لاي طرف يكون ان يحدث ومن خلاله نقوم بحساب قدرة التحمل المسووع بها وهي "  $q_{all}$  " وهي التي سيتم التصميم والمقارنة بها .

# • "q<sub>ult</sub>" طرق حساب CH4 :

1 Terzaghi Bearing Capacity equ. : ~~يذكر في السؤال~~ استعمال

(A)  $q_{ult} = CN_c + \gamma N\gamma + \frac{1}{2} \gamma B N\gamma \rightarrow$  For wall/strip/contin. footing

(B)  $q_{ult} = 1.3 CN_c + \gamma N\gamma + 0.4 \gamma B N\gamma \rightarrow$  For square footing.

(C)  $q_{ult} = 1.3 CN_c + \gamma N\gamma + 0.3 \gamma B N\gamma \rightarrow$  For circular footing.

where :

$q_{ult}$  : Ultimate bearing capacity .  $C$  : Cohesion "for sand = 0"

$\gamma$  : stress at the bottom of footing " $D_f \cdot \gamma$ "

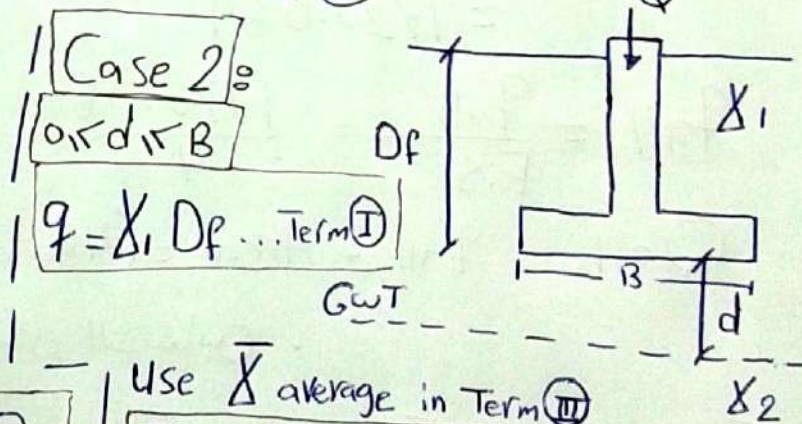
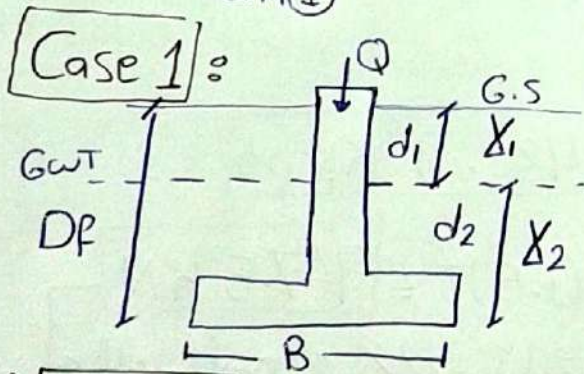
$\gamma$  : Unit of weight of soil underneath of footing الطبقة أسفل الأساس التي تتحمل اللود .

$B$  : width of footing .

$N\gamma, N\gamma, N_c$  : Bearing capacity factor from table .

\* Modification for GWT. : عند وجود مياه في الطبقات تحت تغيرات مستوى على القانون :

$$q_{ult} = \frac{CN_c}{\text{Term I}} + \frac{\gamma N\gamma}{\text{Term II}} + \frac{0.5 \gamma B \gamma N\gamma}{\text{Term III}}$$



if  $0 < d_1 \leq D$

$$\gamma = \gamma_1 d_1 + \gamma_2' d_2 \dots \text{Term II}$$

$$\gamma_2' = \gamma_2 - \gamma_w \text{ used in Term III}$$

Use  $\bar{\gamma}$  average in Term III

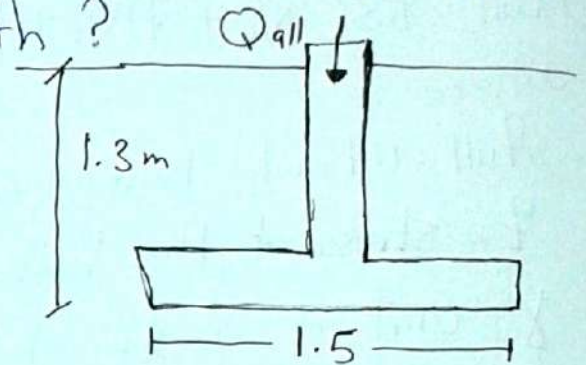
$$\bar{\gamma} = \gamma_2 + (\gamma_1 - \gamma_2) d/B$$

Case 3 : as in case II but  $d > B$ , GWT has no effect.   
 "للمفكرة سنوات"

Ex: A square foundation  $1.5\text{m} \times 1.5\text{m}$  in plane. The supporting soil has a friction angle  $\phi = 20^\circ$ , and effective cohesion  $c' = 65\text{ kPa}$ . The unit weight of soil is  $19\text{ kN/m}^3$ . Determine allowable gross load on foundation if the factor of safety = 4, and general shear failure occurs and ground water table at great depth?

Sol:

~~الحل:  $q_{ult} = c' N_c + \gamma D_f N_q + 0.5 \gamma B N_\gamma$~~   
~~أوجد  $q_{ult}$  من معادلات~~  
~~التأسيس لسائل القاعدة~~



$$q_{ult} = 1.3 c' N_c + \gamma N_q + 0.4 \gamma B N_\gamma$$

\* لا يوجد تأثير لمستوى المياه GW T  $q = D_f \gamma = (19)(1.3) = 24.7\text{ kPa}$

\*  $\phi = 20^\circ \Rightarrow N_c = 17.69, N_q = 7.44, N_\gamma = 3.64$

$$q_{ult} = (1.3)(65)(17.69) + (24.7)(7.44) + (0.4)(19)(1.5)(3.64) = 1720.069$$

$$q_{all} = \frac{q_{ult}}{F.S} = \frac{1720.069}{4} = 430.01\text{ kPa}$$

$$Q_{all} = q_{all} \times \text{Area} = (430.01)(1.5)^2 = 967.5\text{ kN}$$

الحد الأقصى للحمل المسموح به مطبق على الأساس.

Ex2: Same Ex1, the difference is a square found.  $B \times B$   
 Find B:

$$Q_{all} = 1000\text{ kN}$$

$$D_f = 1\text{ m}$$

$$q = D_f \gamma = (19)(1) = 19\text{ kPa}$$

$$Q_{ult} = (Q_{all})(F.S) = (1000)(4) = 4000\text{ kN}$$

$$q_{ult} = \frac{Q_{ult}}{\text{Area}} = 1.3 c' N_c + \gamma N_q + 0.4 \gamma B N_\gamma$$

$$\Rightarrow \frac{4000}{B^2} = (1.3)(65)(17.69) + (19)(7.44) + 0.4(19)B(3.64)$$

$$B = 1.54\text{ m}$$

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Note: if soils fails either in Local or punching shear failure mode use:

$$C^{(2)} = \frac{2}{3} C^{(1)}$$

$$\phi^{(2)} = \tan^{-1} \left( \frac{2}{3} \tan \phi^{(1)} \right)$$

reduction ← مع سؤال سنوات  
 ← دائماً في السؤال لو لم يذكر النوع يكون  
 . general

← معطى يعطيك (Dr%) مع الرسيه، انت يتحسب الـ  $B^*$  و بتسوف النوع اذا كان Local, punch. reduction قبل ما تبش حل (سنوات).

Ex: a circular footing of 1.6 m diameter founded on a soil has a unit weight of  $19.81 \text{ kN/m}^3$ , below water table and  $\gamma = 16.3 \text{ kN/m}^3$  above water table, The soil has  $C = 50 \text{ kPa}$  &  $\phi' = 25^\circ$ , the water table is 0.5 m below the footing, F.S = 3, Soil will fail in Local Shear Failure, find gross allowable Load?

$$q_{ult} = 1.3 C N_c + \gamma N_q + 0.3 \gamma B N_\gamma$$

\*\* Local shear failure: reduction

$$C^{(2)} = \frac{2}{3} C^{(1)} = \frac{2}{3} (50) = \frac{100}{3} \text{ kPa}$$

$$\phi^{(2)} = \tan^{-1} \left( \frac{2}{3} \tan(25) \right) = 17.26 \approx 17^\circ$$

→ From table:  $N_c = 14.6$ ,  $N_q = 5.45$ ,  $N_\gamma = 2.18$

\* GWT: Case (II)  $0 < d \leq B$

$$\bar{\gamma}_{avg} = \gamma_2 + (\gamma_1 - \gamma_2) \frac{d}{B} = (19.81 - 9.81) + (16.3 - (19.81 - 9.81)) * \frac{0.5}{1.6}$$

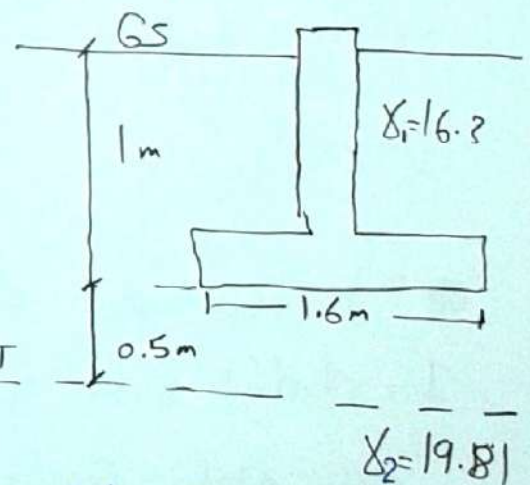
$$= 11.96 \text{ kN/m}^3$$

$$q = \gamma D_f = 16.3(1) = 16.3 \text{ kPa}$$

$$q_{ult} = (1.3) \left( \frac{100}{3} \right) (14.6) + (16.3)(5.45) + 0.3(11.96)(1.6)(2.18) = 734.01 \text{ kPa}$$

$$Q_{all} = q_{all} (Area) = \left( \frac{734.01}{3} \right) \frac{q_{ult}}{F.S} * \frac{\pi}{4} (1.6)^2 = 491.93 \text{ kN}$$

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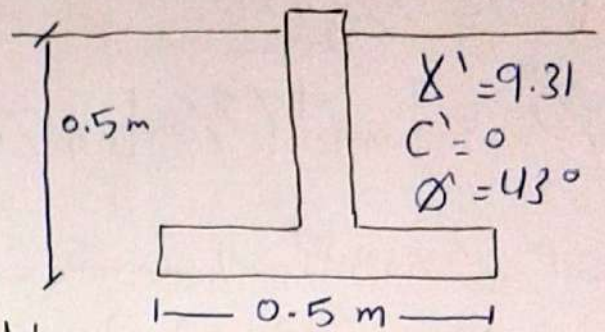




Ex: Compare Terzaghi bearing capacity for wall footing  
Versus a measured field test that result  $P_{ult} = 1863 \text{ KN}$ ?

Strip, wall, cont.  $L \gg B$   
Footing  $L \gg B$

$$\text{Area} = B \times 1$$



$$q_{ult} = c'N_c + \gamma N_q + 0.5 \gamma B N_\gamma$$

$$\gamma = D_f \gamma = (0.5)(9.31) = 4.655 \text{ kPa}$$

$$\phi = 43^\circ \rightarrow N_q = 126.5, N_\gamma = 211.56$$

$$q_{ult} = 0 + (4.655)(126.5) + 0.5(9.31)(0.5)(211.56) = 1081.26 \text{ kPa}$$

$$Q_{ult} = q_{ult} \times \text{Area} = 1081.26 \times 0.5 = 540.63 \text{ KN}$$

Terzaghi: مقارنته بـ 1863 جدآ قليلة فلا حظ بان محافظ جدآ .

● Shortcomings of Terzaghi equation: - Terz.  $Q_{ult}$   $\leftarrow$

- 1- didn't take general shape & like rectangular  
فقط هناك كالتساؤل محصورة على السطح لا يجرى الى عمق  $\leftarrow$
- 2- didn't take depth into consideration
- 3- ~ ~ Load inclination ~ .
- 4- ~ ~ base or ground ~ .
- 5- ~ ~ eccentricity into consideration

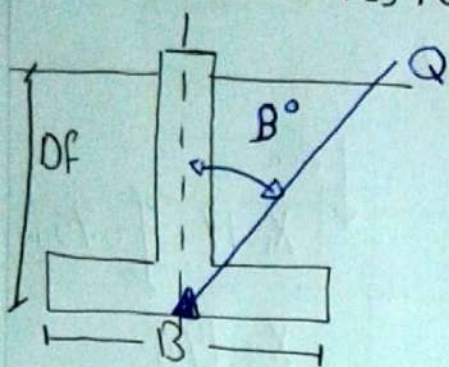
\* لذلك ننتقل للنوع الثاني .

\* ~~يطالب بالسؤال~~

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## 2] General Bearing Capacity :

$$q_{ult} = C N_c F_{cs} F_{cd} F_{ci} + \gamma N_q F_{qs} F_{qd} F_{qi} + 0.5 \gamma N_\gamma F_{\gamma s} F_{\gamma d} F_{\gamma i} B$$



where :  $q_{ult}$  = Ultimate Bearing Capacity

C : cohesion , B : width

$\gamma$  : stress at the bottom of footing

$\gamma$  : unit weight of soil underneath the footing

$N_c, N_q, N_\gamma$  : General Bearing Capacity.  $\text{جواب}$

### \* Shape factor ,

$$F_{cs} = 1 + B/L * \frac{N_q}{N_c}$$

$$F_{qs} = 1 + B/L \tan \phi$$

$$F_{\gamma s} = 1 - 0.4 B/L$$

### \* Depth factor :

- if  $\frac{DF}{B} \leq 1$  :

$$F_{cd} = 1 + 0.4 \frac{DF}{B}$$

$$F_{qd} = 1 + 2 \tan \phi (1 - \sin \phi)^2 \frac{DF}{B}$$

$$F_{\gamma d} = 1$$

- if  $\frac{DF}{B} > 1$  :

$$F_{cd} = 1 + 0.4 \left[ \tan^{-1} \left( \frac{DF}{B} \right) \right] \Rightarrow \text{rad}$$

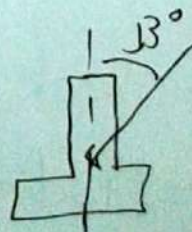
$$F_{qd} = 1 + 2 \tan \phi (1 - \sin \phi)^2 \left[ \tan^{-1} \left( \frac{DF}{B} \right) \right]$$

$$F_{\gamma d} = 1$$

### \* Load Inclination factor :

$$F_{ci} = F_{qi} = \left( 1 - \frac{\beta^\circ}{90^\circ} \right)^2$$

$$F_{\gamma i} = \left( 1 - \frac{\beta^\circ}{\phi^\circ} \right)^2 \Rightarrow \beta^\circ < \phi^\circ$$



Ex: A square footing  $B \times B$  has to be constructed as shown

Assume that:  $\gamma_1 = 17 \text{ kN/m}^3$ ,  $\gamma_2 = 19.5 \text{ kN/m}^3$ ,  $D_1 = 0.75 \text{ m}$

$D_f = 1.2 \text{ m}$ . The gross design allowable Load

$Q_{all} = 600 \text{ kN}$ ,  $F.S = 3$ , find  $B$ :

$C = 0$ ,  $\phi = 36^\circ$

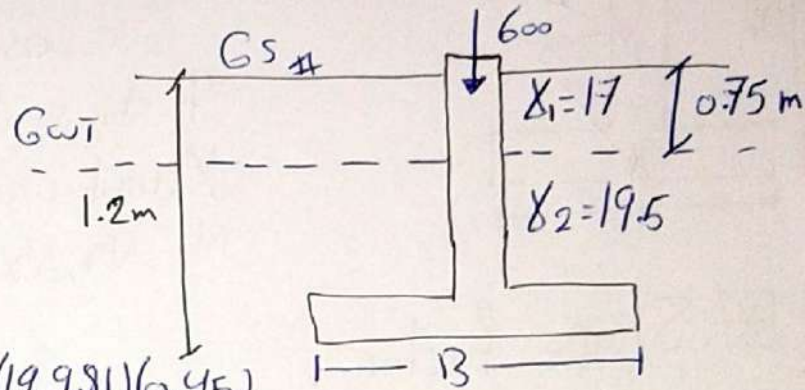
Sol: From general table

$$\phi = 36^\circ \rightarrow N_q = 37.75$$

$$\rightarrow N_\gamma = 56.31$$

$$q = \gamma_1 D_1 + \gamma_2 D_2 = (17)(0.75) + (19.5)(0.45)$$

$$= \boxed{17.11 \text{ kPa}}$$



\* Shape factor:

$$F_{qs} = 1 + \frac{B}{B} \tan(36) = \boxed{1.73}$$

$$F_{\gamma s} = 1 - 0.4 \frac{B}{B} = \boxed{0.6}$$

\* Depth factor: assume  $\frac{D_f}{B} \leq 1$ :

$$F_{qd} = 1 + 2 \tan(36)(1 - \sin 36)^2 \frac{1.2}{B} = \boxed{1 + \frac{0.29}{B}}$$

$$F_{\gamma d} = 1.0$$

\* Load is vertical so  $F_{qi} = F_{\gamma i} = 1.0$

$$Q_{ult} = Q_{all}(F.S) = 600 * 3 = 1800 \text{ kN}$$

$$\Rightarrow q_{ult} = Q_{ult} / \text{Area}$$

$$\Rightarrow \frac{1800}{B^2} = 0 + (17.11)(37.75)(1.73)\left(1 + \frac{0.29}{B}\right)(1) + 0.5(9.69)(B)(56.31)(0.6)(1)(1)$$

$$\frac{1800}{B^2} = 1117.4 + \frac{324.04}{B} + 163.69 B \Rightarrow \boxed{B = 1.06 \text{ m}}$$

$\Rightarrow$  Check assumption:  $\frac{D_f}{B} \leq 1$  ??  $\frac{1.2}{1.06} = 1.13 > 1$  ✗

$$\Rightarrow F_{qd} = 1 + 2 \tan(36)(1 - \sin 36)^2 \frac{1.2}{B}$$

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$$\Rightarrow \frac{DF}{B} > 1$$

$$F_{qd} = 1 + 2 \tan(36) (1 - \sin(36))^2 \tan^{-1} \left( \frac{1.2}{B} \right)$$

$$\Rightarrow \frac{1800}{B^2} = \frac{1117.4 + 163.09B + 275.9 \tan^{-1} \left( \frac{1.2}{B} \right)}{R.H.S}$$

⇒ Use Trial & Error

assume :

B(m)	L.H.S	R.H.S	$\Delta$
1.08	1666.67	1524.62	142.05 $\Delta_1$
1.12	1607.14	1526.15	80.99 $\Delta_2$
<del>1.06</del>		<del>1529.92</del>	$\Delta_3$

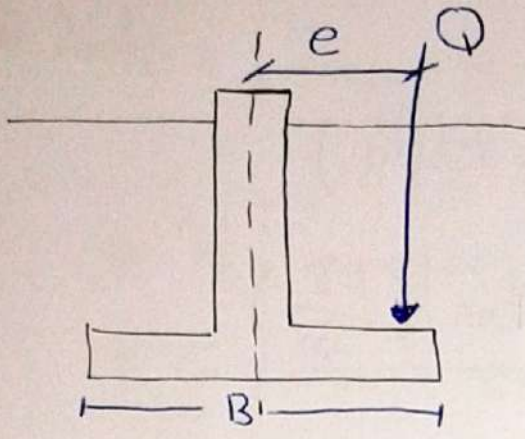
$$\left| \frac{\Delta_3 - \Delta_1}{\Delta_1} \right| \times 100\% < 2\% \quad ??$$

## ● Bearing Capacity of Soils on Eccentrically Loaded Footing :

\*\* في المواضع السابقة كان ال Load في مركز ال footing ، عندما تحصل ازاخة لل Load بمقدار "e" عن مركز الاساس ، سوف يتكون جهد اخر الاصل

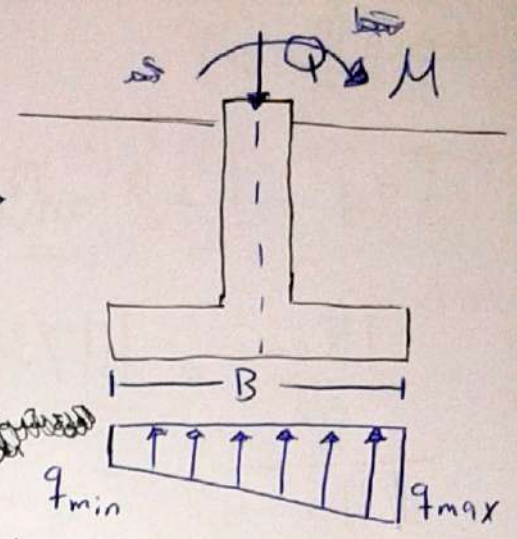
$$bending\ moment = \frac{My}{I} \quad \text{و } q_{xial} = \frac{P}{A} \quad \text{سيغير ذلك}$$

من حسابات ال  $q_{full}$  ،  $q_{fall}$



$$e = \frac{M}{Q}$$

$$\sigma = P/A + \frac{My}{I}$$



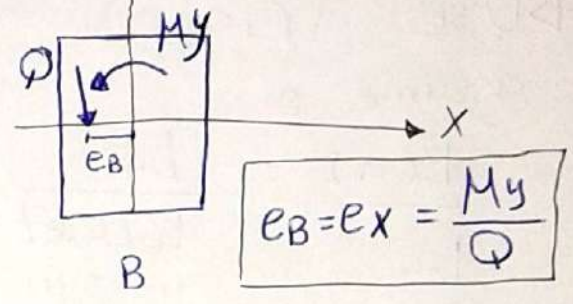
■ Cases of Eccentricity :

[1] In B-direction :

$$q_{max} = \frac{Q}{BL} + \frac{6M}{B^2L} = \frac{Q}{BL} \left( 1 + \frac{6eB}{B} \right)$$

$$q_{min} = \frac{Q}{BL} \left( 1 - \frac{6eB}{B} \right)$$

\* assume  $q_{min} = 0 \Rightarrow eB = \frac{B}{6}$



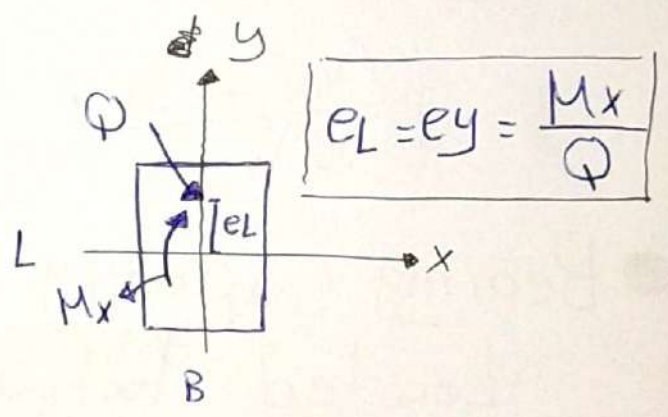
$$e_B = e_x = \frac{My}{Q}$$

[2] In L-direction :

$$q_{max} = \frac{Q}{BL} \left( 1 + \frac{6eL}{L} \right)$$

$$q_{min} = \frac{Q}{BL} \left( 1 - \frac{6eL}{L} \right)$$

\* assume  $q_{min} = 0 \Rightarrow eL = \frac{L}{6}$



$$e_L = e_y = \frac{M_x}{Q}$$

[3] In case of 2 way eccentricity :

$$q_{max} = \frac{Q}{BL} \left( 1 + \frac{6eB}{B} + \frac{6eL}{L} \right)$$

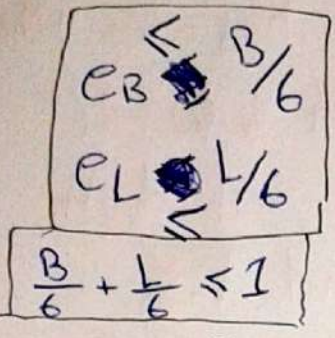
$$q_{min} = \frac{Q}{BL} \left( 1 - \frac{6eB}{B} - \frac{6eL}{L} \right)$$

\* assume  $q_{min} = 0 \Rightarrow$

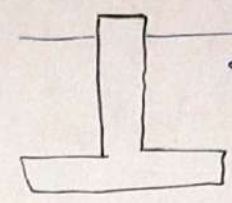
$$\frac{6eB}{B} + \frac{6eL}{L} = 1$$

Note:  $q_{min}$  must be  $\geq 0$

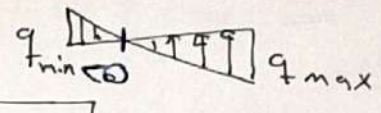
حتى لا يحدث Separation في التربة .  
ولتحقيق ذلك يجب ان تكون كل من



\*\* if  $e_B > B/6$



يحدث خلع، Separation



Define:

$B' = \text{effective width} = B - 2e_B$

$L' = \text{effective length} = L - 2e_L$

$A' = L' * B'$

\* شرط مهم جداً :  
يجب ان تكون  $B' < L'$  دائماً  
اذا كان العكس يستبدلهم.

Ex:  $B = 2m, L = 3m, e_B = 0.1m, e_L = 0.65m$

$B' = 2 - 2(0.1) = 1.8m$

$L' = 3 - 2(0.65) = 1.7m$

$\Rightarrow B' > L'$  so  $L' = 1.8m$   
 $B' = 1.7m$

General Capacity eq. with eccentricity:  $q_{all}$

- (1)  $N_c, N_q, N_\gamma \rightarrow$  same before
- (2) Shape factor  $\rightarrow$  use  $B', L'$  in it:  $F_{cs} = 1 + \frac{B'}{L'} \frac{N_q}{N_c}$
- (3) Depth factor  $\rightarrow$  same as before, use  $L, B$  original.
- (4) Load inclination  $\rightarrow$  no effect.
- (5)  $q_{ult} = C N_c F_{cd} + q N_q + \frac{1}{2} \gamma (B')$  ... use in last term.
- (6) F.s against Bearing capacity  $\Rightarrow F.S = \frac{q_{ult}}{q_{all}} \Rightarrow Q_{ult} = q_{ult} * A' = L' * B'$
- (7) F.s against  $q_{max}$ :  $F.S = \frac{q_{ult}}{q_{max}}$

$F.S > 1$

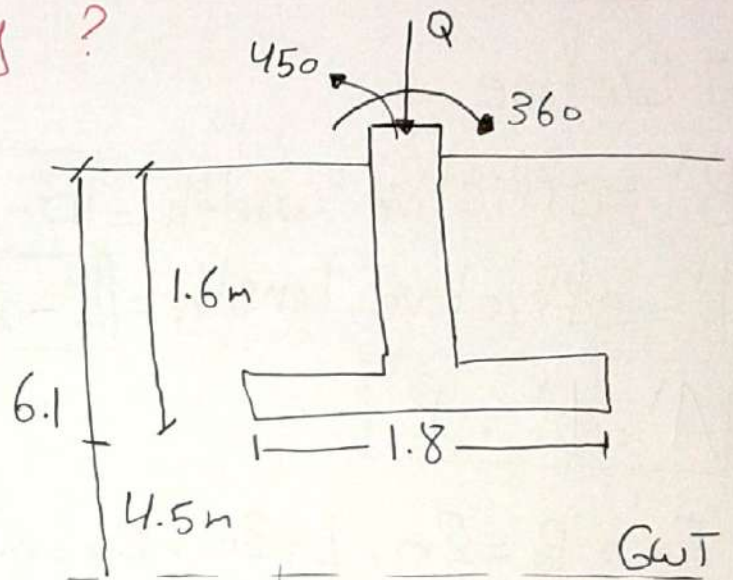
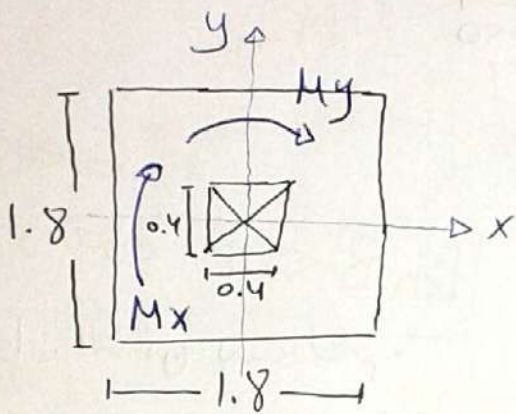
F.s against  $q_{max} > 1$

$q_{min} \geq 0$

\* عند وجود الزاوية هناك 3 checks



Ex 8 A Square Footing is 1.8m X 1.8m with a Square Column 0.4m x 0.4m with an axial Load of 1800 kN and  $M_x = 450$  kN.m and  $M_y = 360$  kN.m Soil shear strength parameter  $C = 20$  kpa &  $\phi' = 36^\circ$  Soil has a  $\gamma = 18$  kN/m<sup>2</sup> and GWT. at depth of 6.1 m below ground surface. Find Factors of safety ?



Sol:  $B = 1.8$  m ,  $L = 1.8$  m

$$* e_B = e_x = \frac{M_y}{Q} = \frac{360}{1800} = \boxed{0.2 \text{ m}}$$

$$* e_L = e_y = \frac{M_x}{Q} = \frac{450}{1800} = \boxed{0.25 \text{ m}}$$

$$* B' = B - 2e_B = 1.8 - 2(0.2) = \boxed{1.4 \text{ m}}$$

$$L' = L - 2e_L = 1.8 - 2(0.25) = \boxed{1.3 \text{ m}}$$

~~must be~~  $B' = 1.4 > L' = 1.3$

لكن يجب ان يكون  $B' < L'$  لذلك نستبدلهم

$\Rightarrow \boxed{B' = 1.3 \text{ m}}$  and  $\boxed{L' = 1.4 \text{ m}}$

$$* \phi' = 36 \Rightarrow N_c = 50.59 , N_q = 37.75 , N_\gamma = 56.31$$

- Shape Factor  $\gamma$  انتبه

$$F_{cs} = 1 + \frac{B'}{L'} \frac{Nq}{Nc} = 1 + \left(\frac{1.3}{1.4}\right) \left(\frac{37.75}{50.59}\right) = \boxed{1.69}$$

$$F_{qs} = 1 + \frac{B'}{L} \tan \phi = 1 + \left(\frac{1.3}{1.4}\right) (\tan 36) = \boxed{1.67}$$

$$F_{\gamma s} = 1 - 0.4 \frac{B'}{L'} = 1 - 0.4 \left(\frac{1.3}{1.4}\right) = \boxed{0.628}$$

- Depth Factors  $\gamma \frac{Df}{B} = \frac{1.6}{1.8} < 1$  انتبه

$$F_{cd} = 1 + 0.4 \frac{Df}{B} = 1 + 0.4 \left(\frac{1.6}{1.8}\right) = \boxed{1.35}$$

$$F_{qd} = 1 + 2 \tan \phi (1 - \sin \phi)^2 \frac{Df}{B} = 1 + 2 \tan(36) (1 - \sin 36)^2 \frac{1.6}{1.8} = \boxed{1.21}$$

$$F_{\gamma d} = 1.0$$

- No Load Inclination  $\gamma$

$$F_{ci} = F_{qi} = F_{\gamma i} = 1.0$$

$$* q = \gamma Df = (18)(1.6) = \boxed{28.8 \text{ Kpa}}$$

$$\Rightarrow q_{ult} = (20)(50.59)(1.69)(1.35)(1) + (28.8)(37.75)(1.67)(1.21)(1) + (0.5)(18) \left(\frac{1.3}{1.4}\right) (56.31)(0.628)(1)(1) = \boxed{4930.72 \text{ Kpa}}$$

$$\Rightarrow Q_{ult} = q_{ult} * A' = 4930.72 * (1.3 * 1.4) = \boxed{8973.91 \text{ Kpa}}$$

$$\textcircled{1} F.S_{BC} = \frac{Q_{ult}}{Q_{all}} = \frac{8973.91}{1800} = 4.98 > 1 \checkmark$$

$$\Rightarrow q_{max} = \frac{Q}{BL} \left(1 + \frac{6eB}{B} + \frac{6eL}{L}\right) = \frac{1800}{(1.8)(1.8)} \left(1 + \frac{6(0.2)}{1.8} + \frac{6(0.25)}{1.8}\right) = \boxed{1388.88 \text{ Kpa}}$$

$$\textcircled{2} F.S_{max} = \frac{q_{ult}}{q_{max}} = \frac{4930.72}{1388.88} = 3.55 > 1 \checkmark$$

$$\textcircled{3} q_{min} = \frac{Q}{BL} \left(1 - \frac{6eB}{B} - \frac{6eL}{L}\right) = -277.77 < 0 \times \text{Separation} \text{ جزء } \boxed{13}$$



Ex: A rectangular footing (1.5 m x 2.0 m) founded on Sand, the footing was designed with a factor of safety = 3, when constructed the contractor was displaced the center of column by 0.26 m away from the center along Long direction, and the column was inclined by  $8^\circ$  from vertical, Determine actual factor of safety.

1)  $Q_{design}$  before

Inc. & eccen. =

\*  $d > B$   
 $4 > 1.6 \Rightarrow$   $\gamma$   $\rightarrow$   $\gamma_{\text{direct}}$

\*  $\phi = 37^\circ \Rightarrow$   $\rightarrow$   $\text{الطبقة أسفل الـ footing مباشرة، Load ووزن (أسفل)}$

$N_q = 42.92$

$N_\gamma = 66.19$

• Shape factors:

$F_{qs} = 1.59$

$F_{\gamma s} = 0.7$

• depth factors:  $\frac{Df}{B} \text{ rad} > 1$

$F_{qd} = 1 + 2 \tan(37^\circ) (1 - \sin 37^\circ)^2 \tan^{-1} \left( \frac{1.8}{1.5} \right) = 1.2$

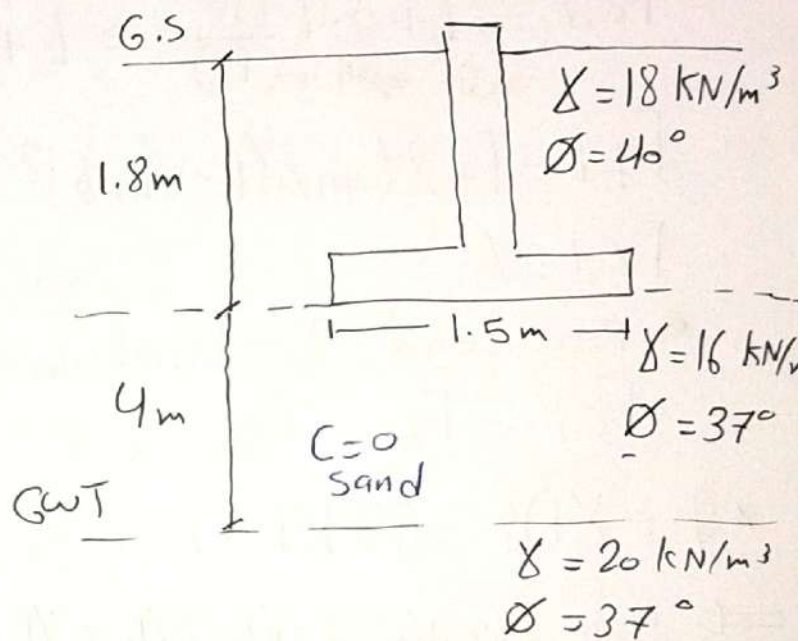
$F_{\gamma d} = 1.0$

• no Incline  $\Rightarrow F_{qi} = F_{\gamma i} = 1.0$

\*  $q = 18 \times 1.8 = 32.4 \text{ kPa}$

$q_{ult} = 3159.21 \text{ kPa}$

$Q_{design} = \frac{Q_{ult}}{F.S} = \frac{q_{ult} \times A}{F.S} = \frac{3159.21 / (1.5 \times 2)}{3} = 3159.21 \text{ kN}$  14



After Construction :

$$eL = 0.26 \text{ m "along Long direction"}$$

$$L' = L - 2eL = 2 - 2(0.26) = \boxed{1.48 \text{ m}}$$

$$B' = B - 2eB = 1.5 - 2(0) = \boxed{1.5 \text{ m}}$$

$B' > L'$   
 لذلك نستبدلهم  
 ↑

$$\boxed{B' = 1.48 \text{ m}} \\ \boxed{L' = 1.5 \text{ m}}$$

\* Shape factors :

$$F_{fs} = 1 + \frac{B'}{L'} \tan \theta = 1 + \frac{1.48}{1.5} \tan 37 = \boxed{1.74}$$

$$F_{xs} = 1 - 0.4 \frac{B'}{L'} = 1 - 0.4 \frac{1.48}{1.5} = \boxed{0.605}$$

\* depth factor : ~~same~~ same

$$F_{fd} = 1.2 \quad - \quad F_{xd} = 1.0$$

\* Incline by  $8^\circ$

$$F_{fi} = \left(1 - \frac{\beta^\circ}{90}\right)^2 = \left(1 - \frac{8}{90}\right)^2 = \boxed{0.83}$$

$$F_{xi} = \left(1 - \frac{\beta^\circ}{\theta}\right)^2 = \left(1 - \frac{8}{37}\right)^2 = \boxed{0.61}$$



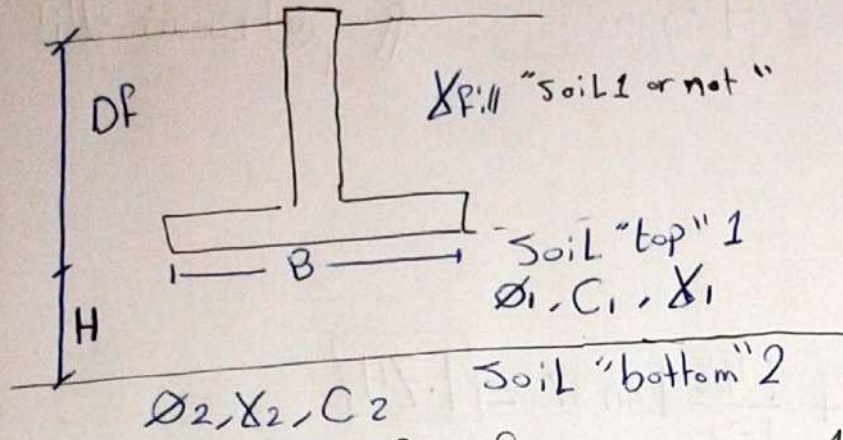
$$\Rightarrow q_{ult} = 0 + (32.4)(42.92)(1.74)(1.2)(0.83) + 0.5(16)(1.48)(66.19)(0.605)(0.61) \\ = \boxed{2699.19 \text{ kPa}}$$

$$\Rightarrow F.S = \frac{Q_{ult}}{Q_{design}} = \frac{q_{ult} A}{Q_d} = \boxed{1.89}$$

~~Find~~ Find  $q_{max}$  & check  $F.S_{max}$

# Bearing Capacity For two Layered Footing :

\* في الامثلة السابقة كان ال Failure يحدث في طبقة واحد ، سوف ندرس بهذا المفهوم حدوث ال Failure في طبقتين .



$C_a \equiv$  Adhesion  
 $K_s \equiv$  punching Coefficient  
 $H \equiv$  البعد من قاعدة الاساس لبطانة الطبقة الثانية

Check if Failure in 1 or 2 Layer :

\*  $H \geq 2B \Rightarrow$  one Layer الحل مثل السابق على القوانين الخاصة

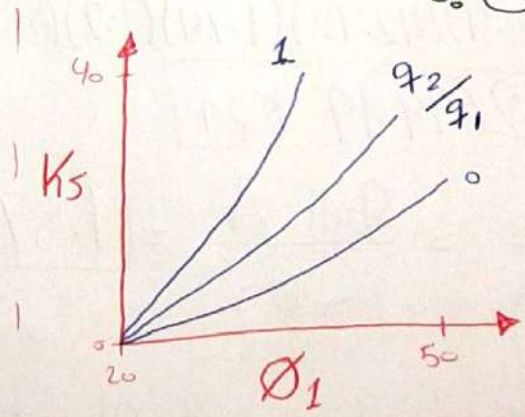
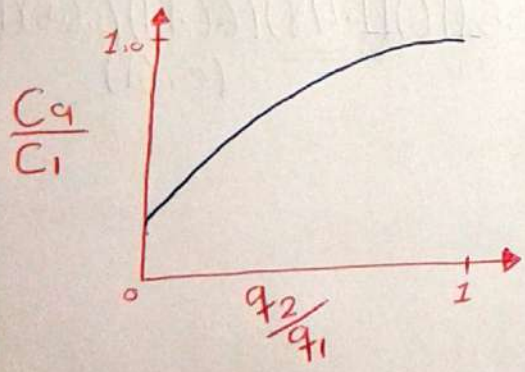
\*  $H < 2B \Rightarrow$  2 Layer قوانين خاصة

$q_{full} = q_b^{bottom} + (1 + B/L) \left( \frac{2C_a H}{B} \right) + \gamma_1 H^2 \left( 1 + \frac{B}{L} \right) \left( 1 + \frac{2DF}{H} \right) \left( \frac{K_s \tan \phi_1}{B} \right) - \gamma_1 H \leq q_t^{top}$

$q_b = C_2 N_{c2} F_{cs2} + \gamma_1 (DF + H) (N_{q2}) (F_{qs2}) + \frac{1}{2} \gamma_1 B N_{\gamma 2} F_{\gamma s2}$

$q_t = C_1 N_{c1} F_{cs1} + \gamma_1 (DF) N_{q1} F_{qs1} + \frac{1}{2} \gamma_1 B N_{\gamma 1} F_{\gamma s1}$

$C_a, K_s$  من الرسومات



\*\* فو حال كانت  $1 < \frac{q_2}{q_1}$  نأخذ منحني ال 1 .

$q_1 = C_1 N_{c1} + \frac{1}{2} \gamma_1 B N_{\gamma 1}$

$q_2 = C_2 N_{c2} + \frac{1}{2} \gamma_2 B N_{\gamma 2}$

undrained Soil  $\Rightarrow \phi = 0$

\*\* في الحل

$q_{full} < q_t$

نأخذ الاصغر ~~من~~ قسمة دائما .

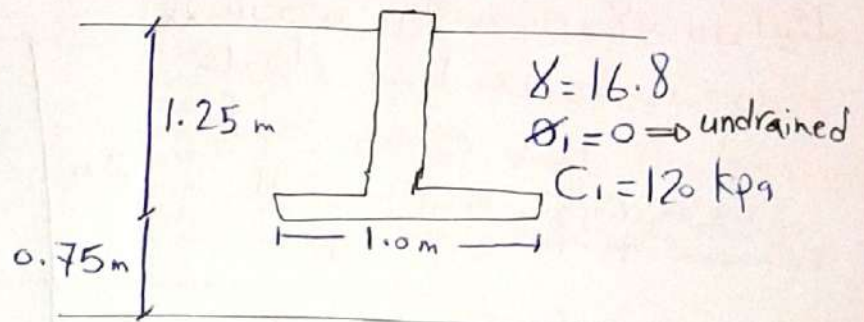
Ex 8 A Foundation 1.5 m x 1.0 m placed at depth of 1.25 m in a stiff clay. A soft clay layer is located at depth of 0.75 m, measured from the bottom of the foundation. \* For Top Layer, The Undrained Shear strength is 120 kPa &  $\gamma = 16.8 \text{ kN/m}^3$   
 \* For the bottom layer - the undrained shear strength is 48 kPa and  $\gamma = 16.2 \text{ kN/m}^3$ , Find the allowable bearing capacity if factor of safety = 3 ?

Sol :

Check :

$$H = 0.75 < 2B = 2$$

Two Layer



$$q_{ult} = q_b + (1 + \frac{B}{L}) \left( \frac{2c_u H}{B} \right) + \cancel{\gamma H^2 (1 + \frac{B}{L}) (1 + \frac{2D_c}{H}) \left( \frac{k \tan \phi_1}{B} \right)} - \gamma_1 H < q_{ft}$$

$= 0 \Rightarrow$  Since  $\tan \phi_1 = 0$

$$q_b = c_2 N_{c2} F_{cs2} + \gamma_1 (D + H) N_{q2} F_{qs2} + \cancel{0.5 \gamma_2 B N_{\gamma 2} F_{\gamma s2}}$$

$\phi_2 = 0 \Rightarrow N_c = 5.14, N_q = 1, N_\gamma = 0$

$$F_{cs2} = 1 + \frac{B}{L} \frac{N_{q2}}{N_{c2}} = 1 + \frac{1}{1.5} * \frac{1}{5.14} = \boxed{1.13}$$

$$F_{qs2} = 1 + \frac{B}{L} \tan \phi_2 = \boxed{1}$$

$$\Rightarrow q_b = (48)(5.14)(1.13) + (16.8)(1.25 + 0.75)(1)(1) + 0 = \boxed{312.4 \text{ kPa}}$$

$$q_{ft} = c_1 N_{c1} F_{cs1} + \gamma_1 D F_{q1} F_{qs1} + \cancel{\frac{1}{2} \gamma_1 B N_{\gamma 1} F_{\gamma s1}}$$

$$\Rightarrow q_{ft} = (120)(5.14)(1.13) + (16.8)(1.25)(1)(1) = \boxed{717.98 \text{ kPa}}$$

$$q_1 = c_1 N_{c1} + \cancel{\frac{1}{2} \gamma_1 B N_{\gamma 1}} = (120)(5.14)$$

$$q_2 = c_2 N_{c2} + \cancel{\frac{1}{2} \gamma_2 B N_{\gamma 2}} = (48)(5.14)$$

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$$\Rightarrow \frac{q_2}{q_1} = \frac{48}{120} = \boxed{0.4} \xrightarrow{\text{من الارسه}} \frac{C_a}{C_1} = 0.9$$

$$\Rightarrow \boxed{C_a = 108 \text{ kpa}}$$

$$q_{ult} = 312.4 + (1 + 1.5) \left( \frac{2 \times 108 \times 0.75}{1} \right) + 0 - (16.8)(0.75) \leq 717.9$$

$$\Rightarrow \underline{569.8} < 717.98 \quad \text{نأخذ الاقل}$$

$$\Rightarrow q_{ult} = 569.8 \Rightarrow q_{all} = \frac{q_{ult}}{3} = \boxed{189.9 \text{ kpa}}$$

Ex 8

\*\* عند وجود تربة ضعيفة ولا بد من البناء

عليها قمنا بعمل حفريات ووضع

طبقة coarse تحت الأساس لزيادة

الbearing capacity

Find  $q_{all}$  if  $F.S. = 3$  ?

Sol 8

$$\phi = 5^\circ \rightarrow \begin{cases} N_c = 6.44 \\ N_q = 1.57 \\ N_\gamma = 0.45 \end{cases}$$

$$F_{cs2} = 1.24, \quad F_{qs2} = 1.08, \quad F_{\gamma s2} = 0.6$$

$$\Rightarrow q_b = (40)(6.44)(1.24) + (20 \times 2 + 1)(1.57)(1.08) + 0.5(16.2)(1.5)(0.45)(0.6) = \boxed{426.92 \text{ kpa}}$$

$$q_2 = (40)(6.44) + 0.5(16.2)(1.5)(0.45) = \boxed{265 \text{ kpa}}$$

$$\phi = 40^\circ \rightarrow \begin{cases} N_c = 64.2 \\ N_q = 109.2 \\ N_\gamma = 109.2 \end{cases}$$

$$\frac{q_2}{q_1} = \frac{265}{1641} = 0.16$$

$$\boxed{K_s = 2.5} \quad \text{من الارسه}$$

$$\Rightarrow F_{qs1} = 1.84, \quad F_{\gamma s1} = 0.6$$

$$\Rightarrow q_E = 0 + (20)(2)(64.2)(1.84) + 0.5(20)(1.5)(109.2)(0.6) = \boxed{5709.72 \text{ kpa}}$$

$$q_1 = 0 + 0.5(20)(1.5)(109.2) = \boxed{1641 \text{ kpa}}$$

$$q_{ult} = 426.92 + 0 + (20)(11)^2 \left( 1 + \frac{1.5}{11.5} \right) \left( 1 + \frac{2 \times 2}{1} \right) \left( \frac{2.5 \tan 40^\circ}{1.5} \right) - (20)(11) \leq 5709.72$$

$$\Rightarrow \underline{686.6 \text{ kpa}} < 5709.72 \text{ kpa} \Rightarrow \text{بوض الاقل}$$

$$\Rightarrow q_{all} = \frac{686.6}{3} = \boxed{228.66 \text{ kpa}}$$

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**Table 3.1** Terzaghi's Bearing Capacity Factors—Eqs. (3.4), (3.5), and (3.6)

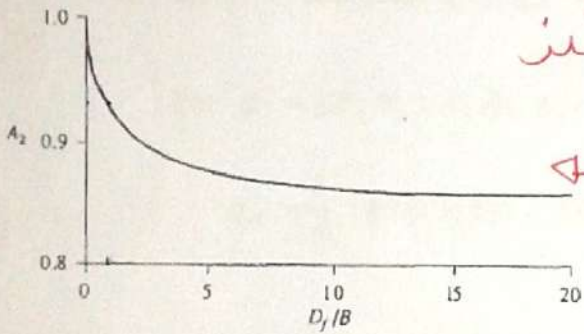
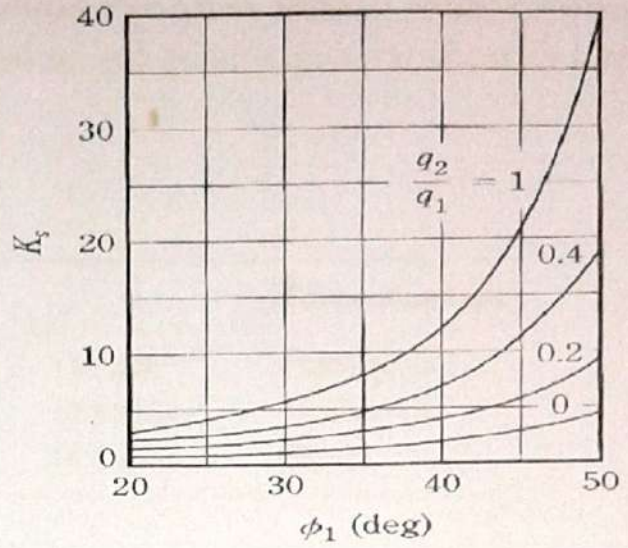
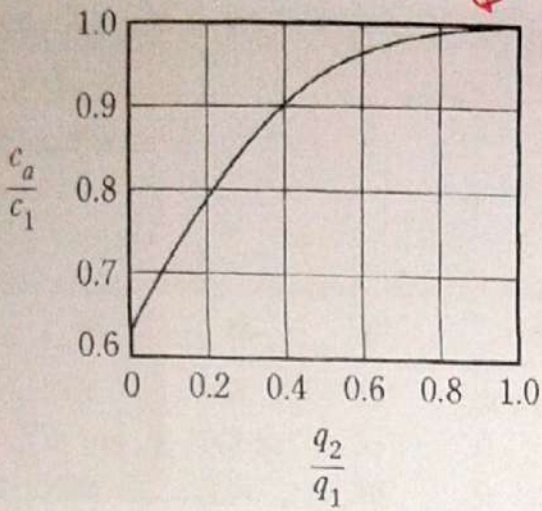
$\phi'$	$N_c$	$N_q$	$N_\gamma$ *	$\phi'$	$N_c$	$N_q$	$N_\gamma$ *
0	5.70	1.00	0.00	26	27.09	14.21	9.84
1	6.00	1.10	0.01	27	29.24	15.90	11.60
2	6.30	1.22	0.04	28	31.61	17.81	13.70
3	6.62	1.35	0.06	29	34.24	19.98	16.18
4	6.97	1.49	0.10	30	37.16	22.46	19.13
5	7.34	1.64	0.14	31	40.41	25.28	22.65
6	7.73	1.81	0.20	32	44.04	28.52	26.87
7	8.15	2.00	0.27	33	48.09	32.23	31.94
8	8.60	2.21	0.35	34	52.64	36.50	38.04
9	9.09	2.44	0.44	35	57.75	41.44	45.41
10	9.61	2.69	0.56	36	63.53	47.16	54.36
11	10.16	2.98	0.69	37	70.01	53.80	65.27
12	10.76	3.29	0.85	38	77.50	61.55	78.61
13	11.41	3.63	1.04	39	85.97	70.61	95.03
14	12.11	4.02	1.26	40	95.66	81.27	115.31
15	12.86	4.45	1.52	41	106.81	93.85	140.51
16	13.68	4.92	1.82	42	119.67	108.75	171.99
17	14.60	5.45	2.18	43	134.58	126.50	211.56
18	15.12	6.04	2.59	44	151.95	147.74	261.60
19	16.56	6.70	3.07	45	172.28	173.28	325.34
20	17.69	7.44	3.64	46	196.22	204.19	407.11
21	18.92	8.26	4.31	47	224.55	241.80	512.84
22	20.27	9.19	5.09	48	258.28	287.85	650.67
23	21.75	10.23	6.00	49	298.71	344.63	831.99
24	23.36	11.40	7.08	50	347.50	415.14	1072.80
25	25.13	12.72	8.34				

\*From Kumbhojkar (1993)

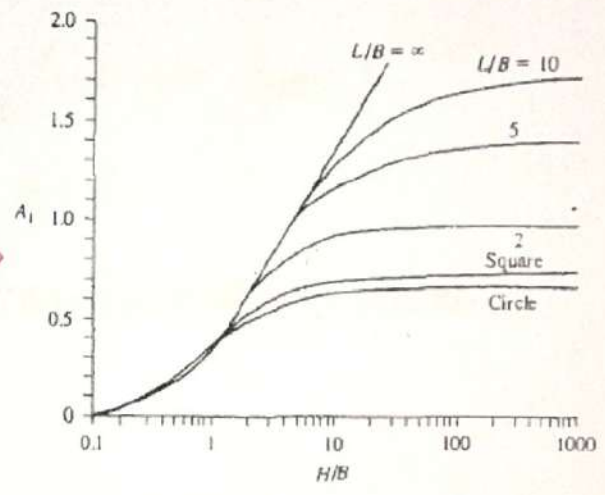
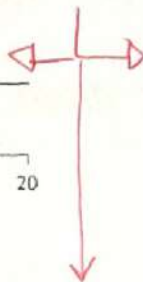
**Table 3.3** Bearing Capacity Factors

$\phi'$	$N_c$	$N_q$	$N_\gamma$	$\phi'$	$N_c$	$N_q$	$N_\gamma$
0	5.14	1.00	0.00	26	22.25	11.85	12.54
1	5.38	1.09	0.07	27	23.94	13.20	14.47
2	5.63	1.20	0.15	28	25.80	14.72	16.72
3	5.90	1.31	0.24	29	27.86	16.44	19.34
4	6.19	1.43	0.34	30	30.14	18.40	22.40
5	6.49	1.57	0.45	31	32.67	20.63	25.99
6	6.81	1.72	0.57	32	35.49	23.18	30.22
7	7.16	1.88	0.71	33	38.64	26.09	35.19
8	7.53	2.06	0.86	34	42.16	29.44	41.06
9	7.92	2.25	1.03	35	46.12	33.30	48.03
10	8.35	2.47	1.22	36	50.59	37.75	56.31
11	8.80	2.71	1.44	37	55.63	42.92	66.19
12	9.28	2.97	1.69	38	61.35	48.93	78.03
13	9.81	3.26	1.97	39	67.87	55.96	92.25
14	10.37	3.59	2.29	40	75.31	64.20	109.41
15	10.98	3.94	2.65	41	83.86	73.90	130.22
16	11.63	4.34	3.06	42	93.71	85.38	155.55
17	12.34	4.77	3.53	43	105.11	99.02	186.54
18	13.10	5.26	4.07	44	118.37	115.31	224.64
19	13.93	5.80	4.68	45	133.88	134.88	271.76
20	14.83	6.40	5.39	46	152.10	158.51	330.35
21	15.82	7.07	6.20	47	173.64	187.21	403.67
22	16.88	7.82	7.13	48	199.26	222.31	496.01
23	18.05	8.66	8.20	49	229.93	265.51	613.16
24	19.32	9.60	9.44	50	266.89	319.07	762.89
25	20.72	10.66	10.88				

فیرست



سکین



$$E_{x(\text{rectangle})} = \left(1 + 0.4 \log \frac{L}{B}\right) E_{x(\text{square})}$$

$$I_{z(m)} = 0.5 + 0.1 \sqrt{\frac{\bar{q} - q}{q'_{z(1)}}}$$

•  $I_z$  at  $z = 0$

$$I_z = 0.1 + 0.0111 \left(\frac{L}{B} - 1\right) \leq 0.2$$

• Variation of  $z_1/B$  for  $I_{z(m)}$

$$\frac{z_1}{B} = 0.5 + 0.0555 \left(\frac{L}{B} - 1\right) \leq 1$$

• Variation of  $z_2/B$

$$\frac{z_2}{B} = 2 + 0.222 \left(\frac{L}{B} - 1\right) \leq 4$$

- 4.1 For the following cases, determine the allowable gross vertical load-bearing capacity of the foundation. Use Terzaghi's equation and assume general shear failure in soil. Use FS = 4.

Part	B	D <sub>r</sub>	φ'	c'	γ	Foundation type
a.	3 ft	3 ft	28°	400 lb/ft <sup>2</sup>	110 lb/ft <sup>3</sup>	Continuous
b.	1.5 m	1.2 m	35°	0	17.8 kN/m <sup>3</sup>	Continuous
c.	3 m	2 m	30°	0	16.5 kN/m <sup>3</sup>	Square

a Eq. (3.3) and Table 3.1:  $q_{all} = \frac{q_u}{FS} = \frac{1}{FS} \left( c'N_c + qN_q + \frac{1}{2}\gamma BN_r \right)$

For  $\phi' = 28^\circ$ ,  $N_c = 31.61$ ,  $N_q = 17.81$ ,  $N_r = 13.7$

$$q_{all} = \frac{1}{4} \left[ (400)(31.61) + (110)(3)(17.81) + \frac{1}{2}(110)(3)(13.7) \right] = 5195 \text{ lb / ft}^2$$

b.  $q_{all} = \frac{q_u}{FS} = \frac{1}{FS} \left( c'N_c + qN_q + \frac{1}{2}\gamma BN_r \right)$

For  $\phi' = 35^\circ$ , from Table 3.1,  $N_c = 57.75$ ,  $N_q = 41.44$ ,  $N_r = 45.41$

$$q_{all} = \frac{1}{4} \left[ 0 + (12 \times 17.8)(41.44) + \frac{1}{2}(17.8)(1.5)(45.41) \right] = 372.8 \text{ kN / m}^2$$



c. Table 3.1:  $\phi' = 30^\circ$ ,  $N_q = 22.46$ ,  $N_\gamma = 19.13$

Eq (3.7), with  $c' = 0$

$$q_{all} = \frac{q_u}{FS} = \frac{1}{FS} (qN_q + 0.4\gamma BN_\gamma)$$
$$= \frac{1}{4} [(2 \times 16.5)(22.46) + (0.4)(16.5)(3)(19.13)] = 280 \text{ kN/m}^2$$

2. A square column foundation has to carry a gross allowable load of 1805 kN (FS = 3). Given:  $D_f = 1.5 \text{ m}$ ,  $\gamma = 15.9 \text{ kN/m}^3$ ,  $\phi' = 34^\circ$ , and  $c' = 0$ . Use Terzaghi's equation to determine the size of the foundation ( $B$ ). Assume general shear failure.

Eq (3.7);  $c' = 0$

$$q_{all} = \frac{q_u}{FS} = \frac{1}{FS} (qN_q + 0.4\gamma BN_\gamma)$$

$$q_{all} = \frac{Q_{all}}{B^2} = \frac{1805}{B^2}$$

From Table 3.1, for  $\phi' = 34^\circ$ ,  $N_q = 36.5$ ,  $N_\gamma = 38.04$

$$\frac{1805}{B^2} = \frac{1}{3} [(15)(15.9)(36.5) + (0.4)(15.9)(B)(38.04)]$$

By trial and error,  $B = 2 \text{ m}$

4.5 A column foundation (Figure P4.5) is  $3\text{ m} \times 2\text{ m}$  in plan. Given:  $D_f = 1.5\text{ m}$ ,  $\phi' = 25^\circ$ ,  $c' = 70\text{ kN/m}^2$ . Using Eq. (4.26) and  $\text{FS} = 3$ , determine the net allowable load [see Eq. (4.22)] the foundation could carry.

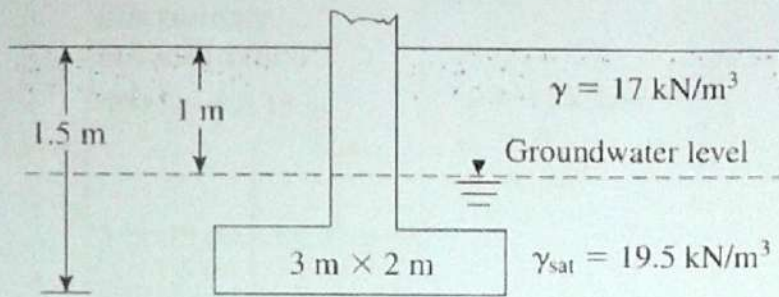


Figure P4.5

From table :

$$\phi = 25 \begin{cases} \rightarrow 20.72 \\ \rightarrow 10.66 \\ \rightarrow 10.88 \end{cases}$$

\* Shape Factors :

$$F_{cs} = 1 + \frac{B}{L} \frac{Nq}{Nc} = 1 + \frac{2}{3} \left( \frac{20.72}{18.88} \right) \left( \frac{10.66}{20.72} \right) = \boxed{1.34}$$

$$F_{gs} = 1 + \frac{2}{3} \tan \phi = 1 + \frac{2}{3} \tan 25 = \boxed{1.31}$$

$$F_{\gamma s} = 1 - 0.4 \times \frac{B}{L} = 1 - 0.4 \left( \frac{2}{3} \right) = \boxed{0.73}$$

\* Depth Factors :  $\frac{D_f}{B} = \frac{1.5}{2} < 1$

$$F_{cd} = 1 + 0.4 \frac{D_f}{B} = 1 + 0.4 \left( \frac{1.5}{2} \right) = \boxed{1.3}$$

$$F_{qd} = 1 + 2 \tan \phi (1 - \sin \phi)^2 \frac{D_f}{B} = 1 + 2 \tan(25) (1 - \sin 25)^2 \frac{1.5}{2} = \boxed{1.23}$$

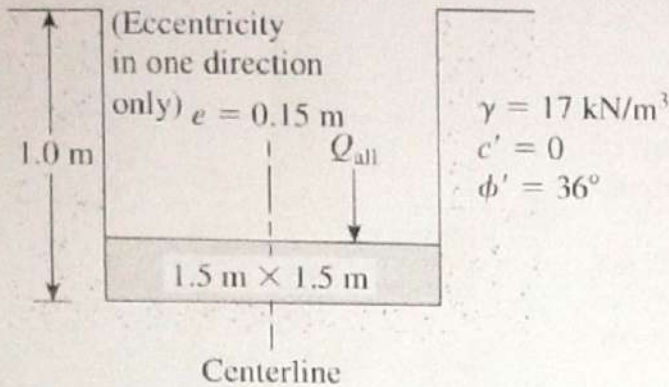
$$F_{\gamma d} = \boxed{1}$$

$$q = (1)(17) + 0.5(19.5 - 9.81)$$

$$q_{ult} = 70(20.72)(1.34)(1.3)(1) + (21.845)(10.66)(1.31)(1.23) + 0.5(19.5 - 9.81)(10.88)(0.73)(1)(2) = 2978.78 \text{ kPa}$$

$$Q_{all} = q_{all} * \text{Area} = \frac{q_{ult}}{\text{F.S.}} * \text{Area} = \frac{2978.78}{3} * 2 * 3 = \boxed{5957.58 \text{ KN}}$$

- 4.8 An eccentrically loaded foundation is shown in Figure P4.8. Use FS of 4 and determine the maximum allowable load that the foundation can carry. Use Meyerhof's effective-area method.



$$e_B = 0.15 \text{ m}$$

$$B' = B - 2e_B = 1.5 - 2(0.15) = \boxed{1.2 \text{ m}}$$

$$L' = L - 2e_L = 1.5 - 2(0) = \boxed{1.5 \text{ m}}$$

Eccent. in one direction only

\*\* from table  $\phi = 36^\circ$

$$\begin{aligned} \rightarrow N_q &= 37.75 \\ \rightarrow N_\gamma &= 56.31 \end{aligned}$$

\* Shape :

$$F_{qs} = 1 + \frac{B'}{1.5} \tan 36^\circ = \boxed{1.58}$$

$$F_{\gamma s} = 1 - 0.4 \times \frac{1.2}{1.5} = \boxed{0.68}$$

\* depth :

$$\frac{D_f}{B} = \frac{1}{1.5} < 1$$

$$F_{qd} = 1 + 2 \tan 36^\circ (1 - \sin 36^\circ)^2 \frac{1}{1.5} = \boxed{1.16}$$

$$F_{\gamma d} = 1$$

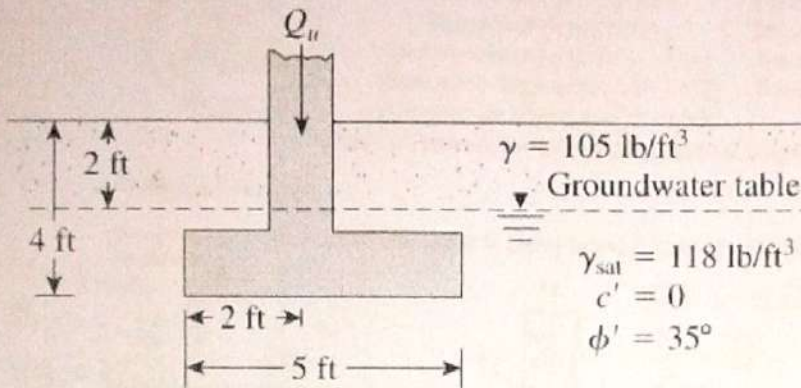
$$q_{ult} = 0 + \overset{q}{17} \times 37.75 \times 1.58 \times 1.16 + 0.5(17)(56.31)(0.68)(1)(\overset{B}{1.2})$$

$$= \boxed{1566.77 \text{ kPa}}$$

$$q_{all} = \frac{1566.77}{4} = 391.69$$

$$Q_{all} = q_{all} \times \text{Area} = 391.69 \times 1.5 \times 1.2 = \boxed{705.04 \text{ kN}}$$

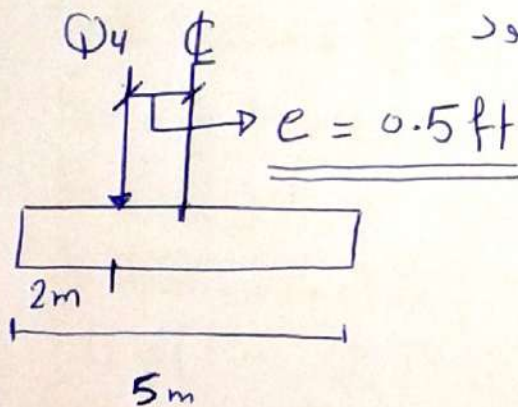
4.11 An eccentrically loaded continuous foundation is shown in Figure P4.11. Determine the ultimate load  $Q_u$  per unit length that the foundation can carry. Use the reduction factor method [Eq. (4.63)].



فكرة السؤال :-

يجب ان يكون اللود " ~~العمود~~ " في مركز ال footing

وال  $e$  هي البعد بين المركز واللود



والحل حل على قوانين ال eccentricity

وانتبه لـ water table

40 min "اختبر نفسك"

الرقم التسلسلي 55

Student Name: ... عمر زياد ... Student Number: 1432740



Hashemite University  
Faculty of Engineering  
Department of Civil Engineering  
Foundation Engineering (04/1435)  
Instructor: Dr. Omar A. Hattamleh

First Exam  
Monday: 31/10/2019  
Attempts: All Problems  
Write Only in the designated space

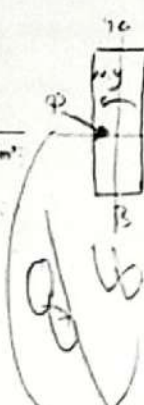
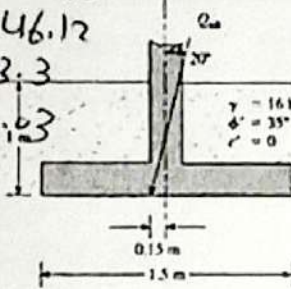
25

Note all calculation are made to nearest 2 significant digits

Problem # 1 (8 points)

A continuous (wall) foundation is shown in Figure below. Estimate the ultimate load, per unit length of the foundation.

From table  $\phi = 35$   
 $N_c = 46.12$   
 $V_q = 33.3$   
 $V_\gamma = 48.03$



$eB = 0.15 \text{ m}$

$B' = B - 2eB = 1.2 \text{ m}$

$\frac{B}{L} = 0$   
 $L \gg B \text{ or } 6$

Shape factor  $s$

$F_{qs} = 1 + \frac{B}{L} \tan^2 \phi \Rightarrow 1$

$F_{\gamma s} = 1 - 0 = 1$

Depth Factor  $s \frac{D_f}{B} \leq 1$

$F_{qd} = 1 + 2 \tan(35) (1 - \sin(35))^2 \frac{1}{1.5} = 1.17$

$F_{\gamma d} = 1.0$

Inclination factor  $\beta = 2^\circ$

$F_{qi} = (1 - \frac{20}{90})^2 = 0.605$

$F_{\gamma i} = (1 - \frac{20}{35})^2 = 0.184$

$q = 16 \times \gamma \times D_f = 16 \times 1 = 16 \text{ kPa}$

$\gamma = 16$

$q_{ult} = c N_c F_{cs} F_{ci} + q N_q F_{qs} F_{qd} F_{qi} + \frac{1}{2} \gamma N_\gamma F_{\gamma s} F_{\gamma d} F_{\gamma i}$

$= 0 + 16 \times 33.3 \times 1 \times 1.17 \times 0.605 + 0.5 \times 16 \times (48.03) \times 1 \times 1.17 \times 0.184$   
 $= 461.98 \text{ kPa}$

نتيجة

$\frac{F_{\gamma i}}{B}$   
 $\frac{1}{1.2} \times 16 \times 0.184$   
 $\times (1.2)$

$$Q_{ult} = q_{ult} * Area$$

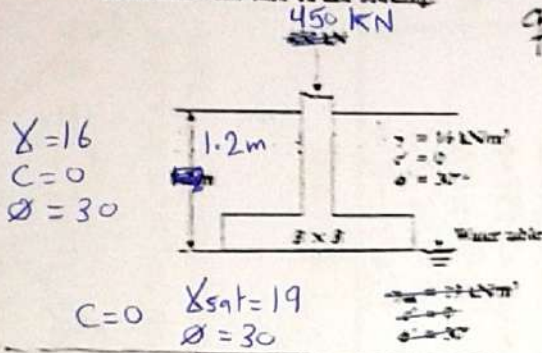
$$= 461.98 * B^1 = 461.98(1.2)$$

$$= \boxed{554.38 \text{ KN}}$$

Student Name: \_\_\_\_\_ Student Number: \_\_\_\_\_

Problem # 2 (7 points)

A square footing is shown in Figure below. Use Factor of Safety = 3 and Terzaghi bearing capacity equation determine the size of the footing.



$$q_{ult} = 1.3 C N_c + \gamma N_q + 0.4 \gamma B N_{\gamma} \quad \text{for square}$$

For G.W.T :

Case 2 :  $0 \leq d \leq B$

$$q = \gamma_1 D_f = 16 \times 1.2 = \boxed{19.2 \text{ kPa}}$$

$$\begin{aligned} \text{use } \bar{\gamma} &= \gamma_2 + (\gamma_1 - \gamma_2) \frac{d}{B} \\ &= \gamma_{sat} - \gamma_w = 19 - 9.81 \\ &= \boxed{9.19 \text{ kN/m}^3} \end{aligned}$$

from Table "Terzaghi"

$$\phi = 30$$

$$N_c = 37.16$$

$$N_q = 22.46$$

$$N_{\gamma} = 19.13$$

$$\begin{aligned} q_{ult} &= F.S \times q_{allowable} \\ &= \frac{3 \times 450}{\text{Area}} = \frac{1350}{B^2} \end{aligned}$$

$$\frac{1350}{B^2} = 1.3 \times (0)(37.16) + 19.2 \times 22.46 + 0.4 \times 9.19 \times B \times 19.13$$

$$\left( \frac{1350}{B^2} \right) = (0 + 431.23 + 70.32 B) \times B^2$$

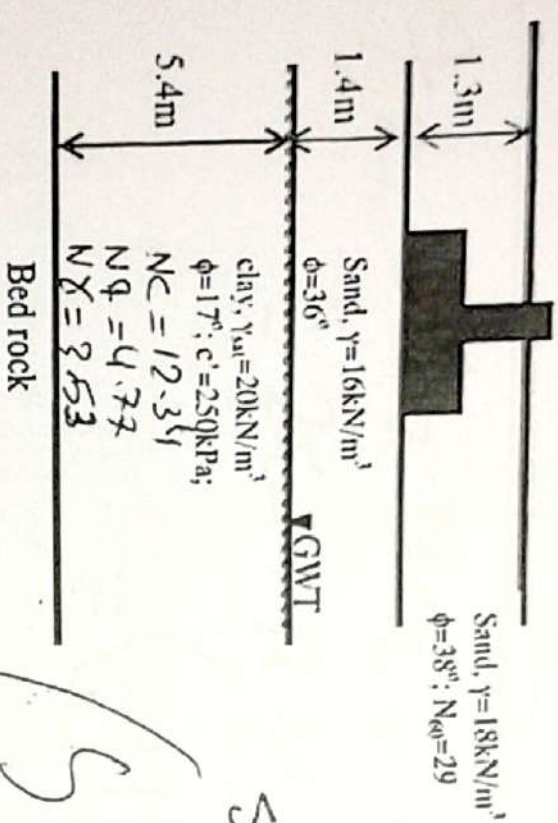
$$\Rightarrow 70.32 B^3 + 431.23 B^2 - 1350 = 0$$

$$\boxed{B = 1.58 \text{ m}}$$

Student Name: ... Student Number: ...

**Problem # 3: (3 points)**

A rectangular footing (1.6m x 2.0m) founded on soil profile shown. The footing was designed using factor of safety equal to 3.0.



Soil  $H = 1.41 \text{ m}$   
 $2B = 2 * 1.6 = 3.2 \text{ m}$

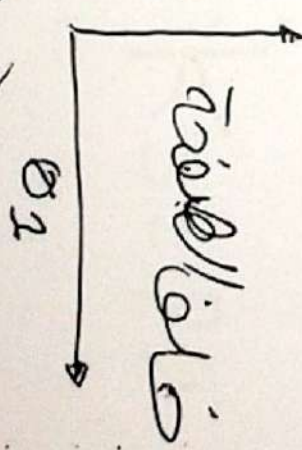
So  $H < 2B \Rightarrow$  ~~fail~~ Footing

will fail in two layers.

1. Is this footing will fail in two layers or in a single layers? Why?
2. If your answer is "yes" determine the punching-shear coefficient  $K_s$ ?

~~$q_2 = c_2 N_c + K_s q_2 + \gamma_1 (D_f + H) (N_q + 2) F_{qs2}$~~   
 ~~$+ \frac{1}{2} \gamma_2 B N_{\gamma 2} F_{\gamma s 2}$~~

~~$K_s = 1 + \frac{1.6}{2} * \frac{4.77}{12.24} = 1.31$~~





3)  $\frac{1}{2}$   $\frac{1}{2}$   $\frac{1}{2}$

2-859

$$q_1 = C_1 N C_1 + \frac{1}{2} \gamma_1 B N \gamma_1$$

$$Q = 36$$

$$N C = 50.5$$

$$N \gamma = 56.31$$

$$= 0 + 0.5 * 16 * 1.6 * 56.31$$

$$= 720.768 \text{ Kp9}$$

$$q_2 = C_2 N C_2 + 0.5 \gamma_2 B N \gamma_2$$

$$= 250 * 12.34 + 0.5 (20 - 9.81) * 1.6 * 3.53$$

$$N C_2$$

$$N \gamma =$$

$$= 3113.77 \text{ Kp9}$$

$$\frac{q_2}{q_1} = 4.32 \text{ السعة}$$

$$K_s = 22$$

1. Is this footing will fail in two layers or in a single layer? Why?
2. If your answer is "yes" determine the punching shear coefficient  $K_s$

$$q_2 = C_2 N_c \lambda_{cs2} + \gamma_1 (D_f + H) (N_q \lambda_{q2}) F_{q s2} + \frac{1}{2} \gamma_2 B \lambda_{cs2} F_{s s2}$$

$$F_{cs2} = 1 + \frac{1.6}{2} \times \frac{4.77}{12.34} = 1.31$$

$$F_{qs2} = 1 + \frac{1.6}{2} \tan(30^\circ) = 1.25$$

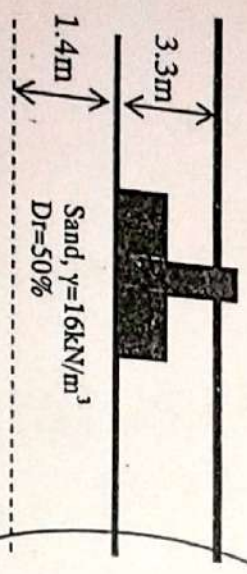
$$F_{s s2} = 1 + 0.4 \left( \frac{1.6}{2} \right) = 0.68$$

$$q_2 = 250 \times 12.34 \times 1.31 + 16(1.3 + 1.4) \times 4.77 \times 1.25 + 0.5(2 \times 9.81) \times 1.6 \times 3.53 \times 0.68$$

$$= 4318.5 \text{ kPa}$$

Problem # 4: (5 points)

A rectangular footing (1.6m x 2.0m) founded on soil profile shown. Find only the bearing capacity factors if  $\phi = 30^\circ$ .



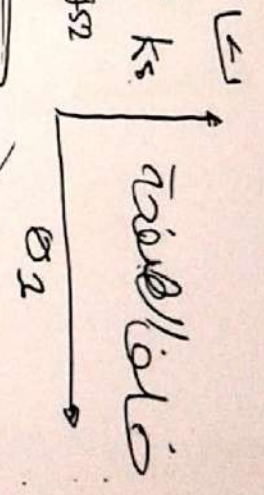
$$\frac{D_f}{B^*} = \frac{3.3}{1.6} = 1.864$$

$$B^* = \frac{2 \times 1.6 \times 2}{1.6 + 2} = 1.77$$

Local Shear Failure  
 $\Rightarrow \phi'' = \tan^{-1} \left( \frac{2}{3} \tan \phi' \right)$

$$= \tan^{-1} \left( \frac{2}{3} \tan 30^\circ \right) = 21^\circ$$

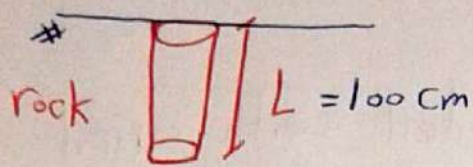
So  $N_c = 15.82$ ,  $N_q = 7.07$ ,  $N_\gamma = 6.2$



Fail 1 & 2

$\sigma = 250 \text{ kPa}$

# Bearing Capacity of Rock :



RQD = Rock Quality Designation

$$= \frac{\sum (\text{all pieces} > 100 \text{ mm})}{\text{Advancement Length}}$$

RQD  $\rightarrow 0 \equiv$  weak

RQD  $\rightarrow 1 \equiv$  excellent

$$q_{ult} = C N_c + q N_q + 0.5 \gamma B \gamma N_\gamma$$

الموقع لم يتم شرحه إلا

في صفحة واحدة 3:

$\phi \Rightarrow$  Rock

$$\rightarrow N_c = 5 \tan^4(45 + \phi/2)$$

$$\rightarrow N_q = \tan^6(45 + \phi/2)$$

$$\rightarrow N_\gamma = N_q + 1$$

# Fully Compensation Footing :

هناك عمق معين يصبح عنه ال Settlement تقريبا صفر ، نقول مرات  
بالإضافة بالابراج العالية بالحفر له حتى نأخذ تأثير الصبوت .  
ويتحقق عندما تكون

$$q_{net} = 0$$

\* Net Bearing Capacity :  $\leftarrow$  صليم

$$q_{net} = q_{ult} - q$$

$$q = \gamma D_f$$

or "gross allowable pressure"  
"سنوات"

\*\* if  $q_{net} = 0 \rightarrow$  Fully compensation footing

$$0 = q_{ult} - q \Rightarrow D_f \gamma = q_{ult}$$

$$\Rightarrow D_f = \frac{q_{ult}}{(A)(\gamma)} \Rightarrow \text{العمق يكون عند الصبوت تقريبا صفر}$$

# ● Foundation Settlement : CH6 , CH7 : السكنة

## ■ Introduction :

\* Foundation settlement must be estimated with great care for building .

\* For other structure such as fill, earthdam, a greater margin of error in settlement can usually be tolerated.

■ problems with soil settlement analysis : "سنوات"

1] Obtaining reliable value of the elastic parameters;  $E_s$

2] Obtaining reliable stress profile from the applied load.

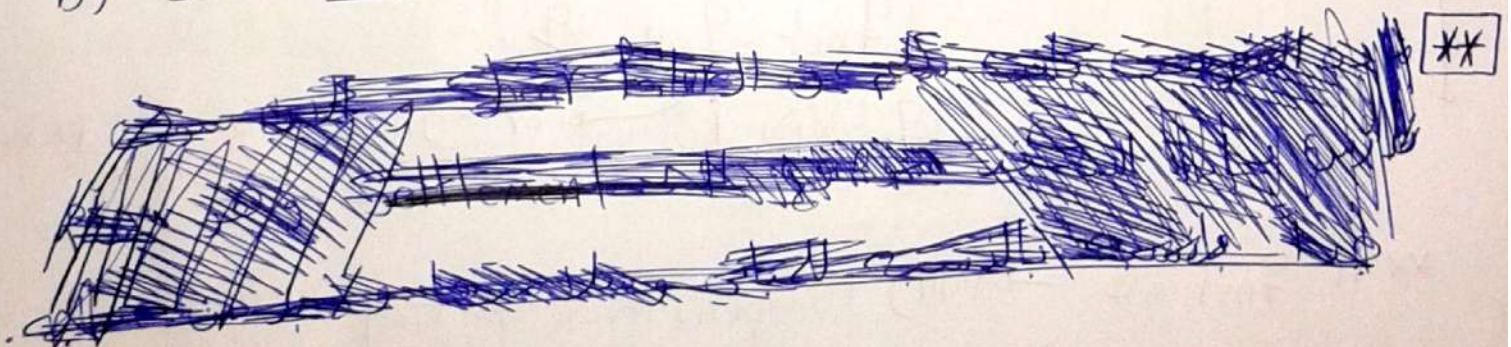
## ■ Type of settlement :

1] Elastic "Immediate" or distortion settlement for (sand, clay).

2] Consolidation settlement only for clay :

a) primary consolidation .

b) secondary consolidation .



# Stress Increments : CH6

\* الضغط المضاف/ الزائد ينتج عند وضع الأساس في التربة نفسها و يحسب مثل السابق

$$\sigma_T = \sigma_0 + \Delta\sigma$$

$\sigma_T$  : Total (final) effective stress

$\sigma_0$  : Initial overburden pressure

العمل الذي قبل وضع الأساس من التربة نفسها و يحسب مثل السابق

$$\sigma_0 = \gamma z$$

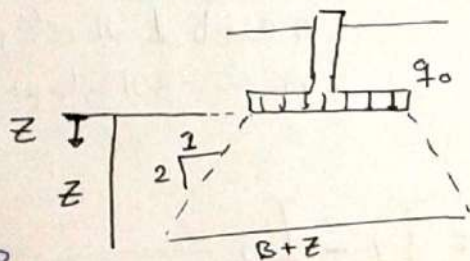
$\Delta\sigma$  : Induced (increment) stress

\*\*\* لحساب  $\Delta\sigma$  هناك طريقتان :

Approximate method [1]

Elastic solution [2]

## Approximate method :



\* Strip Footing

$$\Delta\sigma = \frac{q_0 \times B}{B+z}$$

\* Square

$$\Delta\sigma = \frac{q_0 \times B \times B}{(B+z)(B+z)}$$

$q_0$  : net applied pressure

$z$  : العمق من قاعدة footing للأسفل

\* rectangular

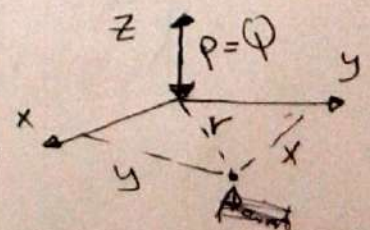
$$\Delta\sigma = \frac{q_0 \times B \times L}{(B+z)(L+z)}$$

## Elastic Solution :

[1] point Load :

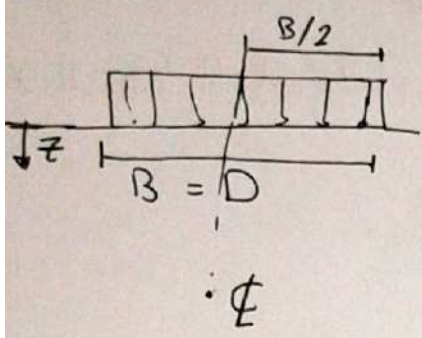
$$\Delta\sigma = \frac{3P}{2\pi z^2 \left[1 + \left(\frac{r}{z}\right)^2\right]^{5/2}}$$

$$r = \sqrt{x^2 + y^2}$$



[2]

2] Circular Loaded Area :  $\Delta \sigma = q_0 I$  I: Influence Factor

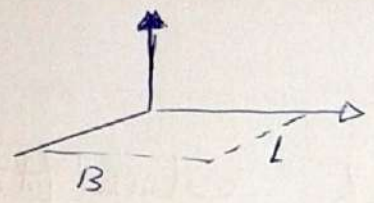


$$I_\phi = 1 - \frac{1}{\left[1 + \left(\frac{B}{2z}\right)^2\right]^{3/2}}$$

Under the center of footing

\* For other point (r, z) use table in book CH6.

3] Stress under corner of load rectangular area :



$$\Delta \sigma = q_0 I$$

\*\* شروط حساب ال I :-

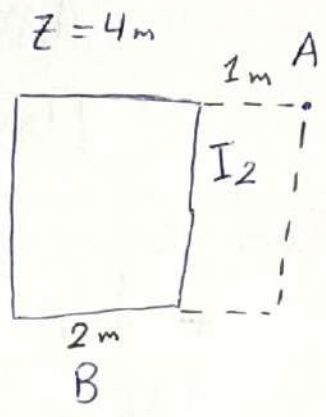
- 1) ان يكون الشكل مستطيل .
- 2) ان تكون النقطة corner

$I_\phi$  للشكل كامل

$$m = \frac{B}{z} = \frac{3}{4}$$

$$n = \frac{L}{z} = \frac{4}{4}$$

I = من جدول بالكتاب



\*\* خطوات الحل :- مثال

- 1) الضلع الاكبر L ← n
- 2) الضلع الاصغر B ← m

← اي تقسيم على ال L تأخذه n  
 و اي تقسيم على ال B ← m

$I_2 \equiv$

$$m = \frac{1}{4} \Rightarrow I_2 = \square$$

$$n = \frac{4}{4}$$

$$I_{total} = I_1 - I_2$$

$$\Delta \sigma = q_0 I_{total} L$$

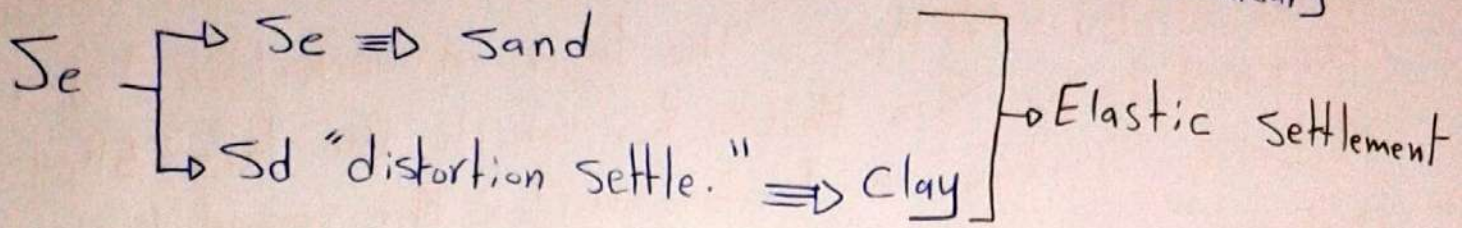
هكذا تكون حسبنا الحل المؤثر من الاساس عند النقطة A .  
 \* راجع الموضع بمادة السوييل

\*\* غالباً اسئلة الامتحان تكون على ال (approximate) methode

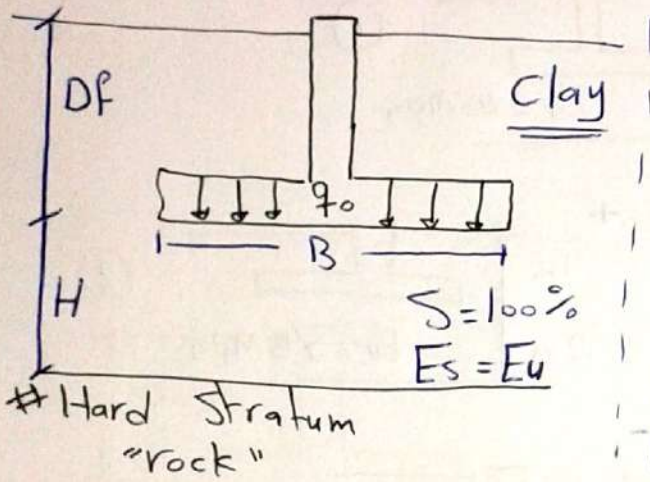
● Settlement :

$$S_T = S_e + S_c + S_s$$

Total                      Primary                      Secondary



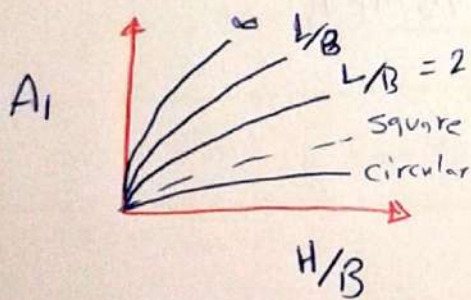
□ Distortion Settlement on saturated clay : متوقع



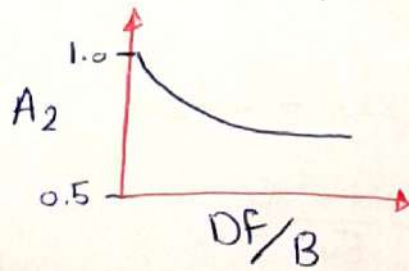
$$S_d = A_1 A_2 \frac{q_0}{E_u} B$$

$q_0$  : net applied pressure  
 $E_u$  : undrained Elastic modulus  
 $B$  : width

$A_1$  : Shape Factor



$A_2$  : Depth Factor : بعمق



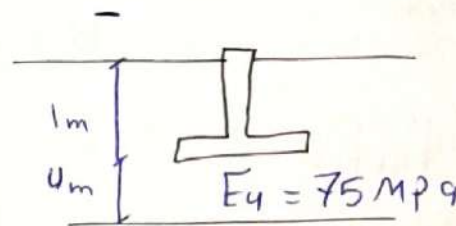
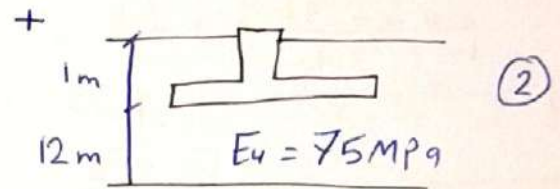
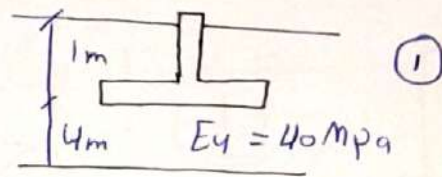
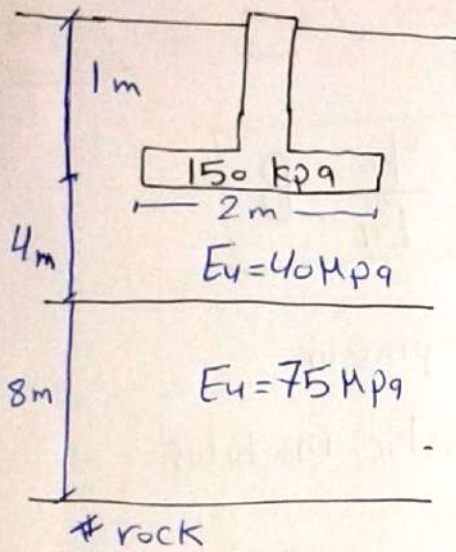
\*\* في حال اعطى  $E_s$  و لا يجاد  $E_u$  نستخدم العلاقة التالية :

$E_u = \beta E_s$   $\Rightarrow \beta$  : جدول في الكتاب يعطى كل حين

$\Rightarrow E_u = \left( \text{[ ]} \right)$  
 $C_u \left( \frac{\alpha R}{\text{[ ]}} \right) \beta \left( \text{[ ]} \right)$

نأخذ الرقعة
على شكل قتره

Ex: A foundation  $4\text{ m} \times 2\text{ m}$ , carrying a net uniform pressure of  $150\text{ kPa}$  is located at a depth of  $1\text{ m}$  in a layer of clay  $5\text{ m}$  thick for which the value of  $E_u = 40\text{ MPa}$ . The layer is underlain by a second layer  $8\text{ m}$  thick for which the  $E_u = 75\text{ MPa}$ . A hard stratum is located under the second layer. Determine the average immediate settlement under load.



Sol:

$$S_d = S_{d1} + S_{d2} - S_{d3}$$

$$\textcircled{1} S_{d1} = A_1 A_2 \frac{q_0}{E_u} B$$

$$A_1 \left( \frac{H}{B} = \frac{4}{2} = 2, \quad L/B = \frac{4}{2} = 2 \right) \xrightarrow{\text{from fig}} A_1 = 0.65$$

$$A_2 \left( \frac{Df}{B} = \frac{1}{2} \right) \xrightarrow{\text{from fig}} A_2 = 0.925$$

$$S_{d1} = (0.65)(0.925) \left( \frac{150}{40 \times 10^3} \right) (2) = \boxed{4.51 \text{ mm}}$$

$$\textcircled{2} S_{d2} = A_1 A_2 \frac{q_0}{E_u} B$$

$$A_1 \left( \frac{H}{B} = \frac{12}{2} = 6, \quad L/B = 2 \right) \xrightarrow{\text{from fig}} A_1 = 0.85$$

**24**



$$A_2 = 0.925$$

$$Sd_2 = (0.85)(0.925) \left( \frac{150}{75 \times 10^3} \right) (2) \times 10^3 = \boxed{3.145 \text{ mm}}$$

③

$$A_1 = 0.65$$

$$A_2 = 0.925$$

$$Sd_3 = (0.65)(0.925) \left( \frac{150}{75 \times 10^3} \right) (2) \times 10^3 = \boxed{2.405 \text{ mm}}$$

$$\therefore Sd = Sd_1 + Sd_2 - Sd_3 = 4.51 + 3.145 - 2.405 = \boxed{5.25 \text{ mm}}$$

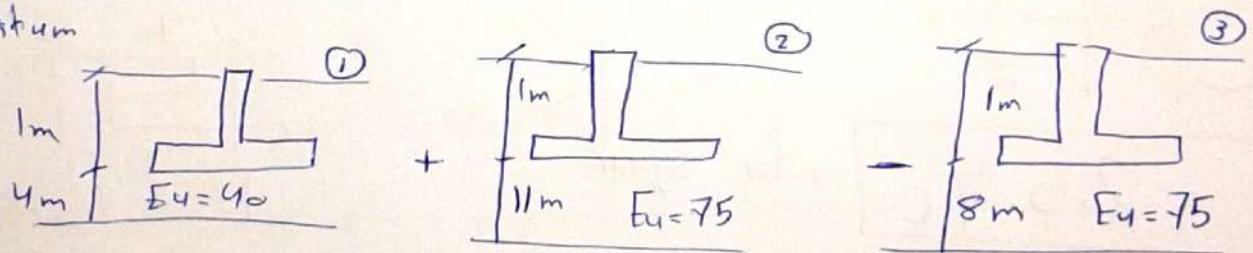
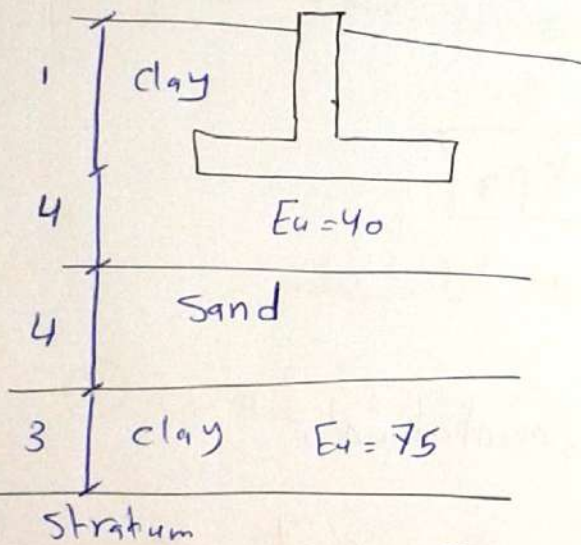
في حال اعطى في السؤال طبقات Clay وبينهم Sand مثلاً :

يقتر انه ما في طبقة sand وبحسب عادي  
لا clay وبتطوع Sd

بجوز بحسب Se sand لا

وبحسب ~~St~~

$$St = Se + Sd$$



$$\Rightarrow Sd = Sd_1 + Sd_2 - Sd_3$$

# Elastic Settlement on Sandy Layer "E<sub>s</sub>"

\* In situ Testing : \* Es له اختبارين للاسفلت هناك \*\*

- ① Standard penetration Test (SPT)
- ② Cone Penetration Test (CPT)

## 1] SPT :

$$N_{60} = \frac{N \eta_H \eta_B \eta_s \eta_R}{60}$$

N : number of blows that the sampler can enter 1 ft.

N<sub>60</sub> : spt N corrected for field procedure .

$\eta_H$  : Hammer efficiency       $\eta_s$  : sample correction

$\eta_B$  : Bore Hole                       $\eta_R$  : rod correction

"سبون"  $\Rightarrow$   $N_{60}$

$$E_s = \alpha (N_{60}) P_a$$

P<sub>a</sub> : atmospheric pressure  $\equiv$  100 kpa

$\alpha$

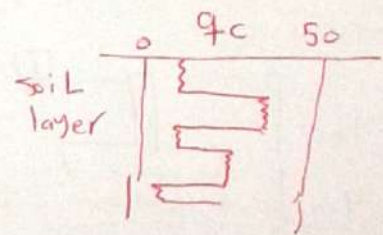
$\rightarrow$ 10	Sand <del>is</del> Clean . $\leftarrow$ ولي
$\rightarrow$ 5	Sand with fine .
$\rightarrow$ 15	Sand with <del>consolidation</del> cementation .

## 2] CPT :

$$E_s = 2.5 q_c \Rightarrow \text{for square}$$

$$E_s = 3.5 q_c \Rightarrow \text{for wall } L/B > 10$$

$$E_s = (1 + 0.4 \log L/B) E_{s \text{ square}} \Rightarrow \text{for rectangular } 1 < L/B < 10$$



$$S_e = C_1 C_2 q_{net} \sum_{i=1}^n \frac{I_{z_i} \Delta z_i}{E_{s_i}}$$

$S_e$  : Elastic settlement on sand layer.

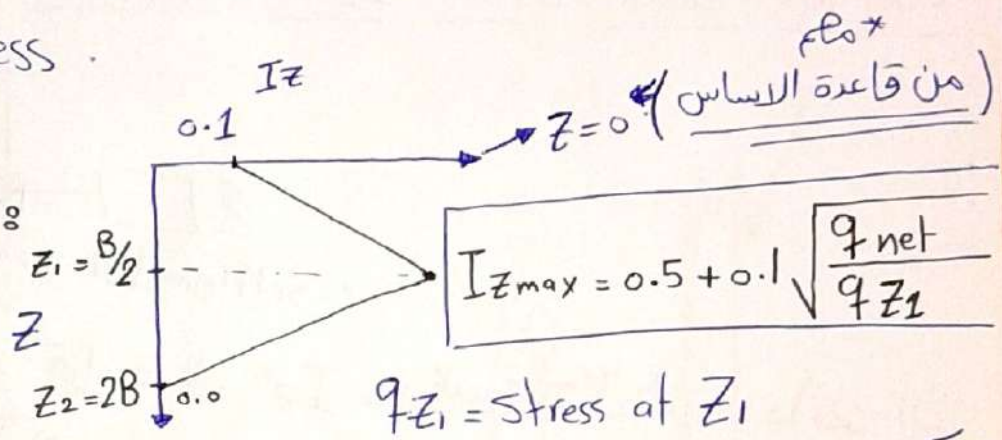
$C_1$  : depth correction =  $1 - 0.5 \frac{q}{q_{net}}$   $\rightarrow D_f \neq \lambda$

$C_2$  : Creep factor =  $1 + 0.2 \text{Log } t/0.1$   $t$ : time since construction

$\Delta z$  : Layer thickness.

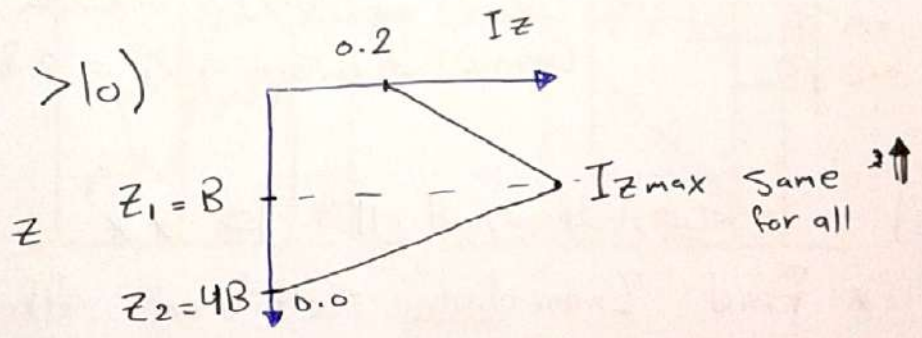
$I_z$  :

① Square :



تذكر ان  $z_1$  مقياسه من نهاية ال footing يعني بينا نصف  $D_f$  على

② wall ( $L/B > 10$ )



③ Rectangular :

\*  $I_z$  at  $z=0 \Rightarrow I_z = 0.1 + 0.0111(L/B - 1) \leq 0.2$

\*  $I_{z_{max}}$  at  $z_1$  :  $\frac{z_1}{B} = 0.5 + 0.0555(L/B - 1) \leq 1$   
Same for all

\*  $I_z = 0$  at  $z_2$  :  $\frac{z_2}{B} = 2 + 0.222(L/B - 1)$

خطوات الحل :-

$$S_e = C_1 C_2 q_{net} \sum \frac{I_z \Delta z_i}{E_s}$$

1. نحسب كل من  $C_1$ ,  $C_2$ ,  $q_{net}$  من القوائين.
2. بحسب ال  $E_s$  لكل طبقة حسب نوع الاضبار المطلوب.
3. برسم رسمة ال  $I_z$  وبعدها علينا حتم  $I_z$  عن  $z=0$   
 $z_1 = \square$   
 $z_2 = \square$

4. نعمل جدول بصتوي على :-  $\frac{I_z \Delta z}{E_s}$

Layer no.	$\Delta z (m)$	$E_s$	$I_z$	$\frac{I_z \Delta z}{E_s}$
1				
2				
...				

5. جوض بقانون  $S_e$  و بوجر ال Settlement.

• ملاحظة مهمة :- عند قراءة ال  $I_z$  من الرسمة لكل طبقة بأخذ ال Avg. للطبقة ، " يعني عند منتصف كل طبقة "

مثلا :-  
 Layer ①  $\Rightarrow 0.5/2 = 0.25 m$   $\Rightarrow$  بوخذ قراءة  $I_z$   
 Layer ②  $\Rightarrow 0.5 + 0.6/2 = 0.8 m$   
 وهكذا

\*\* حل مثال الورقة الخارجية : Sol

\* Find Immediate settlement after 1 year from construction

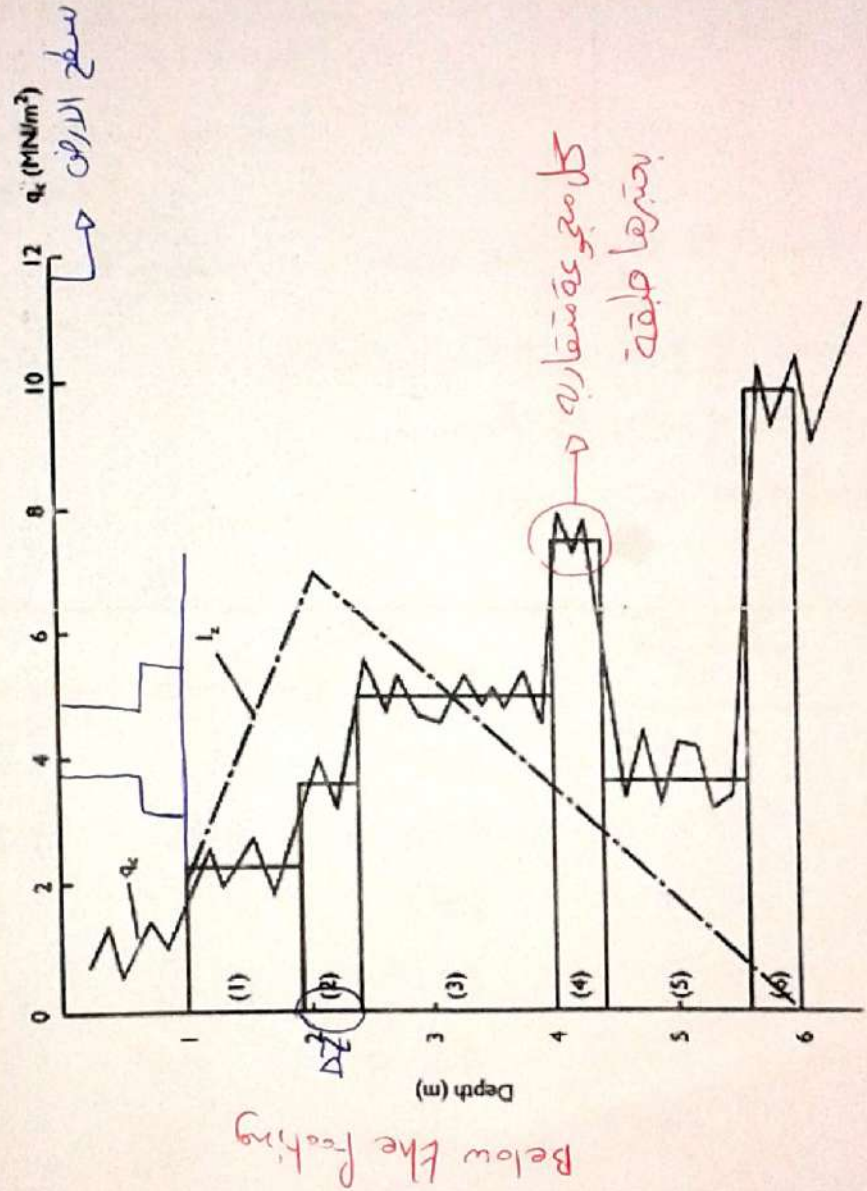
$$C_1 = 1 - 0.5 \left( \frac{q}{q_{net}} \right) = 1 - 0.5 \left( \frac{1 \times 17}{150} \right) = \boxed{0.94}$$

$$C_2 = 1 + 0.2 \log \left( \frac{t}{0.1} \right) = 1 + 0.2 \log \left( \frac{1}{0.1} \right) = \boxed{1.2}$$

$$q_{net} = \boxed{150 \text{ kPa}}$$

# Example

A footing  $2.5 \times 2.5$ m supports a net foundation pressure of  $150 \text{ kN/m}^2$  at a depth of  $1.0$ m in a deep deposit of normally consolidated fine sand of unit weight  $17 \text{ kN/m}^3$ .



$I_z \Rightarrow$  Square :

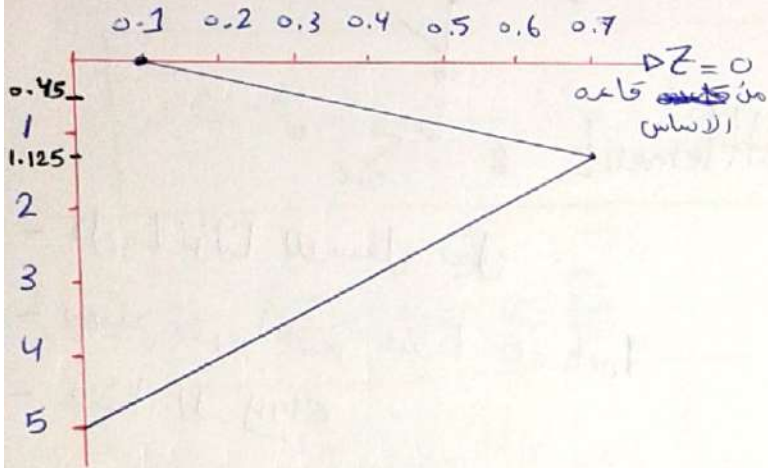
\*  $Z=0 \Rightarrow I_z = 0.1$

\*  $Z_1 = B/2 = 2.5/2 = 1.25 \text{ m} \Rightarrow$  من قاعدة الاساس

$q_{z1} = (17)(1 + 1.25) = 38.25 \text{ Kpa}$

$\Rightarrow I_{z \max} = 0.5 + 0.1 \sqrt{\frac{q_{z1}}{q_{net}}} = 0.5 + 0.1 \sqrt{\frac{38.25}{150}} = 0.698 \Rightarrow 0.7$

\*  $Z_2 = 2B = 5 \text{ m} \Rightarrow I_z = 0$



\*\* لاحظ بالنسبة ال Square فقط يعني footing

الحسابات لعق 2B من اسفل الاساس اي اسي يوجد بها بعمق و ما يدخله بالحسابات .

\* اما ال Wall footing لعق 4B .

Layer no.	$\Delta Z$ (cm)	$q_c$ (mpa)	$E_s = 2.5 q_c$	$I_z$	$\frac{I_z \Delta Z}{E_s}$
1	0.9	2.4	6	0.3	0.045
2	0.45	3.8	9.5	0.6	0.022
3	1.65	5	12.5	0.58	0.0765
4	0.3	7.5	18.75	0.35	0.0056
5	1.25	3.8	9.5	0.22	0.088
6	0.1	10	25	0.04	$2.4 \times 10^{-4}$
					$\Sigma 0.237$

$\therefore S_e = (0.94)(1.2)(150 \times 10^3)(0.237 \times 10^{-6}) = 0.0401 \text{ m} = 40.1 \text{ mm}$

\*\* الطبقات التي تم اخذ قراءان لـ  $I_z$  عندها هي :

Layer 1 =  $0.9/2 = 0.45 \text{ m}$

Layer 2 =  $0.9 + 0.45/2 = 1.125 \text{ m}$

Layer 3 =  $0.9 + 0.45 + 1.65/2 = 2.175 \text{ m}$

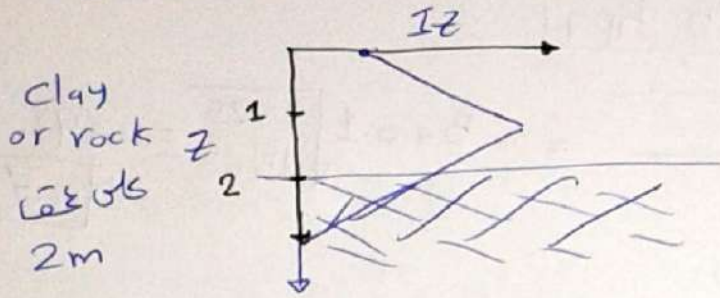
Layer 4 =  $3.15 \text{ m}$

Layer 5 =  $3.925 \text{ m}$

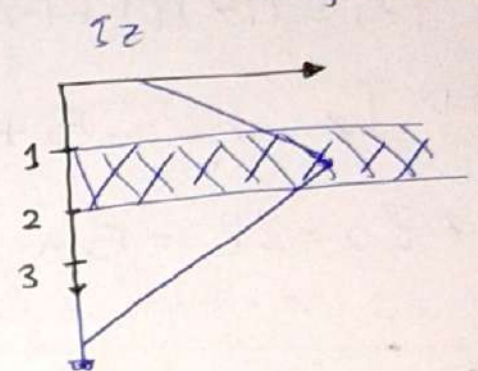
Layer 6 =  $4.6 \text{ m}$

● ملاحظة هامة: في حال كان هناك تفرق في الطبقات، مثلا كان هناك صخر او Clay

← نرسم الرسمة زي كأنها كلها Sand بعدين نحذف الجزء الي فيه Clay or rock



clay or rock على عتبات (1-2)m



● Primary Consolidation Settlement : " $S_c$ "

$$\bar{\sigma}_p = \bar{\sigma}_0 + \Delta \sigma$$

- كلما نزلنا للأسفل يقل

- يصبح تقريبا صفر عندما  $q_{net} = 0$

- فقط لل Clay

$\bar{\sigma}_0$  : Initial effective overburden pressure at middle of Clay Layer.

$\Delta \sigma$  = Induced stress

$$= \frac{1}{6} \left[ \Delta \sigma_{\text{top of clay layer}} + 4 \Delta \sigma_{\text{mid of clay layer}} + \Delta \sigma_{\text{bottom of clay layer}} \right]$$

Cases :

1] Normally Consolidated Clay :  $OCR = 1.0$

$$S_c = \frac{C_c}{1+e_0} H_0 \log \frac{\bar{\sigma}_p}{\bar{\sigma}_0}$$

$$OCR = \frac{\bar{\sigma}_p'}{\bar{\sigma}_0'}$$

لما تكون  $\bar{\sigma}_p < \bar{\sigma}_0$  يعني انه  $\bar{\sigma}_p$  هو ال  $\bar{\sigma}_0$

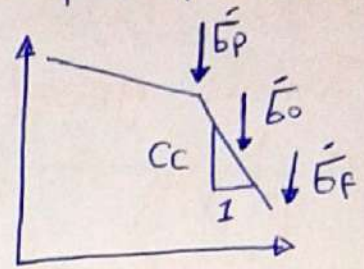
$$\bar{\sigma}_p < \bar{\sigma}_0 < \bar{\sigma}_p'$$

$$\bar{\sigma}_p = \bar{\sigma}_0 < \bar{\sigma}_p'$$

$H_0$  : thickness of clay layer

$\bar{\sigma}_p'$  : preconsolidation pressure "maximum past pressure"

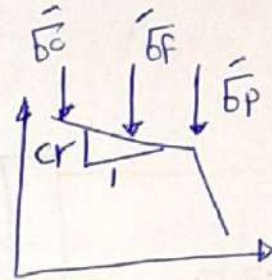
$$\bar{\sigma}_p' < \bar{\sigma}_0 < \bar{\sigma}_f'$$



2 OCR > 1

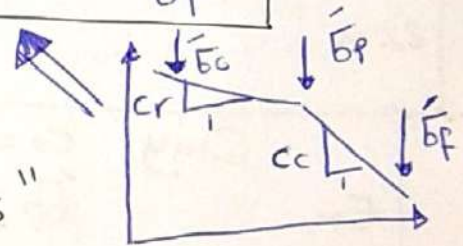
(a)  $\bar{\sigma}_0 < \bar{\sigma}_f' < \bar{\sigma}_p'$

$$S_c = \frac{C_r}{1+e_0} H_0 \log \frac{\bar{\sigma}_f'}{\bar{\sigma}_0}$$

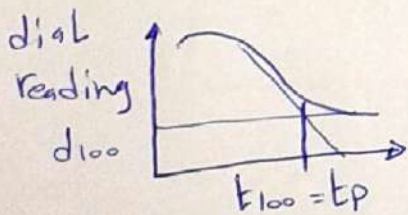


(b)  $\bar{\sigma}_0 < \bar{\sigma}_p' < \bar{\sigma}_f'$

$$S_c = \frac{C_r}{1+e_0} H_0 \log \frac{\bar{\sigma}_p'}{\bar{\sigma}_0} + \frac{C_c}{1+e_0} H_0 \log \frac{\bar{\sigma}_f'}{\bar{\sigma}_p'}$$



Secondary Consolidation Settlement: "S<sub>s</sub>"



$t_{100} = t_p$  = time to end primary consolidation

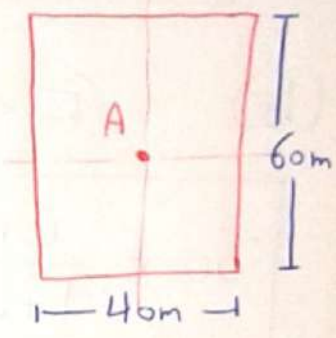
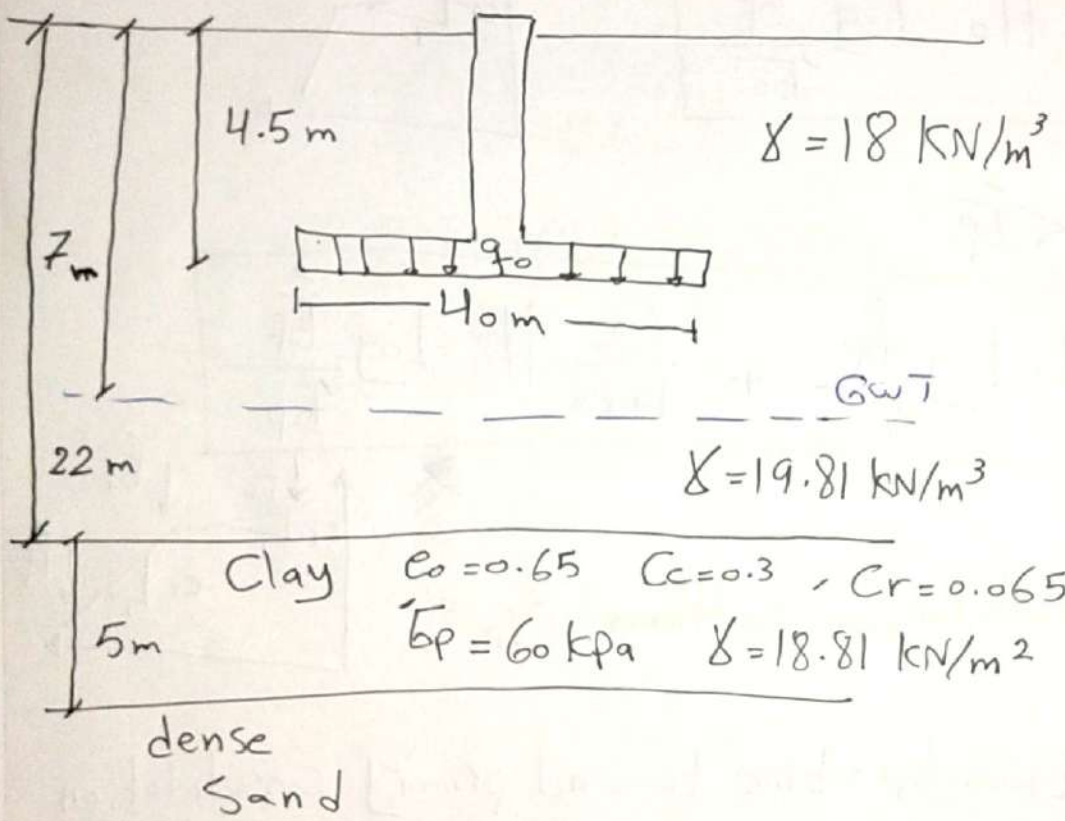
$$\frac{C_\alpha}{C_e} = 0.05 \pm 0.01$$

$$S_s = C_\alpha H_0 \log (t/t_p)$$

$t$  = time after ending primary consolidation



Ex: A Raft Foundation (40 x 60)m carrying a net pressure of 145 kpa is located at depth of 4.5m below the surface in a deposits of dense sandy gravel 22m deep, the water table is at a depth of 7m. Below the sandy gravel is a layer of clay 5m thick which in turn is underlain by dense sand, determine the settlement below the center of Raft ~~the~~?



Sol: Using 2:1 Approximate method  $\Delta \bar{\sigma}$  increment stress

$$\bar{\sigma}_0 = \sum \gamma' z$$

$$= 18(7) + (19.81 - 9.81) * (22 - 7) + (18.81 - 9.81)(2.5)$$

$$= \boxed{298.5 \text{ kpa}}$$

Clay compression   
 "middle"

$$\bar{\sigma}_p = \sigma_0 + \Delta\sigma$$

$$\Delta\sigma = \frac{1}{6} [\Delta\sigma_{top} + 4\Delta\sigma_{mid} + \Delta\sigma_{bottom}]$$

$$\Delta\sigma_{top} = \frac{q_0 B \times L}{(B+z)(L+z)} = \frac{(145)(40)(60)}{(40+22-4.5)(60+22-4.5)} = \boxed{78.09 \text{ kPa}}$$

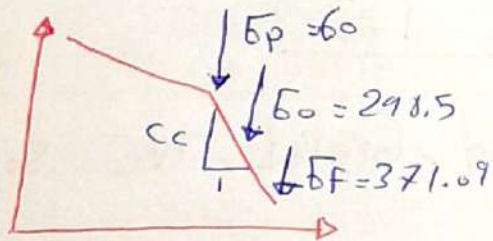
من أسفل الأضلاع إلى  
طبقة clay top

$$\Delta\sigma_{mid} = \frac{(145)(60)(40)}{(40+22-4.5+2.5)(60+22-4.5+2.5)} = \boxed{72.5 \text{ kPa}}$$

$$\Delta\sigma_{bottom} = \frac{(145)(40)(60)}{(40+22-4.5+5)(60+22-4.5+5)} = \boxed{67.5 \text{ kPa}}$$

$$\Delta\sigma = \frac{78.09 + 4(72.5) + 67.5}{6} = \boxed{72.59 \text{ kPa}}$$

$$\bar{\sigma}_p = \sigma_0 + \Delta\sigma = 298.5 + 72.59 = \boxed{371.09 \text{ kPa}}$$



$\bar{\sigma}_p < \bar{\sigma}_0 < \bar{\sigma}_p'$   
(NC clay)  
Case (I)

$$S_c = \frac{c_c}{1+e_0} \frac{H_0}{\sigma_0} \log \frac{\bar{\sigma}_p}{\sigma_0}$$

لطبقة clay

$$= \frac{0.3}{1+0.65} (5) \log \left( \frac{371.09}{298.5} \right) = 0.0859 \text{ m} = \boxed{85.9 \text{ mm}}$$

#

لو طلب ال Settlement عند نقطة اخرى غير ال center

نستخدم elastic method ،  $\Delta\sigma = q_0 I_c$

" مادة رطوبية "

# ■ Lateral Earth pressure : CH 12

\* Geotechnical application : retaining wall

\*\* سوف نقرأ بحساب (Lateral earth pressure and force) الذي يؤثر على الـ wall حتى نتقن ان يكون آمن ضد excessive lateral movement

\*\* 3 Cases :

1 Earth pressure at rest  
\* no strain (no deformation)

\*  $K$  ~~with~~ will be  $K_0$  at rest

$$K_0 = \frac{\bar{\sigma}_h}{\bar{\sigma}_v}$$

Coefficient of Lateral earth pressure

$$K = \frac{\bar{\sigma}_h}{\bar{\sigma}_v} \begin{matrix} \text{horizontal} \\ \text{vertical} \end{matrix}$$

\*  $K_0$  from elastic theory :  $K_0 = \frac{\nu}{1-\nu}$   $\nu$  : poissions ratio

\*  $K_0$  for Granular soil " sand, Gravel, NC soil "

$$K_0 = 1 - \sin \phi'$$

\*\* For undrained soil " $\phi = 0$ "  $K_0 = 1$

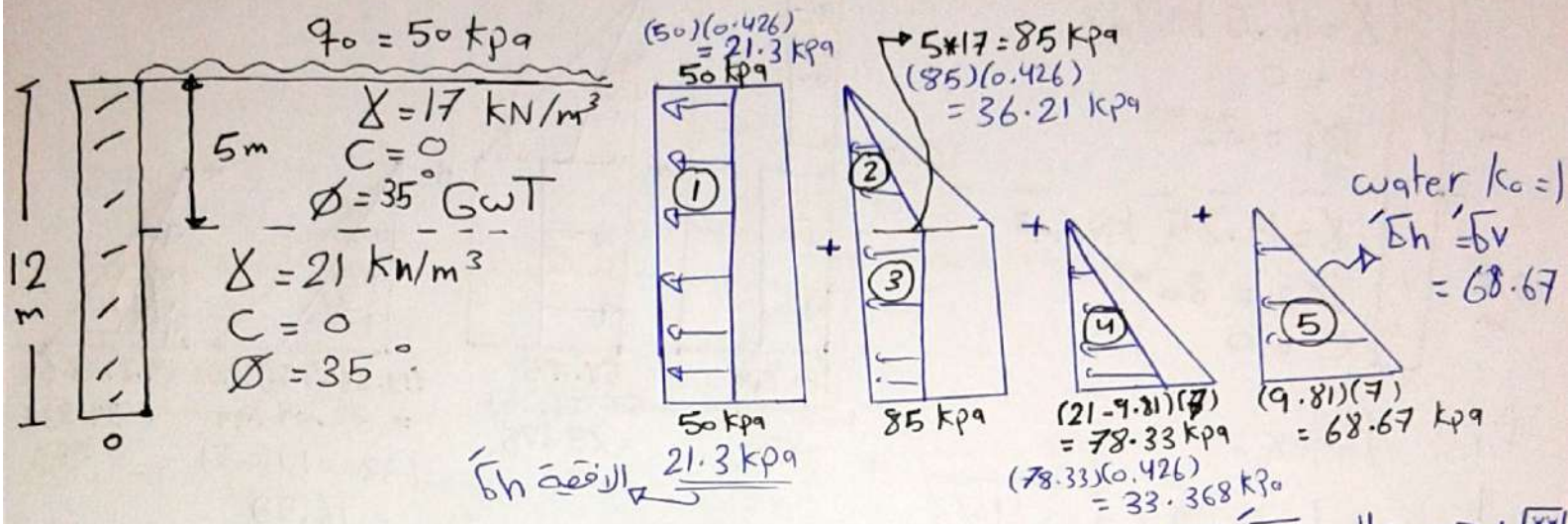
\* For over consolidated soil :

$$K_0 = (1 - \sin \phi') (OCR)^{\sin \phi'}$$

\*\*  $K_0$  for water = 1

Ex: if the wall is prevented from movement at rest

Determin the total force acting on the wall and Line of action of the total force?



بجسب ال  $\bar{b}_v$  القاص من كل طبقة بعين بجول ال  $\bar{b}_h$  عن طريق  $k_o$  من  $\bar{b}_v$  يكون ال  $\bar{b}_h$  ال  $\bar{b}_v$  Load  $\text{KN/m}$

$\bar{b}_v \rightarrow \bar{b}_h$  use  $k_o$

$$k_o = 1 - \sin \phi = 1 - \sin(35) = 0.426$$

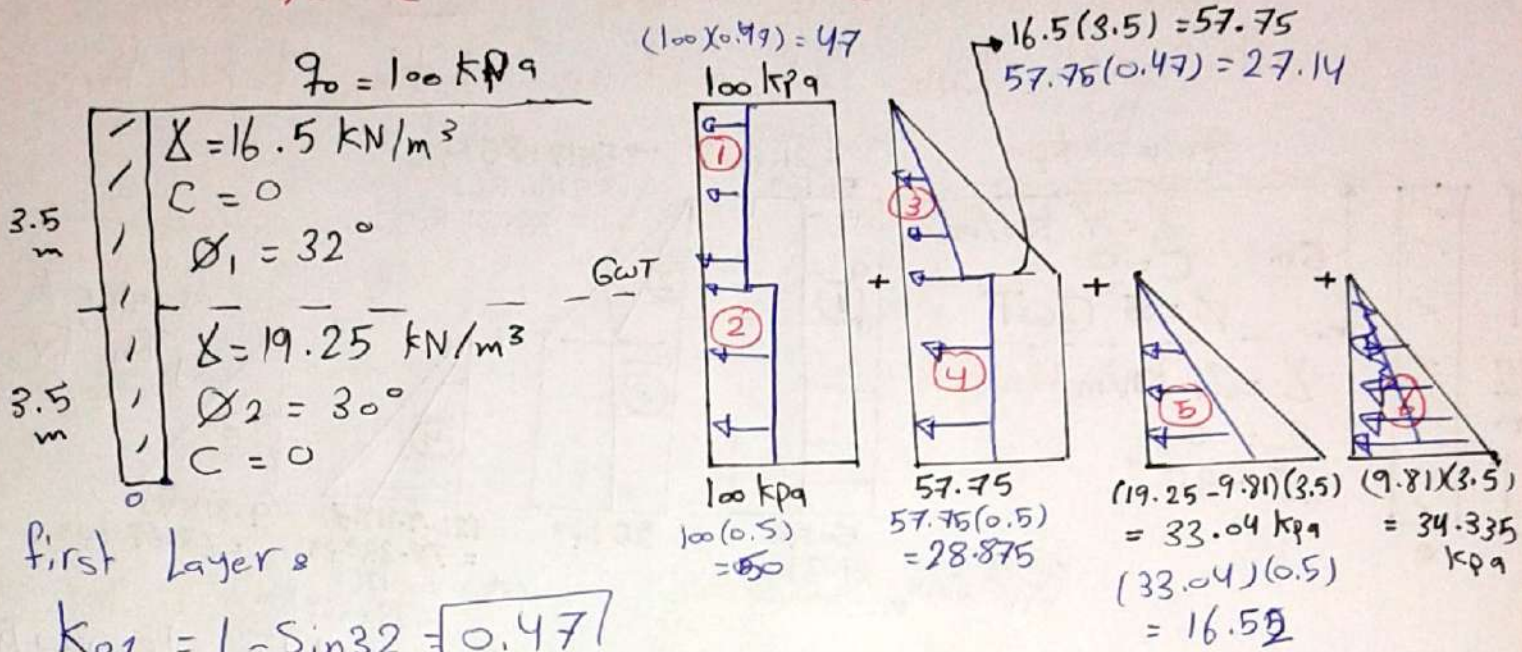
بقسم ال  $\bar{b}_h$  ال  $\bar{b}_v$  في كل  $\text{Seg}$  وكل  $\text{Seg}$  عبارة عن  $\bar{b}_h$  بقدر احسب مساحته و ال center ال

Seg #	Area of Seg $\text{m}^2$	Force $\text{KN/m}$	Arm (m) $X_i$	$\phi_i \times X_i$
1	$12 \times 21.3 = 255.6$	$21.3 \times 12 = 255.6$	$12/2 = 6$	$1533.6$
2	$\frac{1}{2} (21.3 + 85) \times 5 = 90.525$	$\frac{1}{2} (21.3 + 85) \times 5 = 90.525$	$7 + 5/3 = 8.67$	$784.506$
3	$\frac{1}{2} (85 + 0) \times 7 = 297.5$	$36.21 \times 7 = 253.4$	$7/2 = 3.5$	$886.9$
4	$\frac{1}{2} (0 + 78.33) \times 7 = 273.275$	$\frac{1}{2} \times 33.368 \times 7 = 116.788$	$7/3 = 2.33$	$272.4$
5	$\frac{1}{2} (78.33 + 0) \times 7 = 273.275$	$\frac{1}{2} \times 7 \times 68.67 = 240.345$	$7/3 = 2.33$	$560.805$
$\Sigma 956.62 \text{ KN/m}$ ①				$\Sigma 4038.21$

②  $\bar{X} = \frac{\Sigma \rho_i X_i}{\Sigma \rho_i} = \frac{4038.21}{956.62} = 4.22 \text{ m}$

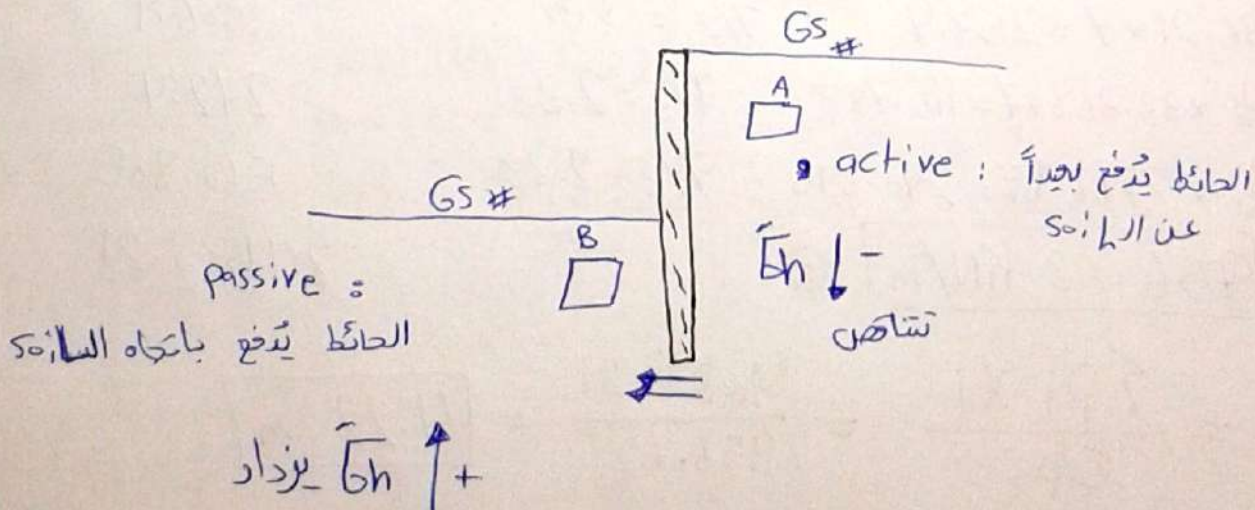
Ex: Same the past example,

الاختلاف في حدود تغير في الطبقات، الزاوية



seg #	$\phi_i / m$	arm $X_i$	$\phi_i \cdot X_i$
1	$47 \times 3.5 = 164.5$	5.25	863.625
2	$50(3.5) = 175$	1.75	306.25
3	$0.5(27.14)(3.5) = 47.5$	4.67	221.825
4	$28.875(3.5) = 101.1$	1.75	176.925
5	$0.5(16.52)(3.5) = 28.91$	1.167	33.74
6	$0.5(34.335)(3.5) = 60.08$	1.167	70.11
	$\Sigma 577.09$		$\Sigma 1672.48$

Cases 2 & 3:



## 2] Active Case "A"

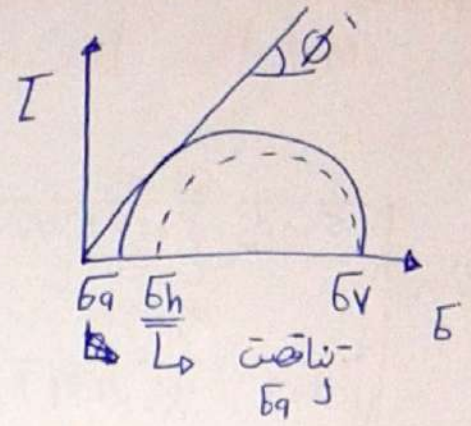
\* For granular soil "C = 0"

$$\sin \phi' = \frac{\bar{\sigma}_v - \bar{\sigma}_a}{\bar{\sigma}_v + \bar{\sigma}_a}$$

$$\bar{\sigma}_a = \frac{1 - \sin \phi'}{1 + \sin \phi'} \bar{\sigma}_v \Rightarrow \bar{\sigma}_a = K_a \bar{\sigma}_v$$

↳ in case "active"

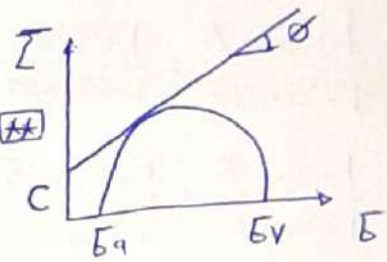
$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi} = \tan^2 \left( 45 - \frac{\phi}{2} \right)$$



\* For OC clay "C = □"

$$\bar{\sigma}_a = K_a \bar{\sigma}_v - 2C \sqrt{K_a}$$

↳ Cohesion



## 3] passive Case "B"

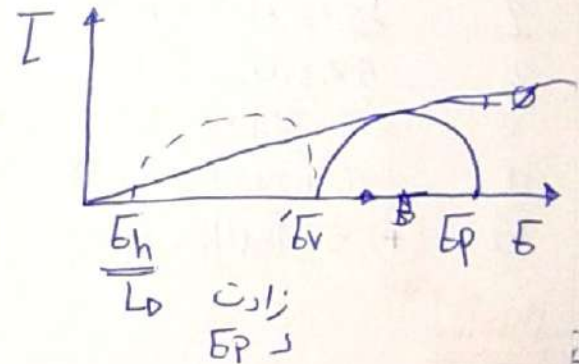
\* For granular soil "C = 0"

$$\sin \phi = \frac{\bar{\sigma}_p - \bar{\sigma}_v}{\bar{\sigma}_p + \bar{\sigma}_v}$$

$$\bar{\sigma}_p = \frac{1 + \sin \phi}{1 - \sin \phi} \bar{\sigma}_v \Rightarrow \bar{\sigma}_p = K_p \bar{\sigma}_v$$

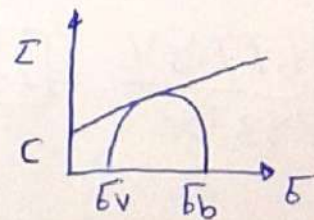
↳ in case passive

$$K_p = \frac{1 + \sin \phi}{1 - \sin \phi} = \tan^2 \left( 45 + \frac{\phi}{2} \right)$$



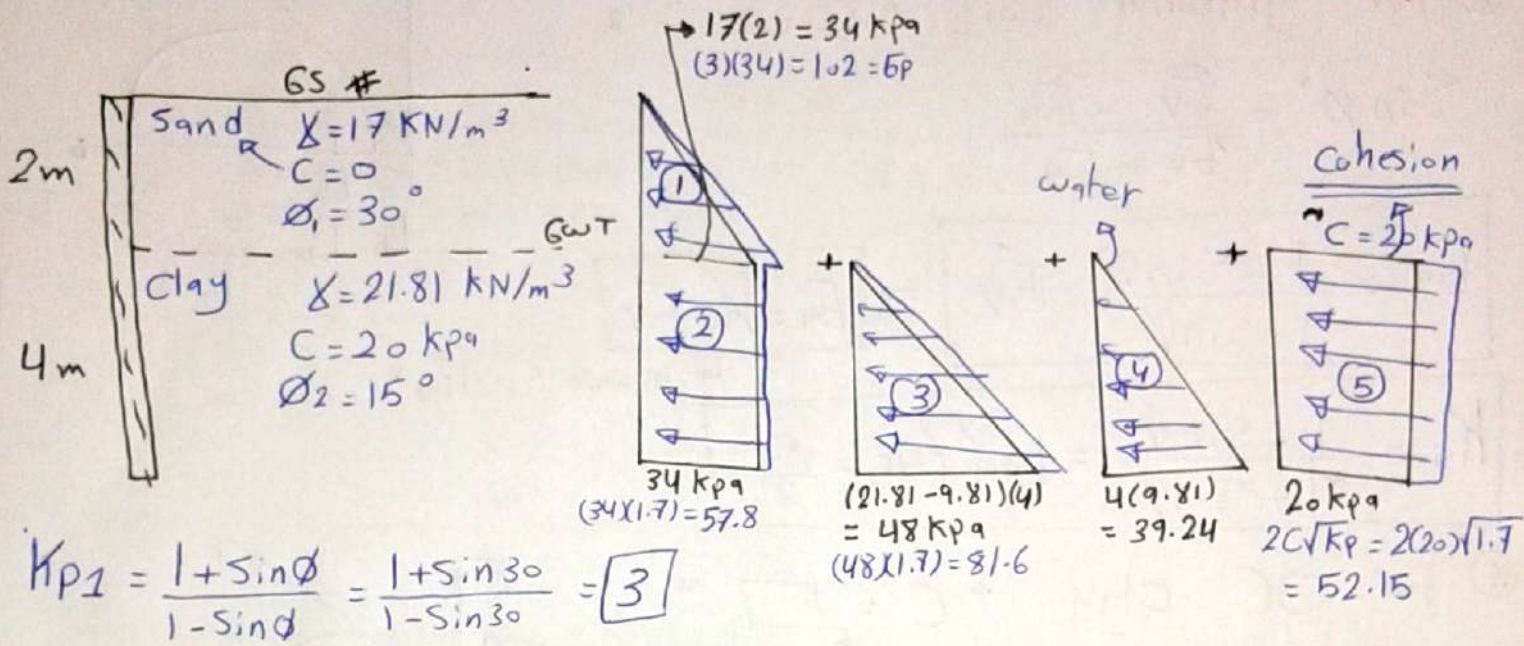
\* For OC clay "C = □"

$$\bar{\sigma}_p = K_p \bar{\sigma}_v + 2C \sqrt{K_p}$$



$$K_a < K_0 < K_b, \quad K_a = \frac{1}{K_p}$$

Ex: Determine the total passive force/m of the wall and the location of Line action of total force?



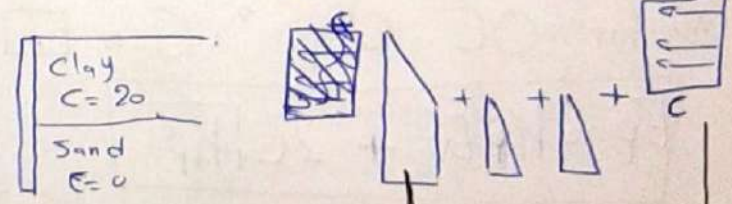
Seg #	$P_{pi}/m$ "kN/m"	$X_i$ (m)	$P_{pi} \times X_i$
1	$\frac{1}{2} \times 2 \times 102 = 102$	4.67	476
2	$57.8(4) = 231.2$	4/2	462.4
3	$0.5 \times 81.6 \times 4 = 163.2$	4/3	217.6
4	$\frac{1}{2} (39.24 \times 4) = 78.48$	4/3	104.64
5	$52.15(4) = 208.6$	4/2	417.2

$C = 20 \equiv \delta v$   
 $2C\sqrt{K_p} \equiv \delta h$

Passive

$P_p = \Sigma = 783.5 \text{ kN/m}$   
 $\bar{X} = \frac{1677.84}{783.5} = 2.14 \text{ m}$

بالنسبة لل cohesion فهي خاصة متعلقة بكل طبقة ~~فقط~~ فقط تكون بالطبقة الواحدة مثلا



لا حظ فقط موجودة بالطبقة العليا لا تنتقل للأسفل  
 على خلاف ال "stress"  $\sigma$  فهو ينتقل

### Example 7.4

Consider a rectangular foundation  $2\text{ m} \times 4\text{ m}$  in plan at a depth of  $1.2\text{ m}$  in a sand deposit, as shown in Figure 7.11a. Given:  $\gamma = 17.5\text{ kN/m}^3$ ;  $\bar{q} = 145\text{ kN/m}^2$ , and the following approximated variation of  $q_c$  with  $z$ :  $t = 10\text{ year}$

$z\text{ (m)}$	$q_c\text{ (kN/m}^2\text{)}$
0-0.5	2250
0.5-2.5	3430
2.5-6.0	2950

$$q_{net} = \bar{q} - q$$

↳ DFx

Estimate the elastic settlement of the foundation using the strain influence factor method.

$$q_{net} = \bar{q} - q = 145 - 17.5(1.2) = \boxed{124\text{ kN/m}^2}$$

$$S_e = C_1 C_2 q_{net} \sum_{i=1}^n \frac{I_{z_i} \Delta z_i}{E_{s_i}}$$

$$C_1 = 1 - 0.5 \frac{q}{q_{net}} = 1 - 0.5 \left( \frac{21}{124} \right) = \boxed{0.93}$$

$$C_2 = 1 + 0.2 \log t/0.1 = 1 + 0.2 \log 10/0.1 = \boxed{1.4}$$

\*\* معلومات لرسم رسيد ال  $I_z$

$$z=0 \rightarrow I_z = 0.1 + 0.0111 \left( \frac{L}{B} - 1 \right) = 0.1 + 0.0111 \left( \frac{4}{2} - 1 \right) = \boxed{0.1111}$$

$$\frac{z_1}{B} = 0.5 + 0.0555 \left( \frac{L}{B} - 1 \right) \leq 1 \Rightarrow \frac{z_1}{2} = 0.5 + 0.0555(2-1)$$

$$\Rightarrow \frac{z_1}{2} = 0.5555 < 1 \Rightarrow \boxed{z_1 = 1.11\text{ m}}$$

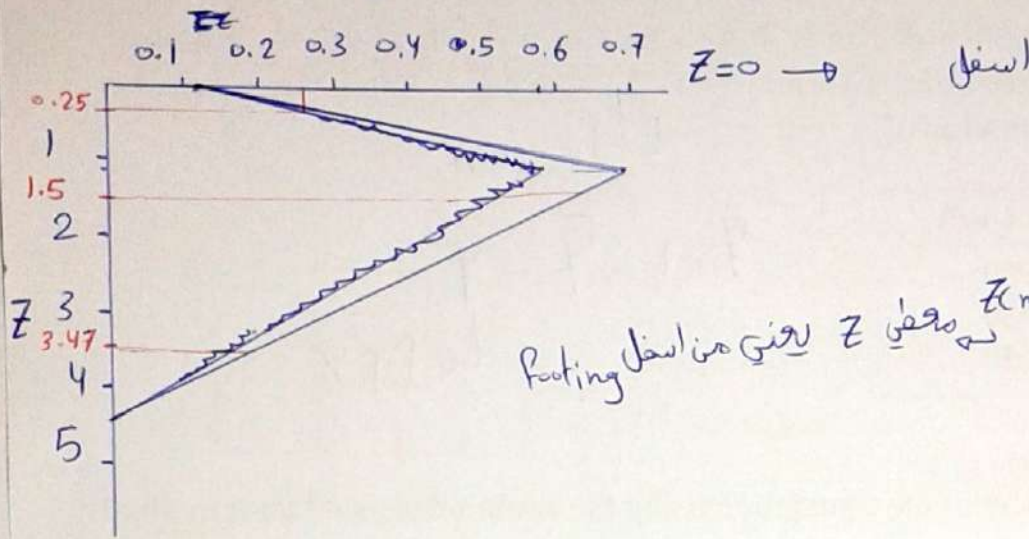
$$q_{z_1} = (1.2 + 1.11)(17.5) = \boxed{40.425\text{ kPa}}$$

$$I_{z_{max}} @ z_1 = 0.5 + 0.1 \sqrt{\frac{124}{40.425}} = \boxed{0.68}$$

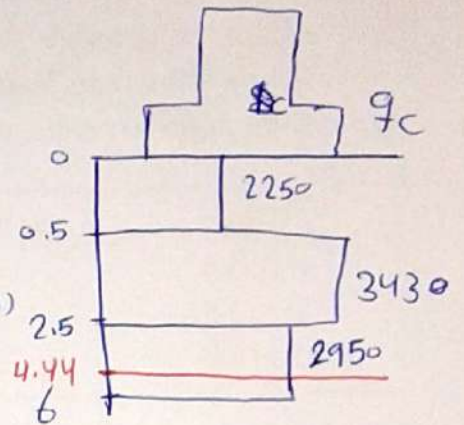


$$I_z = 0 \text{ @ } \frac{z_2}{B} = 2 + 0.222 \left( \frac{L}{B} - 1 \right)$$

$$\Rightarrow \frac{z_2}{2} = 2 + 0.222(2 - 1) \Rightarrow z_2 = 4.44 \text{ m}$$



Footing  $I_z$  in  $z$  (m)



$$E_s = (1 + 0.4 \log \frac{L}{B}) E_{s94} = (1 + 0.4 \log \frac{L}{B}) (2.5 q_c)$$

$$E_{s1} = (1 + 0.4 \log \frac{1}{2}) (2.5 * 2250) = 6302.32$$

$$E_{s2} = (1 + 0.4 \log \frac{1}{2}) (2.5 * 3430) = 9607.53$$

$$E_{s3} = (1 + 0.4 \log \frac{1}{2}) (2.5 * 2950) = 8263.04$$

Layer no	$\Delta z$	$E_s$	$I_z$	$\frac{I_z \Delta z}{E_s}$
1	0.5	6302.32	0.26	$2.06 \times 10^{-5}$
2	2	9607.53	0.64	$1.33 \times 10^{-4}$
3	1.94	8263.04	0.195	$4.58 \times 10^{-5}$
				$\sum 1.994 \times 10^{-4}$

$$S_e = 0.93 (1.4) (124 \times 10^3) (1.994 \times 10^{-4}) = 32.19 \text{ mm}$$

7.10 A continuous foundation on a deposit of sand layer is shown in Figure P7.10 along with the variation of the cone penetration resistance  $q_c$ . Assuming  $\gamma = 18 \text{ kN/m}^3$  and creep is at the end of ten years after construction, calculate the elastic settlement of the foundation using the strain influence factor method. Use Eqs. (7.20) and (7.26).

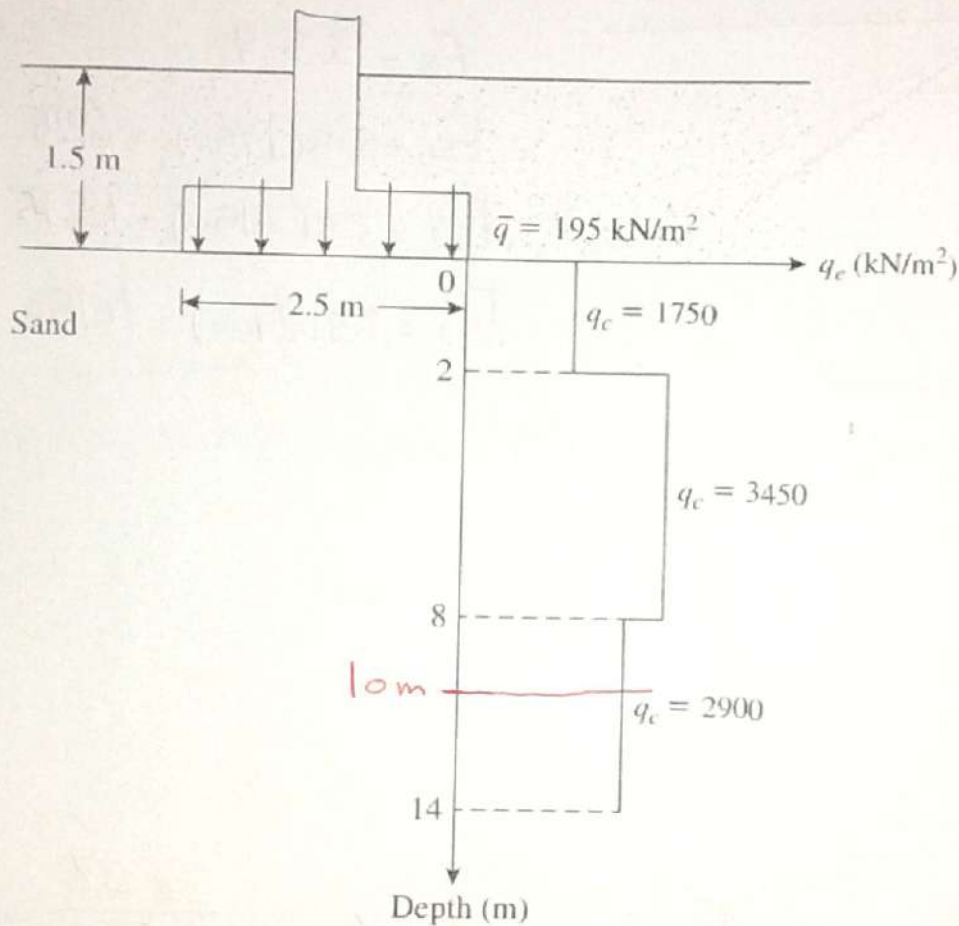


Figure P7.10

$$q_{\text{net}} = \bar{q} - \gamma = 195 - (18)(1.5) = \boxed{168 \text{ kPa}}$$

$$C_1 = 1 - 0.5 \left( \frac{27}{195} \right) = \boxed{0.93}$$

$$C_2 = 1 + 0.2 \log \frac{10}{0.1} = \boxed{1.4}$$

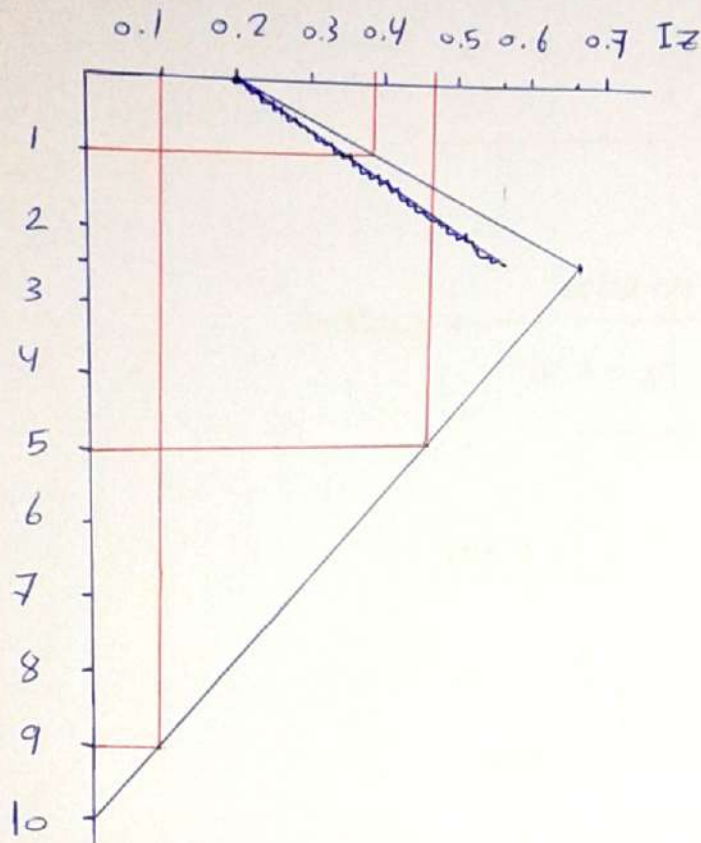
$$z=0 \rightarrow I_z = 0.2 \quad \text{و } I_z \text{ من الرسم الرسمة } \boxed{**}$$

$$z_1 = \cancel{z} B = 2.5 \text{ m}$$

$$q_{z_1} = (2.5 + 1.5)(18) = \boxed{72 \text{ kPa}}$$

$$I_{z_{\max}} = 0.5 + 0.1 \sqrt{\frac{195}{72}} = \boxed{0.66}$$

$$z_2 = 4B = 4(2.5) = \boxed{10 \text{ m}} \rightarrow \boxed{I_{z_2} = 0}$$



$$E_s = 3.5 q_c$$

$$E_{s1} = 3.5(1750) = 6125$$

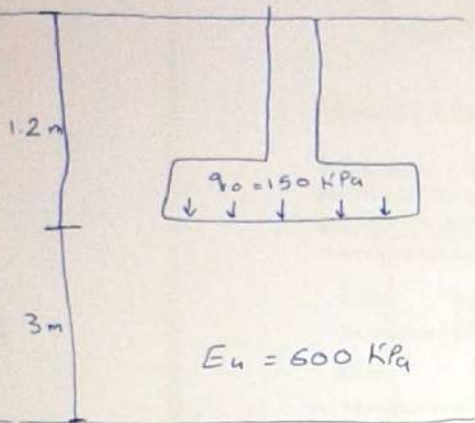
$$E_{s2} = 3.5(3450) = 12075$$

$$E_{s3} = 3.5(2900) = 10150$$

Layer no	$\Delta z$	$E_s$	$I_z$	$\frac{I_z \Delta z}{E_s}$
1	2	6125	0.39	$1.27 \times 10^{-4}$
2	6	12075	0.47	$2.34 \times 10^{-4}$
3	2	10150	0.1	$1.97 \times 10^{-5}$
				$\Sigma 3.81 \times 10^{-4}$

$$S_e = 0.93(1.4)(168 \times 10^3)(3.81 \times 10^{-4}) = \boxed{83.34 \text{ mm}}$$

7.1 Refer to Figure 7.1. A flexible foundation measuring  $1.5 \text{ m} \times 3 \text{ m}$  is supported in a saturated clay. Given:  $D_f = 1.2 \text{ m}$ ,  $H = 3 \text{ m}$ ,  $E_s$  (clay) =  $600 \text{ kN/m}^2$ , and  $q_o = 150 \text{ kN/m}^2$ . Determine the average elastic settlement of the foundation. Use Eq. (7.1)



Sol.

$$s_d = A_1 A_2 \frac{q_o}{E_u} \times B$$

$$* A_1 \rightarrow \left( H/B = \frac{3}{1.5} = 2 < L/B = \frac{3}{1.5} = 2 \right) \rightarrow A_1 = \underline{0.65}$$

$$* A_2 \rightarrow \left( D_f/B = \frac{1.2}{1.5} = 0.8 \right) \rightarrow A_2 = \underline{0.935}$$

$$s_d = 0.65 \times 0.935 \times \frac{150 \times 10^3}{600 \times 10^3} \times 1.5 = 0.228 \text{ m} = \boxed{228 \text{ mm}}$$

40 min

22-5

Student Name: Abdulaziz Z. Al-Hattamleh Student Number: 1438854  
 Student Section: 2 Student New Serial Number: 4

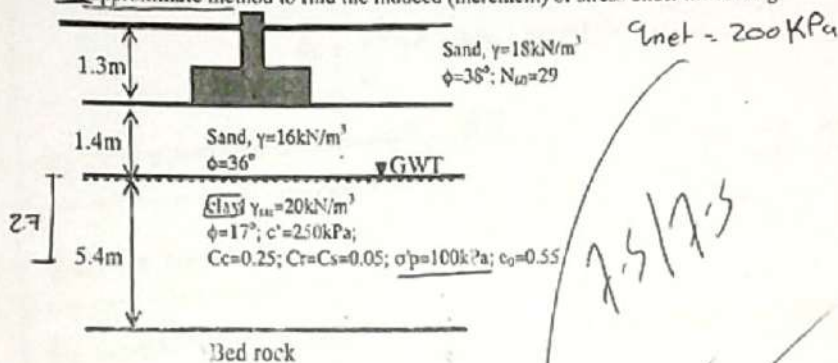


Hashemite University Second Exam  
 Faculty of Engineering Wed: 30/11/2016  
 Department of Civil Engineering Attempts All Problems  
 Foundation Engineering (0401435) Write Only in the designated space  
 Instructor: Dr. Omar Al-Hattamleh

Note all calculation are made to nearest 2 significant digits

Problem # 1 (7.5 points)

A rectangular footing (1.6m x 2.0m) founded on soil profile shown. The footing was carried a net uniform pressure of 200 kPa. Determine, only, the primary consolidation settlement due to footing loading? Hint: Use 2:1 approximate method to find the induced (increment) of stress under the footing.



$$\sigma'_1 = \bar{\sigma}_1 + \Delta \sigma$$

$$\sigma'_0 = 18 \times 1.3 + 16 \times 1.4 + 2.7 \times (20 - 9.81) = 73.31 \text{ kPa}$$

$$OCR = \frac{100}{73.1} > 1$$

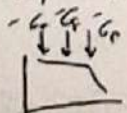
$$\sigma'_{top} = \frac{q_0 \times B \times L}{(B+z)(L+z)} = \frac{200 \times 1.6 \times 2}{(1.6+1.4)(2+1.4)} = 62.75 \text{ kPa}$$

$$\sigma'_{mid} = \frac{200 \times 1.6 \times 2}{(1.6+4.1)(2+4.1)} = 18.41 \text{ kPa}$$

$$\sigma'_{bot} = \frac{200 \times 1.6 \times 2}{(1.6+6.8)(2+6.8)} = 8.66 \text{ kPa}$$

$$\Delta \bar{\sigma} = \frac{1}{6} (8.66 + 4 \times 18.41 + 62.75) = 24.18 \text{ kPa}$$

$$\sigma'_f = 73.31 + 24.18 = 97.5 \text{ kPa}$$



$$S_c = \frac{C_r}{1+e_0} \times H_0 \log \frac{\sigma'_f}{\sigma'_0} = \frac{0.05}{1.55} \times 5.4 \times \log \frac{97.5}{73.31} = 0.0216 \text{ m} \approx 21.6 \text{ mm}$$

1/3

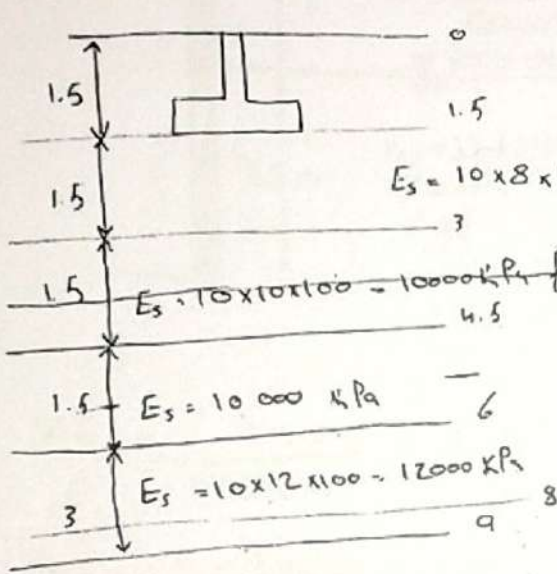
Student Name: Abus alhe Student Number: 1438854  
 Student Section: 2 Student New Serial Number: 4

Problem # 2 (7.5 points)

Consider a square foundation  $2\text{ m} \times 2\text{ m}$  in plan at a depth of  $1.5\text{ m}$  in a clean sand deposit, given:  
 $\gamma = 16\text{ kN/m}^3$  gross allowable load  $150\text{ kPa}$ . The value of  $N_{60}$  with depth given in the table below:

Depth (m)	0.0-1.50	1.5-3.0	3.0-4.50	4.5-6.0	6.0-9.0	9.00
$N_{60}$	6	8	10	10	12	50

Estimate the elastic settlement of the foundation using the strain influence factor method after 5 years?



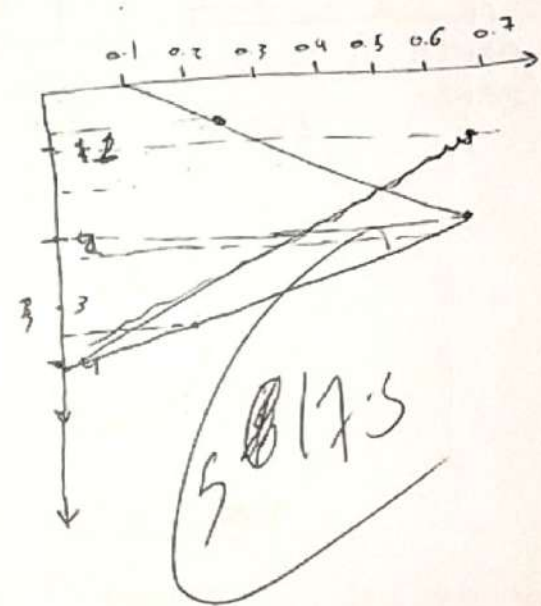
$4B = 8\text{ m}$   
 $E_s = \alpha \times N_{60} \times P_a$

$E_s = 10 \times 8 \times 100 = 8000\text{ kPa}$

$E_s = 10 \times 10 \times 100 = 10000\text{ kPa}$

$E_s = 10000\text{ kPa}$

$E_s = 10 \times 12 \times 100 = 12000\text{ kPa}$



$c_1 = 1 - 0.5 \times \frac{1.5 \times 16}{150} = 0.92$

$c_2 = 1 + 0.2 \log \frac{E_s}{0.1} = 1.34$

$z = z_0 \rightarrow I_z = 0.1$

$z_1 = 2 \rightarrow I_z = 0.5 + 0.1 \sqrt{\frac{150}{E_s \times (z + 1.5) / 16}} = 0.66$

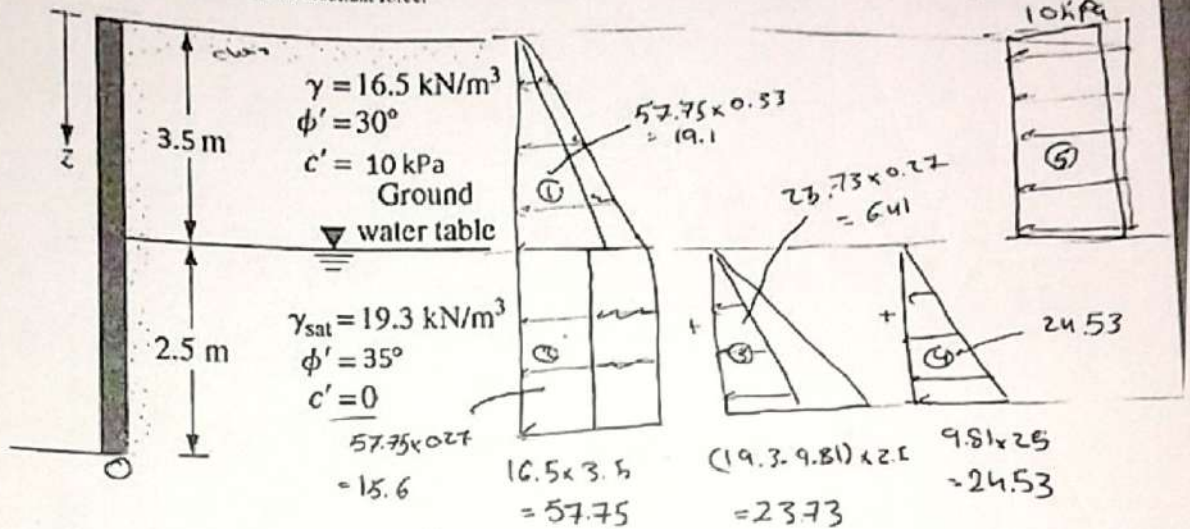
seg	$\Delta z$	$E_s$	$I_z$	$\frac{\Delta z I_z}{E_s}$
1	1.5	8000	0.25	$4.69 \times 10^{-5}$
2	1.5	10000	0.6	$9.2 \times 10^{-5}$
3	1	10000	0.2	$15.7 \times 10^{-5}$

$z_2 = 4$

$S_e = 0.92 \times 1.34 \times 150 \times 10^3 \times 15.7 \times 10^{-5} \times 10^{-3} = 0.629$   
 $\boxed{= 29\text{ mm}}$

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 Student Section: 7 Student New Serial Number: 4

Problem # 3 (10 points)  
 For the retaining wall shown in Figure below, determine the lateral earth force in active state per unit length of the wall.  
 Also determine the location of the resultant force.



$$K_{a1} = \frac{1 - \sin 30^\circ}{1 + \sin 30^\circ} = 0.33$$

$$K_{a2} = \frac{1 - \sin 35^\circ}{1 + \sin 35^\circ} = 0.27$$

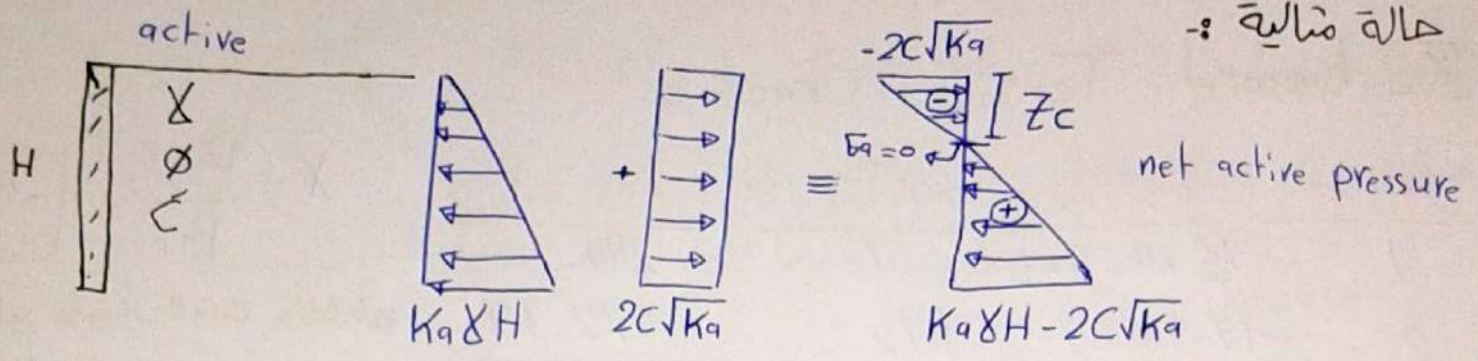


No	$P_i$ (kPa)	$X_i$	$P_i \times X_i$
1	$19.1 \times 3.5 \times 0.5 = 33.43$	$2.5 + \frac{3.5}{3}$	122.55
2	$15.6 \times 2.5 = 39$	1.25	48.75
3	$0.5 \times 6.41 \times 2.5 = 8.1$	$2.5/3$	6.75
4	$24.53 \times 0.5 \times 2.5 = 30.66$	$2.5/3$	25.55
5	$-11.5 \times 3.5 = -40.25$	2.5	-17.1
$\Sigma$	<b>70.94 kPa</b>		<b>32.48</b>

$\bar{X} = \frac{32.48}{70.94} = 0.45 \text{ m}$

• Tensile Cracks occur in active case only  $\delta$

حالة سلبية  $\delta$



$Z_c$  : depth of tensile crack :

$Z_c$  @  $\sigma_a = 0$

$$0 = K_a \gamma' H - 2C\sqrt{K_a} \Rightarrow Z_c = \frac{2C\sqrt{K_a}}{\gamma' K_a} = \boxed{\frac{2C}{\gamma' \sqrt{K_a}}}$$

$$0 = K_a \gamma' Z_c - 2C\sqrt{K_a}$$

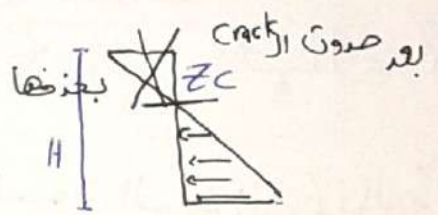
\* Horizontal force  $P_a$  / m before Tensile crack :

$$P_a = \frac{1}{2} (\gamma' K_a H^2) - 2C\sqrt{K_a} H$$

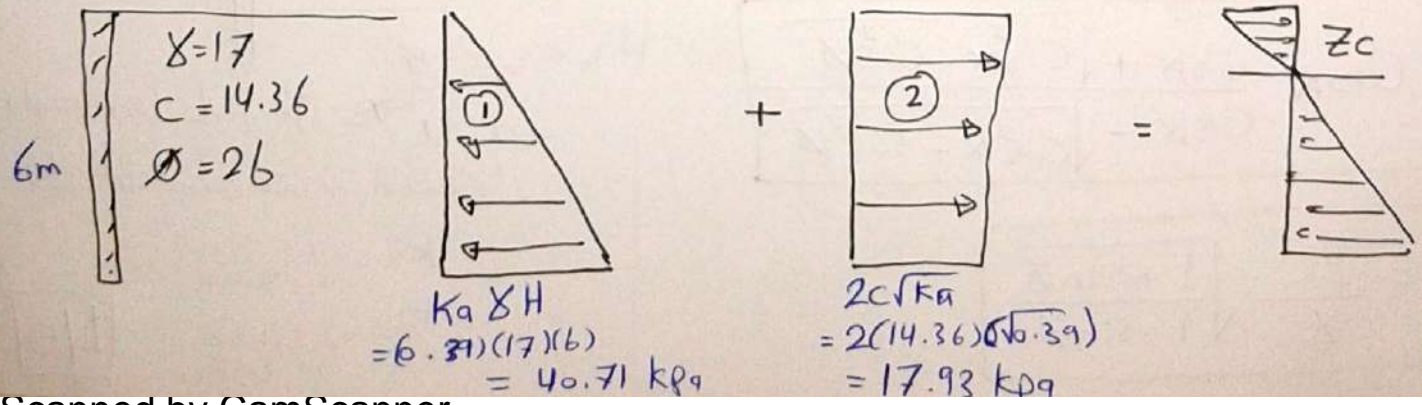
\* after tensile cracks occur :

$$P_a = \frac{1}{2} (K_a \gamma' H - 2C\sqrt{K_a}) (H - Z_c)$$

$$\bar{x} = \frac{H - Z_c}{3}$$



Ex: A 6m high retaining wall is to support a soil with unit weight  $\gamma = 17 \text{ kN/m}^3$ ,  $\phi = 26^\circ$ ,  $C = 14.36 \text{ kPa}$ . Determine retaining active force per unit length of wall before and after tensile cracks occur, and the line of action of the resultant in both cases :





$$* K_a = \frac{1 - \sin \phi}{1 + \sin \phi} = \frac{1 - \sin 26}{1 + \sin 26} = \boxed{0.39}$$

\*\*) before Tensile Crack :

Seg #	$P_{a_i}/m$	$X_i$	$P_{a_i} \times X_i$
1	$\frac{1}{2} \times 40.71 \times 6$	6/3	244.26
2	-17.93(6)	6/2	-322.74
$\Sigma 14.55 \text{ kN/m}$			$\Sigma = -78.48$

$$\bar{X} = \frac{P_{a_i} X_i}{P_{a_i}} = \boxed{-5.39 \text{ m}}$$

لأن اللود على الارتفاع وللمحافظة أسفل الجدار بسبب ال Cohesion.

\*\*) after Tensile crack :

$$z_c = \frac{2c}{\gamma \sqrt{K_a}} = \frac{2 \times 14.36}{17.4 \times \sqrt{0.39}} = \boxed{2.64 \text{ m}}$$

$$P_a = \frac{1}{2} (H - z_c) (\gamma K_a H - 2c \sqrt{K_a}) = \frac{1}{2} (6 - 2.64) ((17.4)(0.39)(6) - 2(14.36)\sqrt{0.39})$$

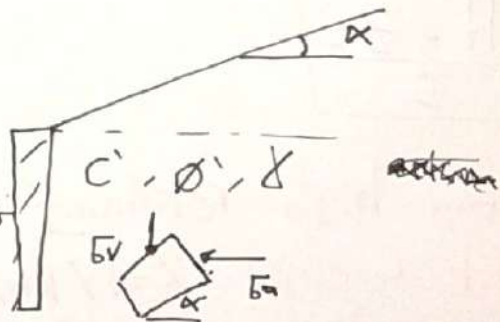
$$= \boxed{38.27 \text{ kN/m}}$$

$$\bar{X} = \frac{H - z_c}{3} = \frac{6 - 2.64}{3} = \boxed{1.12 \text{ m}}$$

• في حال كان هناك ميلان في التربة في منطقة ال active (or passive) بزوايا  $\alpha$

1) Rankine earth pressure :

$$\bar{\sigma}_a = K_a \bar{\sigma}_v, \quad \bar{\sigma}_p = K_p \bar{\sigma}_v$$

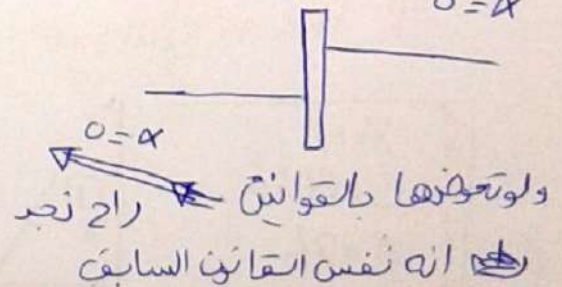


$$K_a = \cos \alpha \frac{\cos \alpha - \sqrt{\cos^2 \alpha - \cos^2 \phi}}{\cos \alpha + \sqrt{\cos^2 \alpha - \cos^2 \phi}}$$

$$K_p = \cos \alpha \frac{\cos \alpha + \sqrt{\cos^2 \alpha - \cos^2 \phi}}{\cos \alpha - \sqrt{\cos^2 \alpha - \cos^2 \phi}}$$

$$z_c = \frac{2c}{\gamma} \sqrt{\frac{1 + \sin \phi}{1 - \sin \phi}}$$

\*\*) في الامثلة السابقة كان السوييل افقي يعني  $\alpha = 0$

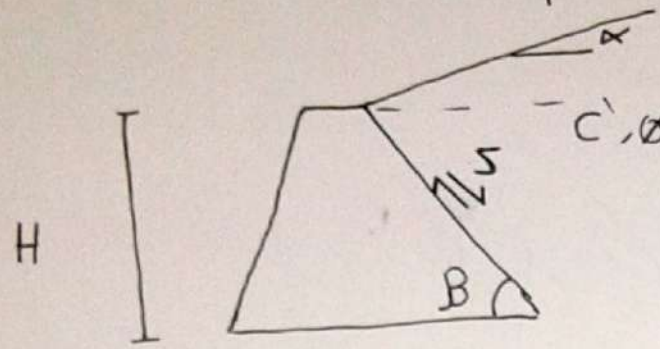


$$K_a = \frac{1 - \sin \phi}{1 + \sin \phi}$$

$$K_b = \frac{1 + \sin \phi}{1 - \sin \phi}$$

40

2/ Colombs earth pressure Coefficients :



$\delta$  = Interface friction angle  
 \* نلاحظ ان Rankine لم يهتم بشكل ال wall او زاوية ميلته  $\alpha$  بينما Colombs اخذها بعين الاعتبار هو و زاوية الاحتكاك .

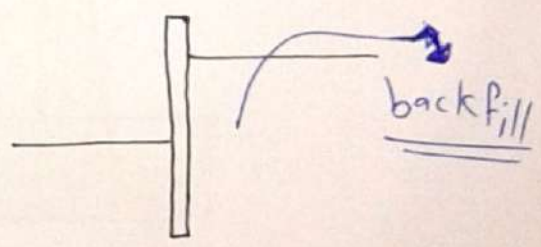
$$K_a = \frac{\sin^2(\beta + \phi)}{\sin^2\beta \sin(\beta - \delta) \left[ 1 + \sqrt{\frac{\sin(\phi + \delta) \sin(\phi - \alpha)}{\sin(\beta - \delta) \sin(\alpha + \beta)}} \right]^2}$$

$$K_p = \frac{\sin^2(\beta - \phi)}{\sin^2\beta \sin(\beta + \delta) \left[ 1 + \sqrt{\frac{\sin(\phi + \delta) \sin(\phi + \alpha)}{\sin(\beta + \delta) \sin(\alpha + \beta)}} \right]^2}$$

Ex : Compare Rankine & ~~Rankine~~ Colomb Lateral earth pressure coefficient for a wall retains a granular back fill soil with ( $\phi = 35^\circ, \delta = 15^\circ, \alpha = 20^\circ, \beta = 90^\circ$ )

\*\* Rankine :  $K_a = 0.322$   
 $K_p = 2.74$

\* Colomb :  $K_a = 0.323$   
 $K_p = 24.46$

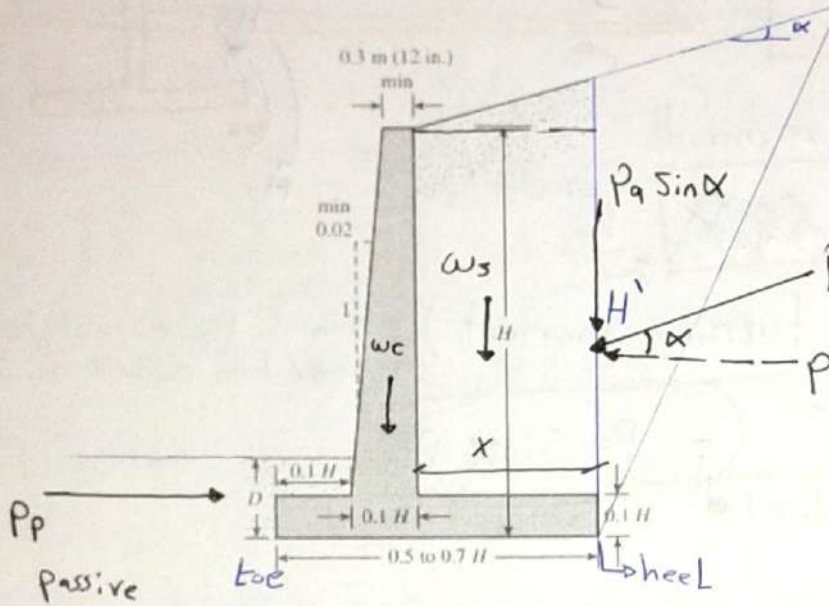


⇒ Colomb أدق

# ☐ Lateral earth pressure application :

☒ Conventional retaining walls (RSW) :

☐ Cantilever R.w "reinforced concrete"



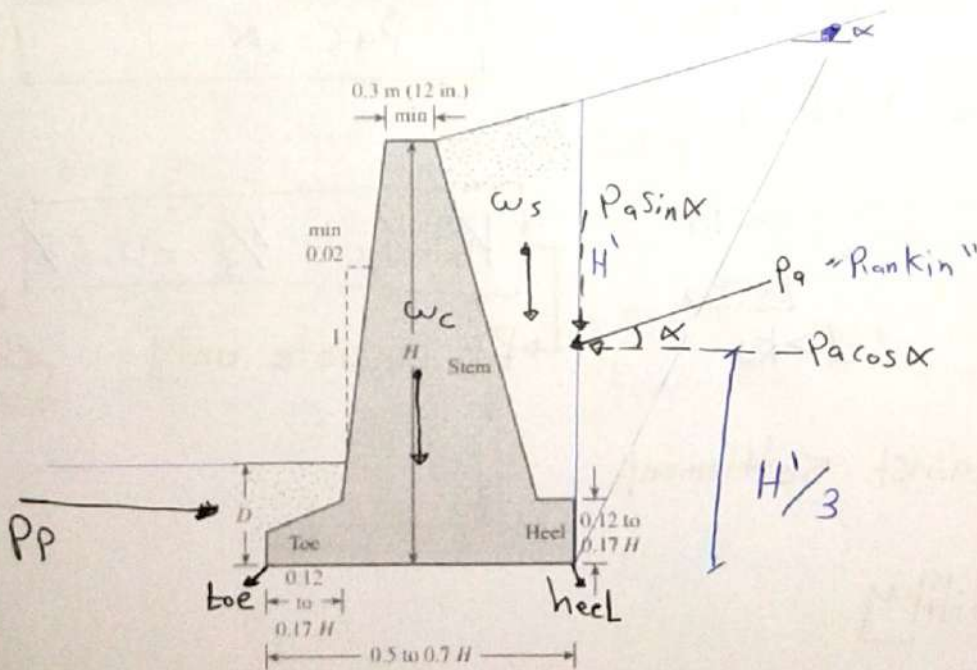
$$H' = H + X \tan \alpha$$

☒ هذه الصيغة لا تأخذ في الاعتبار عن Rankine Theory لأن Pa تلاحظ أيضا على ال Soil تؤثر

☐ Gravity wall "plain concrete only"

☒ بالنسبة لـ Coulomb Theory

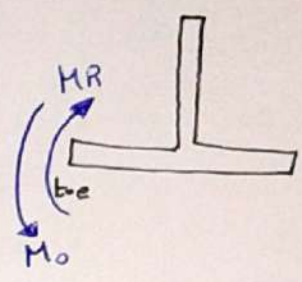
Pa مؤثرة مباشرة على الحائط (سوف تدرس لاحقا)



The R.w must satisfied the following stability checks :

1] safe against over turning about the toe (point o) :

$$F.S_{ot} = \frac{\sum MR}{\sum M_o} \geq \underline{\underline{3}}$$



\*  $\sum MR$  : all Resistance moment

$$= \sum w_i \bar{x}_i + \cancel{\dots} \quad \leftarrow \begin{matrix} \text{و} \text{ و} \text{ و} \text{ و} \\ P_p \end{matrix}$$

\*  $\sum M_o$  : Driving (over turning moment) : sum of the moment tend to over turn the wall around toe

$$= (P_a \cos \alpha) \frac{H^3}{3} - P_a \sin \alpha B$$

~~...~~ اختياري

2] safe against sliding along the base "friction, adhesion, passive force"

$$F.S_{sliding} = \frac{\text{Resistance force}}{\text{driving force}} = \frac{\sum V \tan \delta + BCa + P_p}{P_a \cos \alpha} \geq \underline{\underline{1.5}}$$

\*  $\sum V$  → sum of all vertical force (w)

$$\delta = k_1 \phi_2$$

$$Ca = k_2 C_2$$

$\alpha < k_1$   
"  
~~...~~  
 $1 > k_2$

$$k_1 = k_2 = \frac{2}{3} = 0.67$$

↳ For concrete only

4] footing safe against settlement

5] over all stability

3/ Footing safe against Bearing Capacity Failure :

$$e = \frac{B}{2} - \frac{\sum MA - \sum M_o}{\sum V} \leq B/6$$

$$F.S.BC = \frac{q_{ult}}{q_{mat}} \geq 3$$

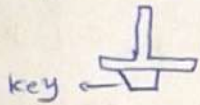
$q_{ult}$  : تعطى بالسؤال  
 أو تحسب المادة المرست  
 for eccentricity footing.

$$q_{toe} = q_{max} = \frac{\sum V}{B} \left( 1 + \frac{6e}{B} \right)$$

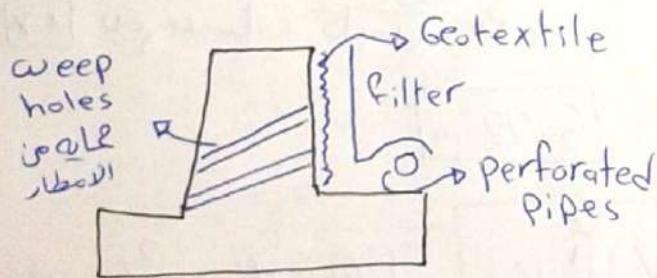
$$q_{heel} = q_{min} = \frac{\sum V}{B} \left( 1 - \frac{6e}{B} \right) \geq 0$$

\*\* IF sliding not satisfy : \* اختر مستطيل و يكون لها من خلال

- (1) Use stronger back fill soil =  $\phi \uparrow$   $K_a \downarrow$
- (2) Install Tie back anchor.
- (3) extend the heel
- (4) provide Key : increase  $p_p$  by increas  $D_f \Rightarrow (D_f + D_{key})$



\*\* Backfill drainage :



\* Two conditions must met :

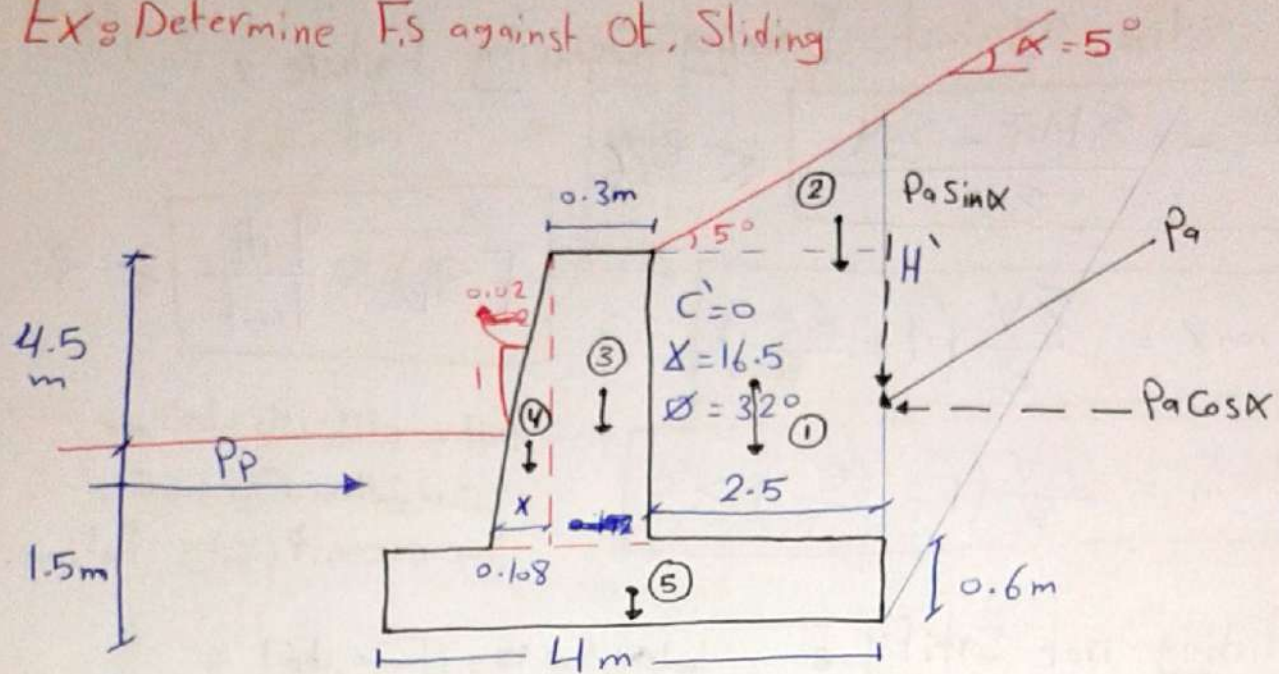
$$\left\{ \frac{D_{15} \text{ Filter}}{D_{85} \text{ backfill}} < 5 \right. \quad \text{حتى لا تدخل اجزاء ال backfill الى ال Filter}$$

$$\left\{ \frac{D_{15} \text{ Filter}}{D_{15} \text{ backfill}} > 5 \right. \quad \text{يمنع تسكل ال U Lapore water pressure}$$

$D_{15} \rightarrow 15\% \text{ passing}$   
 $\hookrightarrow$  Diameter

Ex: Determine F.S against Ot, Sliding

$\gamma_{concrete} = 24 \frac{kN}{m^3}$



$c' = 40 \text{ kPa}$  -  $\gamma = 18 \text{ kN/m}^3$   
 $\phi = 22^\circ$

$$\frac{0.02}{1} = \frac{x}{6 - 0.6}$$

$$x = 0.108 \text{ m}$$

Sol:  $K_{a1} = \cos \alpha \frac{\cos \alpha - \sqrt{\cos^2 \alpha - \cos^2 \phi}}{\cos \alpha + \sqrt{\cos^2 \alpha - \cos^2 \phi}} = \cos 5 \frac{\cos 5 - \sqrt{\cos^2 5 - \cos^2 32}}{\cos 5 + \sqrt{\cos^2 5 - \cos^2 32}}$

$$= \boxed{0.31}$$

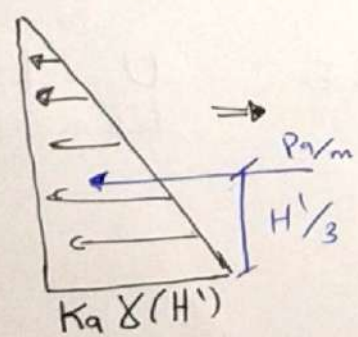
$K_{p2} = \frac{1 + \sin \phi}{1 - \sin \phi} = \frac{1 + \sin 22}{1 - \sin 22} = \boxed{2.19}$

لأن الـ  $\alpha$  ليس متساوي افقي  
 $\alpha = 0^\circ$

\*\*\* يتم حساب كل من  $P_p$  و  $P_a$  مثل السابق -

$H' = H + 2.5 \tan \alpha = 6 + 2.5 \tan 5 = \boxed{6.22 \text{ m}}$

•  $P_a$



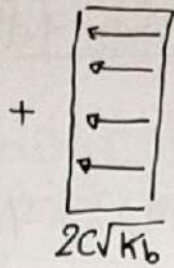
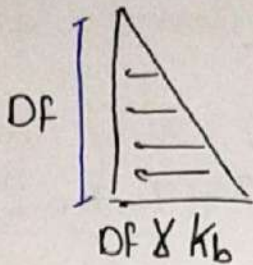
$P_a/m = \frac{1}{2} \gamma H'^2 K_a = \frac{1}{2} (16.5) (6.22)^2 (0.31)$

$$= \boxed{98.94 \text{ kN/m}}$$

\*  $P_{ah} = P_a \cos \alpha = 98.94 \cos 5 = \boxed{98.56 \text{ kN/m}}$

\*  $P_{av} = P_a \sin \alpha = 98.94 \sin 5 = \boxed{8.62 \text{ kN/m}}$

•  $P_p =$



$$\Rightarrow P_p/m = \frac{1}{2} \times Df \times Kb + 2C\sqrt{Kb} Df$$

$$= 0.5(18)(1.5)^2(2.19) + 2(40)(\sqrt{2.19})(1.5)$$

$$= \boxed{221.93 \text{ KN/m}}$$

Seg #	$A_i$	$V_i \text{ (KN/m)}$	$X_i$	$M_{Fi}$
1	$(2.5)(6-0.6) = 13.5$	$(13.5)(16.5) = 227.75$	$4 - \frac{2.5}{2} = 2.75$	626.31
2	$\frac{1}{2}(2.5)^2 \tan 5 = 0.27$	$0.27(16.5) = 4.455$	$4 - \frac{2.5}{3} = 3.167$	14.11
3	$0.3(6-0.6) = 1.62$	$1.62(24) = 38.88$	$4 - 2.5 - \frac{0.3}{2} = 1.35$	52.488
4	$\frac{1}{2}(0.108)(6-0.6) = 0.2916$	$0.2916(24) = 6.998$	$4 - 2.5 - 0.3 - \frac{0.108}{3} = 1.164$	8.145
5	$4 \times 0.6 = 2.4$	$2.4(24) = 57.6$	$4/2 = 2$	115.2
6	$P_{av} =$	8.62	4	34.48

$$\Sigma V = 344.303$$

$$\Sigma MR = 850.733 \text{ (KN/m)} \cdot m$$

with  $P_{av}$

$$\Sigma MR = 816.253 \text{ (KN/m)} \cdot m$$

without  $P_{av}$

$X_i$  : المسافة الأفقية بين PV toe وال toe

$$* F.Sot = \frac{\Sigma MR}{\Sigma M_o}$$

$$\Sigma M_o = (P_{ah}) H \frac{1}{3} = 98.56 \left( \frac{6.22}{3} \right) = 204.34 \text{ KN}\cdot\text{m/m}$$

$$F.Sot = \frac{850.733}{204.34} = 4.163 > 3 \text{ ok}$$

~~with out~~  $\Rightarrow$  كل عال وافي

$$F.Sot = \frac{816.25 \text{ "without } P_{av} \text{"}}{204.34 - 34.48} = 4.805 > 3 \text{ ok}$$

$P_{av} \sin \alpha$  B  $\leftarrow$  المسافة

مهم جداً ~~الاستاذ~~ الاستاذ كان الدكتور يقول ان  $P_p$  بال  $M_R$  في حال لم يقل  $\Sigma MR = \Sigma w_i X_i + P_p \bar{X}$

$$\Sigma MR = \Sigma w_i X_i + P_p \bar{X}$$

\*\*\*

$$* F.S \text{ sliding} = \frac{\sum V \tan \delta + B C_a + P_p}{P_{ah}}$$

$$= \frac{344.303 \tan\left(\frac{2}{3}(22)\right) + 4\left(\frac{2}{3}(40)\right) + 221.93}{98.94}$$

$$= 4.23 > 1.5 \text{ OK}$$

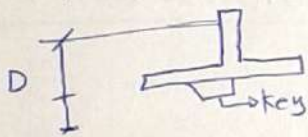
**\*\*** IF GW Rise To the surface :

$$P_{ah} = P_{ah_1} + P_{ah \text{ hydrostatic}}$$

$$= 98.94 + \frac{1}{2} (\gamma_w) (H_w)^2 = 98.94 + \frac{1}{2} (9.81) (6)^2 = \boxed{275.52 \text{ kN/m}}$$

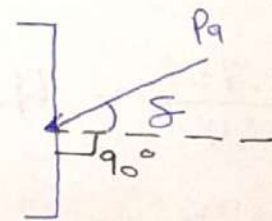
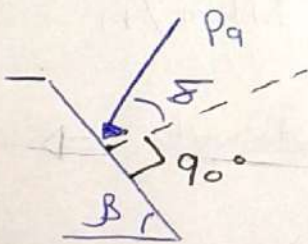
$$F.S \text{ sliding}_{\text{new}} = \frac{344.303 \tan\left(\frac{2}{3}(22)\right) + 4\left(\frac{2}{3}(40)\right) + 221.93}{275.52} = 1.519 > 1.5 \checkmark$$

في حال كانت F.S اقل من 1.5 ، نفرضها انها 1.5 ونحسب من خلالها  $P_p$  ومن قانون ال  $P_p$  نحسب ال  $D$  ثم اطرح ال  $D$  الاصلية من ال  $D$  المحسوبة والفرق سوف يكون طول ال Key كحل لل-sliding .



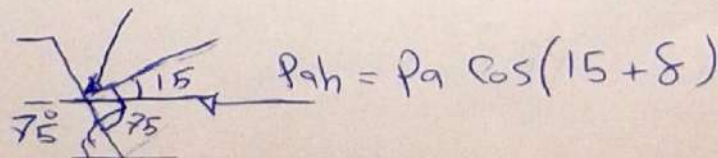
**\*\*** For Colomb Theory :

القوة مؤثرة مباشرة على الطائفة



**\*\*** يوجد مثال عليها بالكتاب Ex 13.2 صفته 669

\* اهم استيعاد عند تحليل  $P_{ah}$  في حال الجدار المتائل

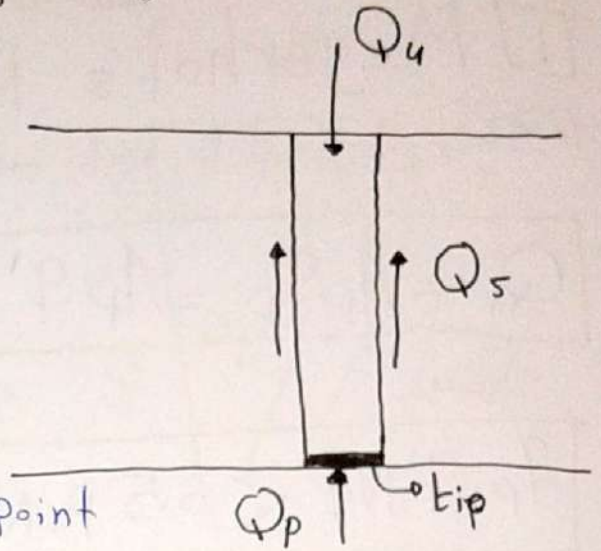




# Deep Foundation "Piles" :

## Static Pile Capacity :

$$Q_u = Q_p + Q_s$$



$Q_u$  : ultimate load carrying capacity

$Q_p$  : Load-carrying capacity of the pile point

$Q_s$  : Frictional resistance (skin friction) derived from the soil-pile interface.

$$Q_p = A_p q_p = A_p (\bar{c} N_c^* + q' N_q^*)$$

$A_p$  : area of pile tip

$\bar{c}$  : Cohesion of the soil supporting the pile tip  $\approx \frac{c}{2}$

$q_p$  : unit point resistance

$q'$  : effective vertical stress at level of the pile tip =  $\gamma' z$

$N_c^*, N_q^*$  = Bearing capacity factors.

$$Q_s = \sum p \Delta L f$$

$p$  : Perimeter of the pile section  $\text{الدائرة}$

$\Delta L$  : incremental pile length over which  $p$  &  $f$  are taken to be constant :  $p, f$   $\text{باعتبارهما ثابتين}$

$f$  : unit friction resistance at any depth.

$$Q_{All} = \frac{Q_u}{F.S}$$

$Q_{All}$  : allowable load-carrying capacity  
 $F.S$  : Factor of safety

● For Estimating  $Q_p$  &  $Q_s$  in sand :

1 Meyerhof's Method :

\*\* For tip pile rest on sand

$$Q_p = A_p q_p = A_p q' N_q^*$$

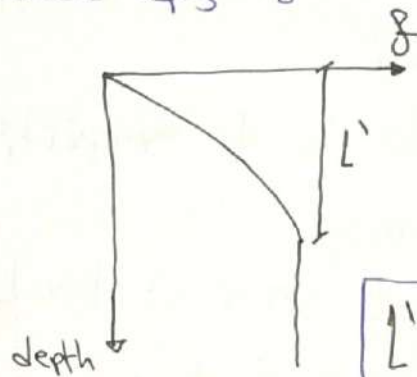
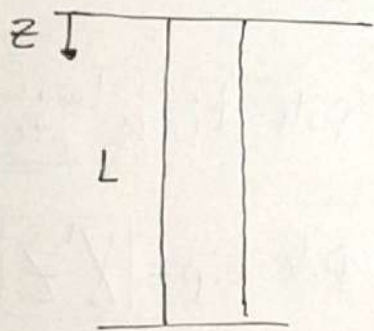
بشرط

$$q_p = q' N_q^* < 0.5 P_a N_q^* \tan \phi'$$

بافتتاح القتيمة الاقل منهم وبعتمدها

$P_a = 100 \text{ kN/m}^2 \Rightarrow$  atmospheric pressure

\*\* Frictional resistance  $Q_s$  :



\*\* معامل الاحتكاك يصل بزيادة  
لعمق بعميقه  
Critical depth  $L'$   
بدرين بنيت .

$$L' = 15 D$$

●  $z = 0 \rightarrow L'$

$$f = K_0 \bar{\sigma}_o \tan \delta'$$

$z = L' - L$  بنيت

$$f = f_z @ L'$$

$$Q_s = \sum f \Delta L p$$

عند عند الحل بقسم الطبقات من  $L' - 0$  و  $L - L'$

$K_0 \Rightarrow$  جدول من الكتاب

$\bar{\sigma}_o \Rightarrow$  effective stress at each level

له الطريقة حل توضع بالامثلة

$\delta' \Rightarrow$  friction angle ( $0.5\phi' - 0.8\phi'$ )

\* medium - displacement driven

\*\* قسرة سنوات

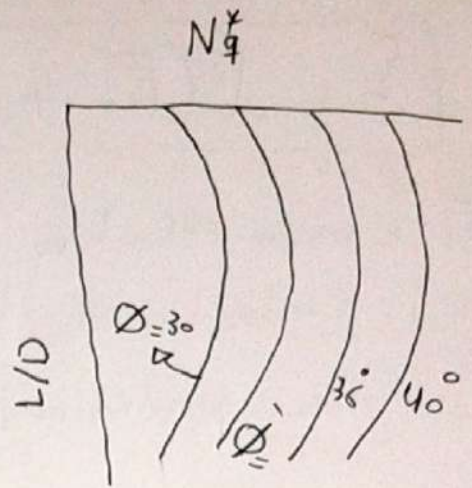
$$\therefore K_0 = 1.6(1 - \sin \phi')$$

## 2] Coyle & Castello's Method :

\*\* For estimating  $Q_p$  on sand :

$$Q_p = q' N_q^* A_p$$

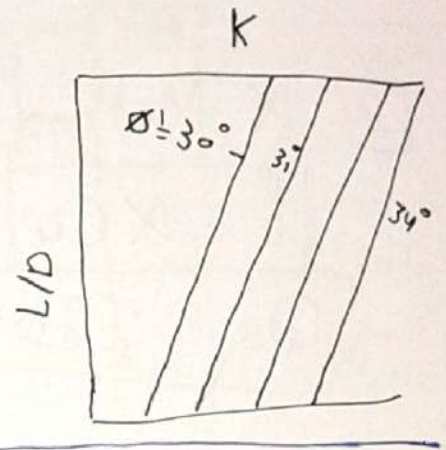
$q'$  : effective vertical stress at pile tip.



\*\* Frictional resistance  $Q_s$  :

$$Q_s = \int_{0}^{L} p \, dL = \sum (K \bar{\sigma}_0 \tan \delta') PL$$

$K$  is from chart  $\Rightarrow$



for estimating  $Q_p$  &  $Q_s$  in clay

$Q_p$  for pile in saturated clays under undrained conditions ( $\phi = 0$ )

$$Q_p = 9 C_u A_p$$

$C_u$  : undrained cohesion of the soil below the tip of the pile.

Frictional (Skin) Resistance in Clay :

\* Three methods exist :

1.  $\alpha$  method

2.  $\alpha$  method

3.  $\beta$  method

$$Q_s = \sum \int \Delta L P$$

for all

1)  $\lambda$  method :

$$f = \lambda (\bar{\sigma}_0 + 2C_u)$$

$\bar{\sigma}_0$  = mean effective vertical stress for the entire ~~length~~ Embedment Length.

$C_u$  = mean undrained shear strength " $\phi = 0$ "

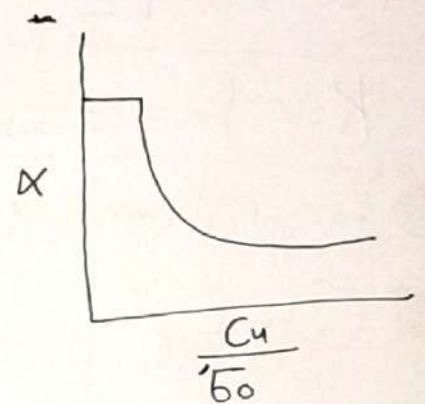
"interpolation" سنوان ←

Embedment Length $\Delta L$	$\lambda$

2)  $\alpha$  Method "total stresses"

$$f = \alpha C_u$$

$$Q_s = \sum f p \Delta L = \sum \alpha C_u p \Delta L$$



3)  $B$  method (effective stress) :

$$f = B \bar{\sigma}_0$$

$$f = (1 - \sin \phi'_R) \tan \phi'_R \sqrt{OCR} \bar{\sigma}_0$$

$\bar{\sigma}_0$  = vertical effective stress

$$B = K \tan \phi'_R$$

$\phi'_R$  = drained friction angle of remolded clay

$K$  = earth pressure ~~coeff~~ coefficient

OCR = overconsolidation ratio

$$Q_u = Q_p + Q_s - W$$

وزن كونكريت

\* ملاحظة : في حل الأسئلة

$$W = (A p L) \gamma_c$$

Ex: for square precast prestress driven pile of 0.25m  
Estimate:

- (1) point resistance capacity by using both meyerhoff & Coyle & Castellos method.
- (2) shaft (skin) resistance by using both methods = high-diephrem ent "
- (3) ultimate carrying capacity if  $\gamma_c = 25 \text{ kN/m}^3$

Sol:

(1)

\* Meyerhoff:

$$Q_p = q_p A_p$$

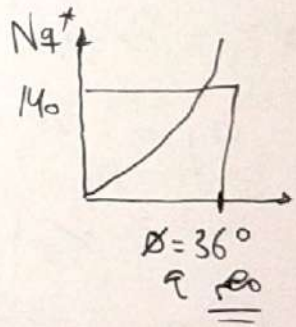
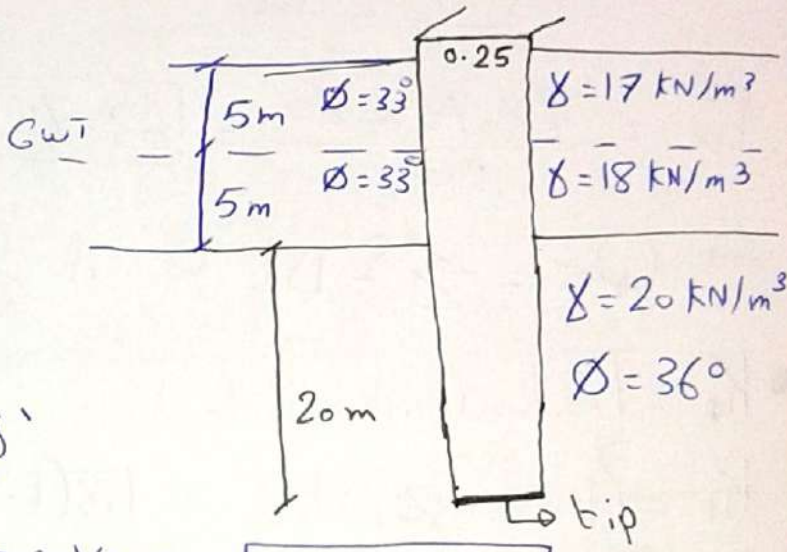
$$q_p = q' N_q^* < 0.5 P_a N_q^* \tan \phi'$$

$$q' = (17 * 5) + (18 - 9.81)(5) + (20 - 9.81)(20) = \boxed{329.75 \text{ kPa}}$$

$$q_p = 329.75 (140) < 0.5 (100) (140) (\tan 36)$$

$$46165 < \frac{5085.8}{L} \rightarrow \text{نأخذ الأقل مقداراً}$$

$$Q_p = (5085.8) (0.25)^2 = \boxed{317.8 \text{ kN}}$$

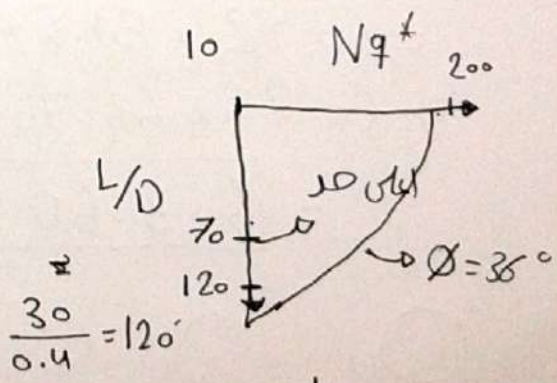


\* Coyle & Castello:

$$Q_p = q' (N_q^*) A_p$$

$$= 329.75 (10) (0.25)^2$$

$$= \boxed{206.1 \text{ kN}}$$



$120 = L/D$  \*  
بوض أقل قيمه  $N_q^* = 10$

(2)

⊗ Meyerhoff :

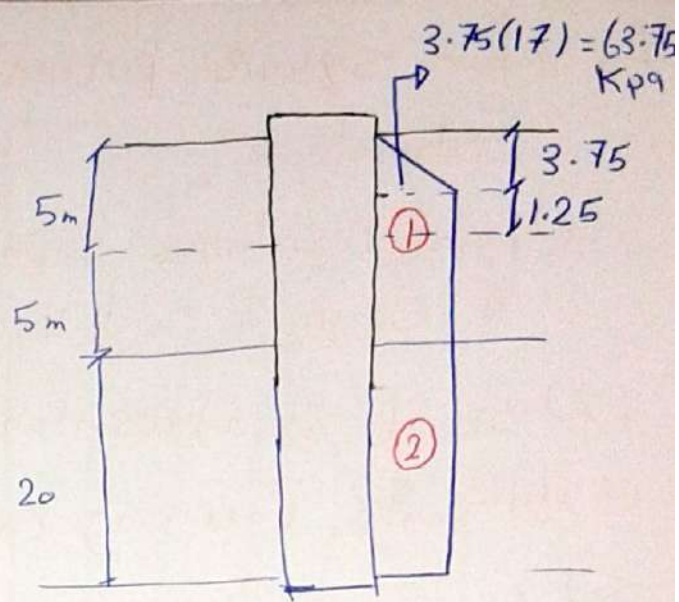
f → increase 0 - L' "critical depth"

$$L' = 15 \times 0.25 = 3.75 \text{ m}$$

$$\bar{b}_1 = \frac{\left[ \frac{1}{2} \times 3.75 \times 63.75 + 63.75(10 - 3.75) \right]}{10}$$

① طبقة

$$= \boxed{51.8 \text{ kpa}}$$



$$\bar{b}_2 = \frac{63.75 \times 20}{20} = \boxed{63.75 \text{ kpa}}$$

⇒  $Q_s = \sum \delta \Delta L P$  if ① high-displacement driven  
 ②  $\delta = \frac{2}{3} \phi'$

•  $k_s = 1.8 k_0$  (high-displ.)

$$k_1 = (1 - \sin \phi_1) 1.8 = 1.8(1 - \sin 33) = \boxed{0.82}$$

$$k_2 = 1.8(1 - \sin \phi_2) = 1.8(1 - \sin 36) = \boxed{0.72}$$

•  $\delta = \frac{2}{3} \phi'$

$$\delta_1 = \frac{2}{3}(33) = \boxed{22^\circ}$$

$$\delta_2 = \frac{2}{3}(36) = \boxed{24^\circ}$$

مساحة  
 $P$  per square =  $4 \times$  المساحة

$$Q_s = \sum (k_s \tan \delta p L)$$

$$= (0.82 \times 51.8 \times \tan 22 \times (4 \times 0.25 \times 10)) + (0.72 \times 63.75 \times \tan 24 \times (4 \times 0.25 \times 20))$$

$$= \boxed{603.65 \text{ kN}}$$

$$** w = (A_p L) \delta_c$$

$$= (0.25)^2 (30) (25)$$

$$= \boxed{46.8 \text{ kN}}$$

$$Q_u = Q_p + Q_s - w$$

Meyerhoff

$$= 317.8 + 603.65 - 46.8$$

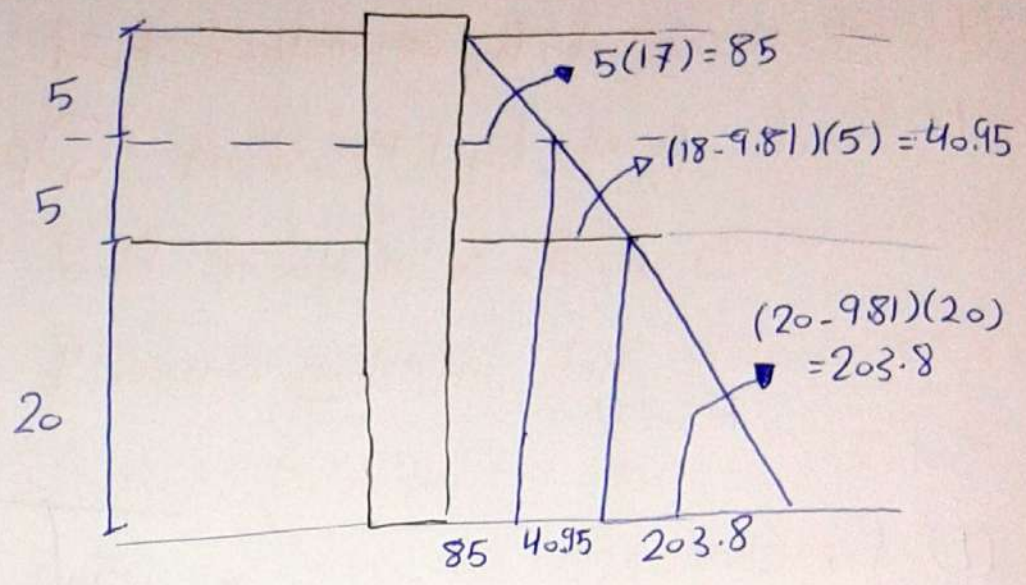
$$= \boxed{874.65 \text{ kN}}$$

54

\*7 Coyle & Castells 8

$$Q_s = \sum \gamma_s A_s$$

$$= K \bar{\sigma}_0 \tan \delta pL$$



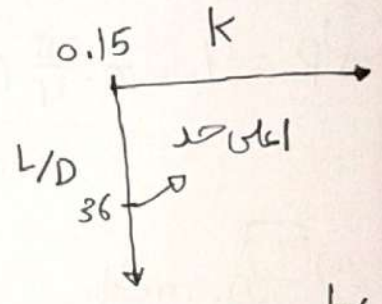
$$\bar{\sigma}_1 = \frac{[\frac{1}{2} * 85 * 5 + 85(5) + \frac{1}{2}(40.95)(5)]}{10} = \boxed{73.98 \text{ kPa}}$$

$$\bar{\sigma}_2 = \frac{(85 + 40.95)(20) + \frac{1}{2}(203.8)(20)}{20} = \boxed{277.85 \text{ kPa}}$$

$$Q_s = [0.15 * 73.98 * \tan(\frac{2}{3}(33)) * (4 * 0.25 * 10)]$$

$$+ [0.15 * 277.85 * \tan(\frac{2}{3}(36)) * (4 * 0.25 * 20)]$$

$$= \boxed{349.17 \text{ kN}}$$



$L/D = 36 = 120 = \frac{L}{D}$  اعلى حد لزيادة  
 اختيار اقل قيمة  $0.15 = k$

$$Q_u = Q_p + Q_s - w$$

Coyle & Castells

$$= 349.17 + 206.1 - 46.8 = \boxed{508.47 \text{ kN}}$$

Ex: For the pile shown, Estimate  $Q_p$

~~By using  $\alpha, \beta, \alpha$  method find~~

- (1) Find point (tip) resistance  $Q_p$ .
- (2) By using  $\alpha, \beta, \alpha$  method find  $Q_s$ .
- (3) allowable net carrying capacity if  $\gamma_c = 23 \text{ kN/m}^3$

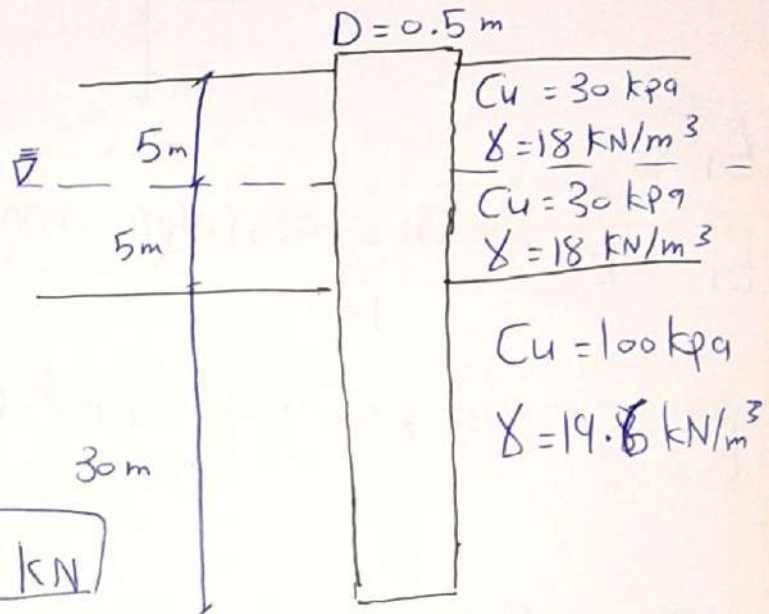
Sol: F.S = 4

(1) For clay:

$$Q_p = q_p \cdot A_p \quad \begin{matrix} \text{الطبقة التي} \\ \text{يقع فيها} \end{matrix}$$

$$q_p = 9(100) = 900 \text{ kPa}$$

$$Q_p = 900 \cdot \frac{\pi}{4} (0.5)^2 = \boxed{176.71 \text{ kN}}$$

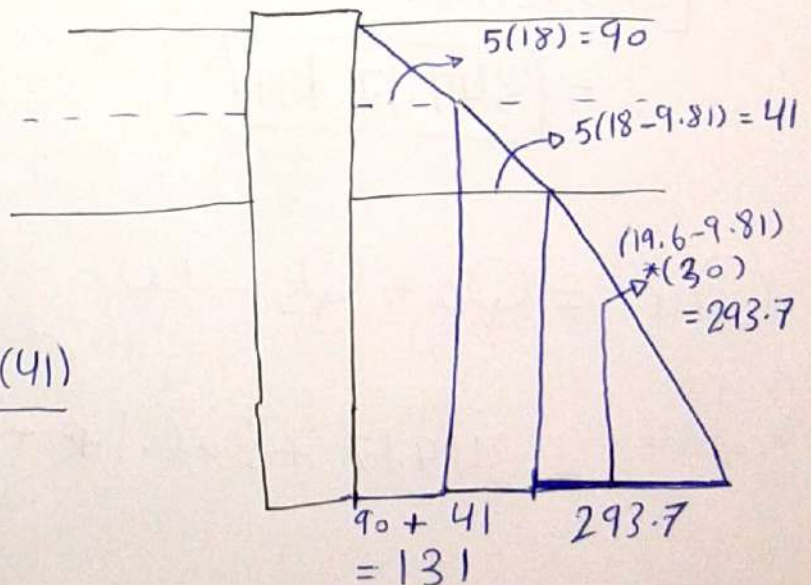


(2)  $\alpha$  method:

$$Q_s = \sum f_s A_s$$

$$f = \alpha (\bar{\sigma}_0 + 2C_u)$$

$$\bar{\sigma}_0 = \frac{(\frac{1}{2}(5 \times 90)) + 90(5) + \frac{1}{2}(5)(41)}{10} = \boxed{77.75 \text{ kPa}}$$



$$\bar{\sigma}_0 = \frac{131 \cdot 30 + \frac{1}{2}(30)(293.7)}{30} = \boxed{277.85 \text{ kPa}}$$



⇒ From table

$$L=10 \rightarrow \alpha = 0.245$$

$$L=30 \rightarrow \alpha = 0.136$$

$$Q_s = \sum \alpha_i (E_{oi} + 2C_{ui}) * \pi D L_i$$

$$= [0.245(77.75 + 2(30)) * \pi * (0.5) * 10]$$

$$+ [0.136(277.85 + 2(100)) * \pi * (0.5) * 30]$$

$$= 529.86 + 3060.92 = \boxed{3590.78 \text{ kN}}$$

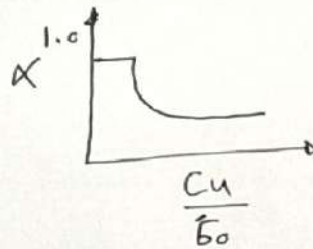
$$W = (A_p L) \gamma_c = \frac{\pi}{4} (0.5)^2 * 40 * 23 = \boxed{180.32 \text{ kN}}$$

$$Q_u = Q_s + Q_p - W = 3590.78 + 176.71 - 180.32$$
$$= \boxed{3587.17 \text{ kN}}$$

$$Q_{all} = \frac{Q_u}{F.S} = \frac{3587.17}{4} = \boxed{896.79 \text{ kN}}$$

2) X-method :

$$\gamma_s = X C_u$$



\* First Layer :

$$\frac{C_{u1}}{\sigma_{o1}} = \frac{30}{77.75} = 0.386 \approx \boxed{X_1 = 0.1}$$

\* Second Layer :

$$\frac{C_{u2}}{\sigma_{o2}} = \frac{100}{277.85} = 0.36 \approx \boxed{X_2 = 0.1}$$

$$Q_s = \sum \gamma_s A_s = (1 * 30 * \pi * (0.5) * 10) + (1 * 100 * \pi * 0.5 * 30)$$
$$= \boxed{5181 \text{ kN}}$$

57

[3]  $\beta$  - method :

$$\left[ \begin{array}{l} \phi_{R1} = 30^\circ, C_1 = 0 \\ \phi_{R2} = 35^\circ, C_2 = 0 \\ OCR = 1 \end{array} \right] \text{ نظر بالسؤال}$$

$$f_s = \beta \bar{\sigma}_0$$

$$B = (1 - \sin \phi_R) \tan \phi_R \sqrt{OCR}$$

$$f_{s1} = (1 - \sin 30) \tan 30 \sqrt{1} * 77.75 = 22.44$$

$$f_{s2} = (1 - \sin 35) \tan 35 \sqrt{1} * 277.85 = ~~194.58~~ 82.96$$

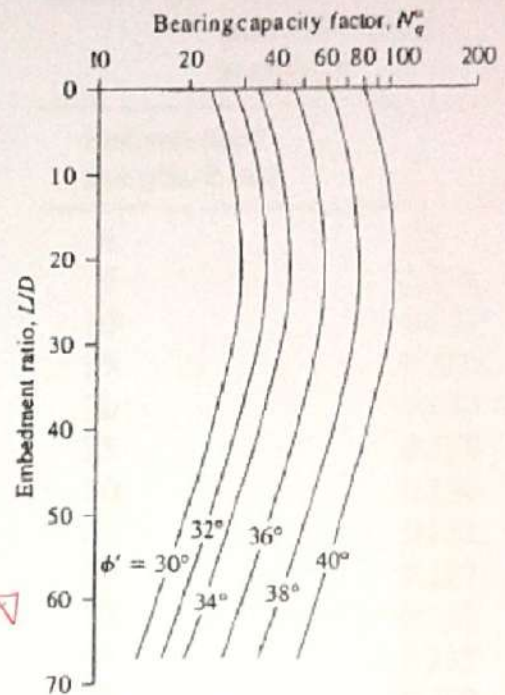
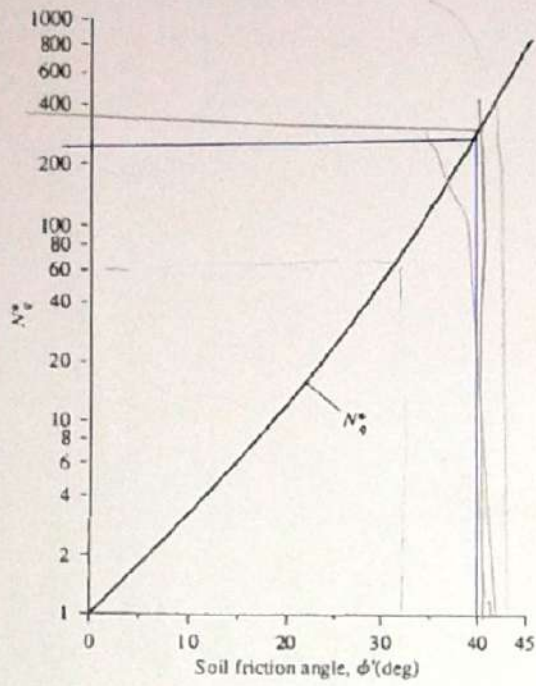
$$Q_s = \sum f_s P \Delta L$$

$$= 22.44 * \pi(0.5)(10) + ~~194.58~~^{82.96} * \pi(0.5)(30)$$

$$= 352.308 + ~~915.713~~ 3907.416$$

$$= ~~915.713~~ \text{ KN}$$

$$= ~~915~~ 4259.724 \text{ KN}$$



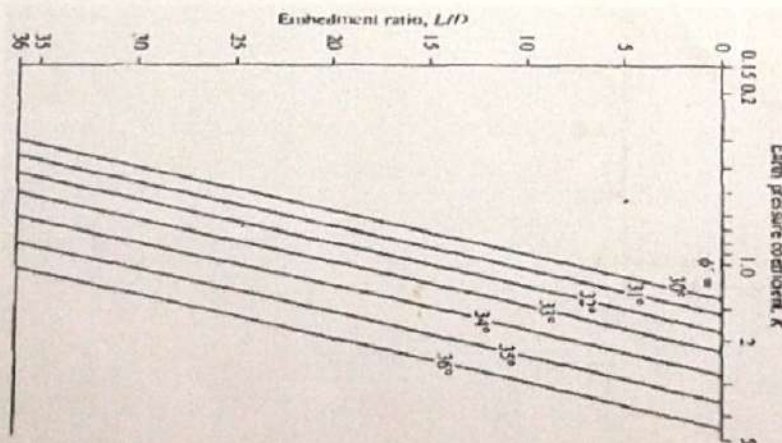
$$Q_p = q' N_q^* A_p$$

$$f = K \bar{\sigma}'_o \tan \delta'$$

$$\diamond L' = 15D$$

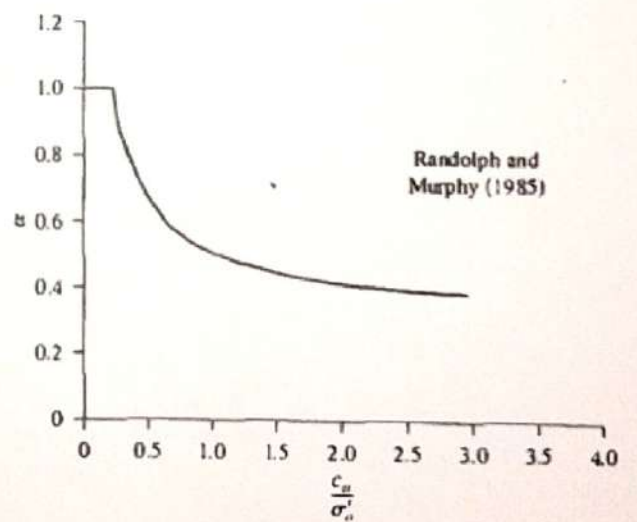
Pile type	K
Bored or jettied	$\approx K_o = 1 - \sin \phi'$
Low-displacement driven	$\approx K_o = 1 - \sin \phi'$ to $1.4K_o = 1.4(1 - \sin \phi')$
High-displacement driven	$\approx K_o = 1 - \sin \phi'$ to $1.8K_o = 1.8(1 - \sin \phi')$

$$Q_r = f_{av} \rho L = (K \bar{\sigma}'_o \tan \delta') \rho L$$



**Table 11.7** Variation of  $\lambda$  with pile embedment length,  $L$

Embedment Length, $L$ (m)	$\lambda$
0	0.5
5	0.336
10	0.245
15	0.200
20	0.173
25	0.150
30	0.136
35	0.132
40	0.127
50	0.118
60	0.113
70	0.110
80	0.110
90	0.110



In Problems 13.1 through 13.4, use  $\gamma_{\text{concrete}} = 23.58 \text{ kN/m}^3$ . Also, in Eq. (13.11), use  $k_1 = k_2 = 2/3$  and  $P_p = 0$ .

13.1 For the cantilever retaining wall shown in Figure P13.1, let the following data be given:

Wall dimensions:  $H = 8 \text{ m}$ ,  $x_1 = 0.4 \text{ m}$ ,  $x_2 = 0.6 \text{ m}$ ,  $x_3 = 1.5 \text{ m}$ ,  $x_4 = 3.5 \text{ m}$ ,  $x_5 = 0.96 \text{ m}$ ,  $D = 1.75 \text{ m}$ ,  $\alpha = 10^\circ$

Soil properties:  $\gamma_1 = 16.8 \text{ kN/m}^3$ ,  $\phi'_1 = 32^\circ$ ,  $\gamma_2 = 17.6 \text{ kN/m}^3$ ,  $\phi'_2 = 28^\circ$ ,  $c'_2 = 30 \text{ kN/m}^2$

Calculate the factor of safety with respect to overturning, sliding, and bearing capacity.

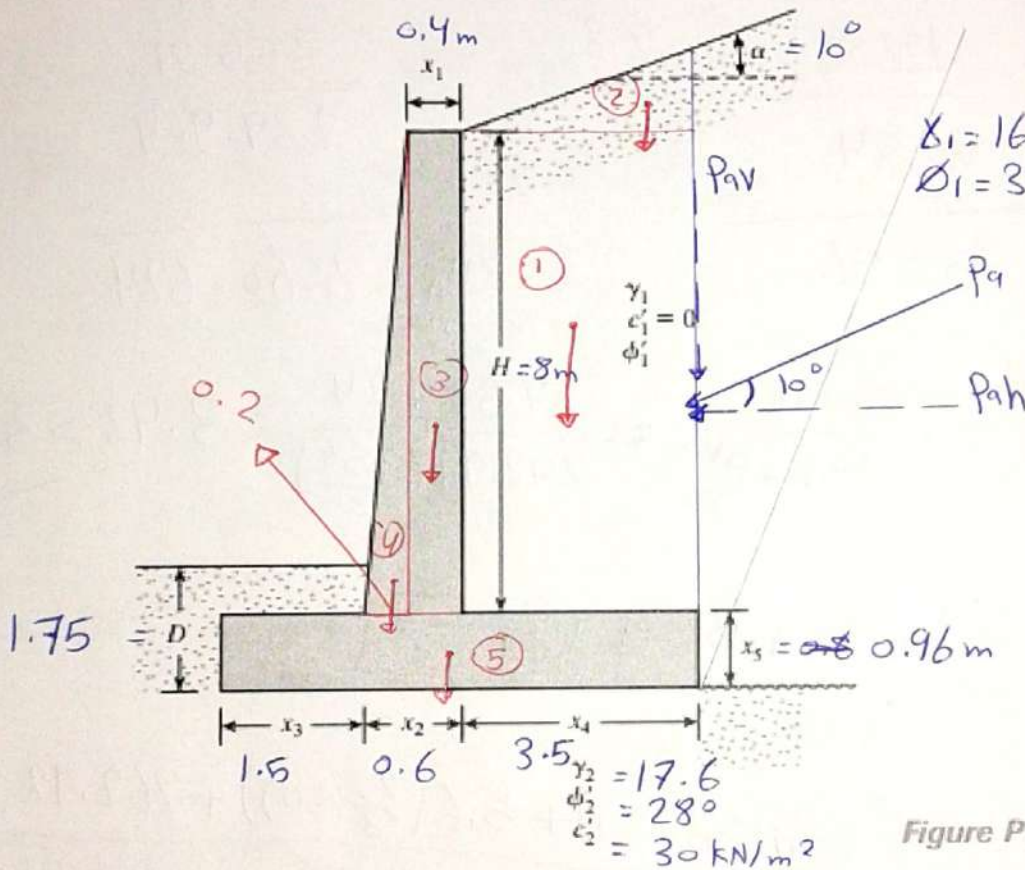


Figure P13.1

$$\begin{aligned}
 H' &= H + x_4 \tan \alpha \\
 &= 8.96 + 3.5 \tan 10^\circ \\
 &= \boxed{9.58 \text{ m}}
 \end{aligned}$$

$$k_{a1} = \cos 10^\circ \frac{\cos 10^\circ - \sqrt{\cos^2 10^\circ - \cos^2 32^\circ}}{\cos 10^\circ + \sqrt{\cos^2 10^\circ - \cos^2 32^\circ}} = \boxed{0.32}$$

$$k_{p2} = \frac{1 + \sin \phi}{1 - \sin \phi} = \frac{1 + \sin 30^\circ}{1 - \sin 30^\circ} = \boxed{3}$$

$$P_a = \frac{1}{2} \gamma H'^2 k_a = \boxed{246.69 \text{ kN/m}}$$

$$P_{aH} = P_a \cos \alpha = \boxed{242.94 \text{ kN}} \quad // \quad P_{aV} = P_a \sin \alpha = \boxed{42.84 \text{ kN/m}}$$

•  $P_p = 0.5 \times DF^2 K_p + 2C \sqrt{K_p} DF$   
 $= 0.5(17.6)(1.75)^2(3) + 2(30)\sqrt{3}(1.75)$   
 $= \boxed{262.72 \text{ kN}}$

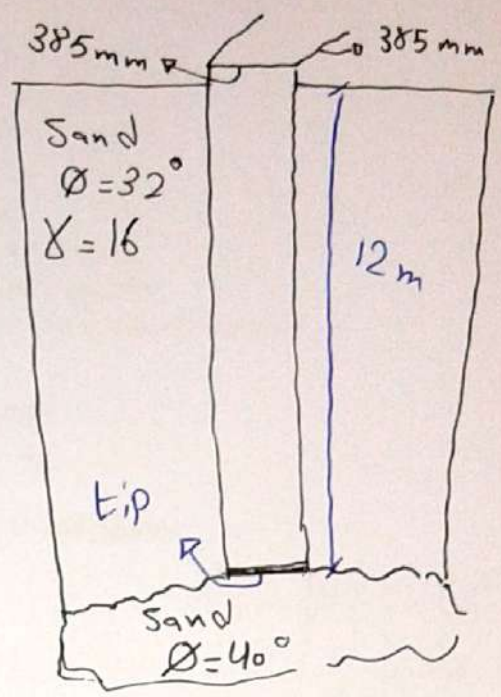
Seg #	$A_i$	$V_i$	$X_i$	$M F_i$
1	28	470.4	3.85	1811.04
2	1.08	18.14	4.43	80.36
3	3.2	75.46	1.9	143.37
4	0.8	18.86	1.63	30.74
5	5.38	126.86	2.8	355.21
6		$\Sigma V = 752.56$	5.6	$\Sigma MR = 2660.624$

\*  $F.S_{ot} = \frac{\Sigma MR}{\Sigma M_o} = \frac{\Sigma MR}{P_{ah} \times \frac{H^3}{3}} = \frac{2660.624}{242.94 \left(\frac{9.58}{3}\right)} = 3.43 > 3$  ✓

$F.S_{sliding} = \frac{\Sigma V \tan \delta + C_a + P_p}{P_{ah}}$   
 $= \frac{752.56 \tan\left(\frac{2}{3}(28)\right) + 5.6\left(\frac{2}{3}(30)\right) + 262.72}{242.94}$   
 $= 2.59 > 1.5 \text{ ok}$  ✓

Q : فكرة سنوات فصل ماضي 2016

① Find  $Q_p$  : لاحظ ان هناك طبقة صغيرة بالاسفل مختلفة عن اعلى هي التي تدخل ال Tip لذلك نستخدم  $\phi = 40^\circ$  او  $\phi = 32^\circ$



Using Meyerhof's :

$$Q_p = A_p q' N_q^*$$

$$A_p = (0.385)^2 = 0.14823 \text{ m}^2$$

$$q' = 16 \times 12 = 192 \text{ kPa}$$

$$N_q^* \text{ from chart @ } \phi = 40^\circ = 250$$

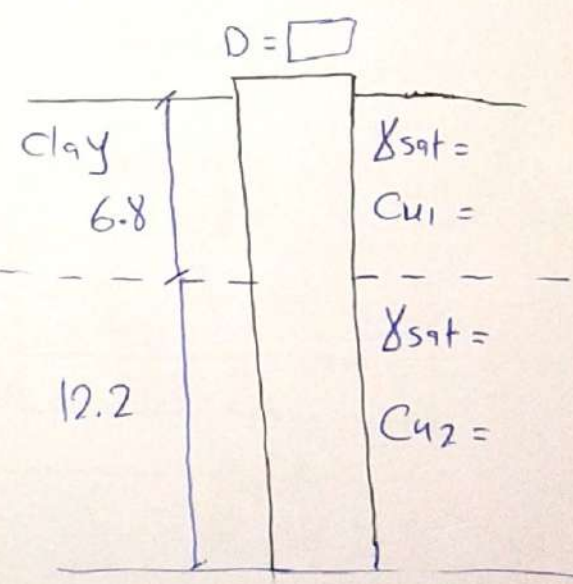
$$Q_p = 7115.04 \text{ kN}$$

فكرة \*\*

② كانت ايجاد  $Q_s$  بالطريقتين medium-displacement Driven  $K_0 = 1.6(1 - \sin \phi)$

③ اوجد  $Q_u$  و  $Q_y$

Q : \* كان فيه  $\gamma_{sat}$  اعلى ال water table : 3



اسأل الدكتور عنها

①  $Q_p = 9C_{u2} =$  مباشرة قانون

②  $Q_s \rightarrow$  3 method  $\alpha, \beta, \alpha$

③  $\rightarrow$  سؤال فكرة

\*\* اعطي  $Q_u$  و  $Q_y$  وحسبنا  $Q_y$  وسأل هل تستطيع التحمل، اذا لا اصيب كم لازم تزيد طول ال pile بالطبقة الثانية مشان يتحمل .

$$Q_{all} = \frac{Q_p + [Q_{s1} + \gamma_{s2} * P * L]}{F.S} \sim \text{or } (A_p L \gamma_c)$$

لكن تأثيرها قليل

# امتحان فصل ماضي "اول" 2016

Student Name: ..... Student Number: .....



Hashemite University  
Faculty of Engineering  
Department of Civil Engineering  
Foundation Engineering (0401333)  
Instructor: Dr. Omar Al-Hattamleh

First Exam  
Thursdays: 30/05/2009  
**Attempts All Problems**  
*Write Only in the designated space*

## No Partial Credit Will Be Given

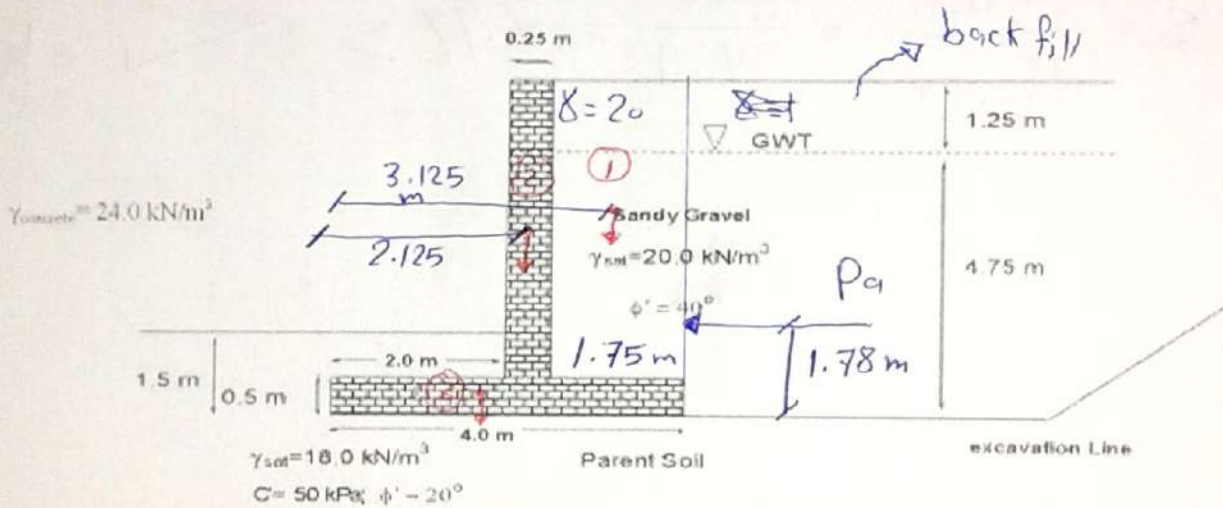
**Question # 1: (12 Points)**

Determine if the retaining wall shown with straight stem in the following figure is safe against:

- 1) Sliding (F.S. > 1.5)
- 2) Overtuning (F.S. > 2.0)
- 3) Bearing capacity failure, use ultimate bearing capacity,  $q_{ult} = 750.0$  kPa.

(Note ignore passive contribution; consider  $\gamma_{dry} = \gamma_{sat}$  for backfill soil)

$\gamma_c = 24 \text{ kN/m}^3$   
ب20



Section no	Area(m <sup>2</sup> )	Weight/m (kN/m)	Moment arm(m)	Moment (kN.m)/m
1	1.75(5.5) = 9.63	9.63(20) = 192.6	3.125	601.875
2	0.25(5.5) = 1.38	1.38(24) = 33.12	2.125	70.38
3	0.5(4) = 2	2(24) = 48	$\frac{1}{2} \times 4 = 2$	96
$\Sigma V = 273.72$				$\Sigma MR = 768.26$

\*  $F.S_{ot} = \frac{\Sigma MR}{\Sigma M_o} = \frac{768.26}{Pa_h \times 1.78} = \frac{768.26}{289.48} = 2.65 > 2 \checkmark$

\*  $F.S_{sliding} = \frac{\Sigma V \tan \delta + B C_a + PP}{Pa_h} = \frac{273.72 \tan(\frac{2}{3}(20)) + 4(\frac{2}{3} \times 50) + 244.09}{165.415} = 2.67 > 1.5 \checkmark$



**☆☆** B.S Failure &

$$e = \frac{B}{2} - \frac{\sum M_R - \sum M_O}{\sum V} \leq \frac{B}{6}$$

$$= 2 - \frac{768.26 - 289.48}{273.72} = \boxed{0.25 \text{ m}}$$

$$q_{\text{toe}} = q_{\text{max}} = \frac{\sum V}{B} \left( 1 + \frac{6eB}{B} \right) = \frac{273.72}{4} \left( 1 + \frac{6(0.25)}{4} \right)$$

$$q_{\text{heel}} = q_{\text{min}} \Rightarrow 0 \checkmark = \boxed{94.09 \text{ kPa}}$$

$$F_{B.S} = \frac{q_{\text{ult}}}{q_{\text{max}}} = \frac{750}{94.09} = 7.97 \geq 3 \checkmark \text{ ok}$$

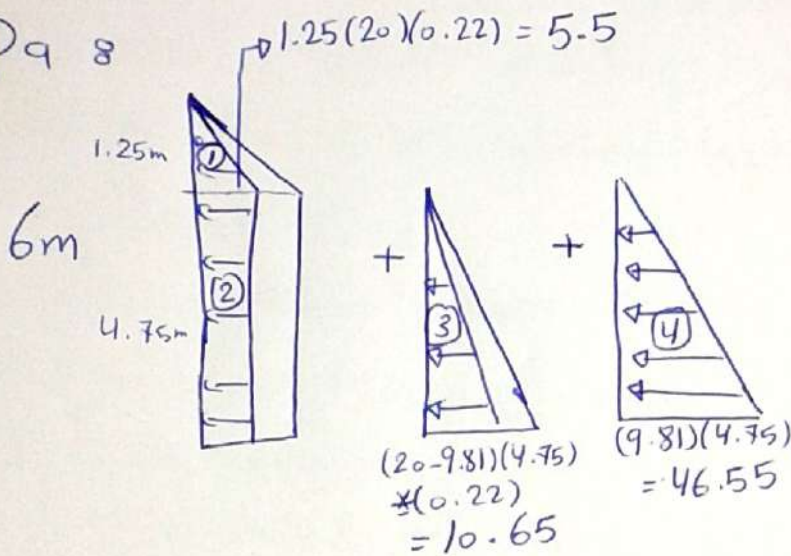
Q1 (12 point) :

$$K_{a1} = \frac{1 - \sin \phi_1}{1 + \sin \phi_1} = \boxed{0.22}$$

$$K_{p2} = \frac{1 + \sin \phi_2}{1 - \sin \phi_2} = \frac{1 + \sin 20}{1 - \sin 20} = \boxed{2.04}$$

\*\* يتم حساب كل من  $P_a$  ,  $P_p$  من السابفة :

•  $P_a$  :

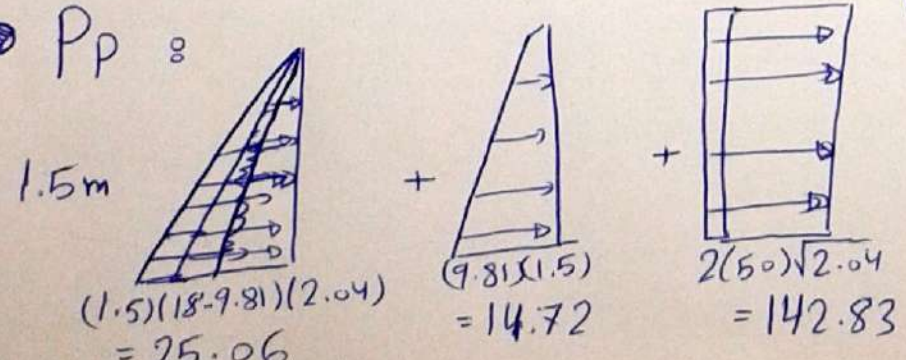


Seg #	$\phi_i / m$	$X_i$	$\phi_i \cdot X_i$
1	3.44	5.167	17.77
2	26.125	2.375	62.05
3	25.29	1.58	39.96
4	110.56	1.58	174.68
$\Sigma$			$\Sigma 294.46$

$$\bar{X} = \frac{\Sigma \phi_i X_i}{\Sigma \phi_i} = \boxed{1.78 \text{ m}}$$

$$P_a / m = 165.415$$

•  $P_p$  :



$$\begin{aligned}
 P_p / m &= 0.5(1.5)(25.06) \\
 &+ 0.5(1.5)(14.72) \\
 &+ 142.83(1.5) \\
 &= 18.8 + 11.04 + 214.25 \\
 &= \boxed{244.09 \text{ KN/m}}
 \end{aligned}$$

1] Piles are commonly used for 8 اذكر 5 نقاط

- 1- to carry structure loads into or through a soil stratum
- 2- To resist uplift or overturning forces.
- 3- To control earth movements such as landslides
- 4- To control settlement when spread footing are on marginal or highly compressible soil.
- 5- To control scour problems on bridge abutment or piers

2] footing should be carried below 8 نوايا

- 1) The frost line خط التجمد
- 2) Zones of high volume change due to moisture fluctuation
- 3) Top soil or organic matter
- 4) Peat or muck
- 5) unconsolidated materials such as abandoned dumps

3] problems with soil settlement analysis 8 موجهة بالرسالة

4] Serviceability Limit = اشرح المفاهيم

$\overline{AA'}$ : Total settlement "S<sub>TA</sub>"

$\overline{BB'}$ : ~ ~ "S<sub>TB</sub>"

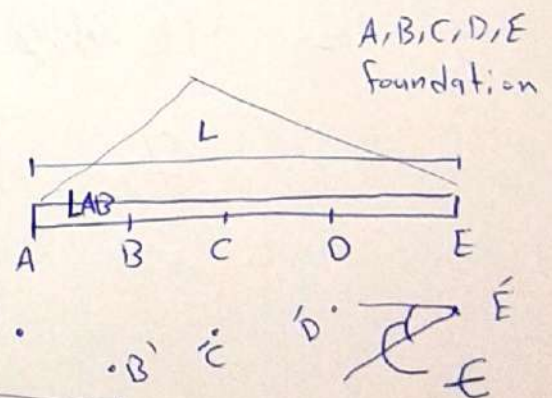
$\Delta S_{TAB}$ : differential settlement between A & B

$\alpha$  = gradient between any two footing.

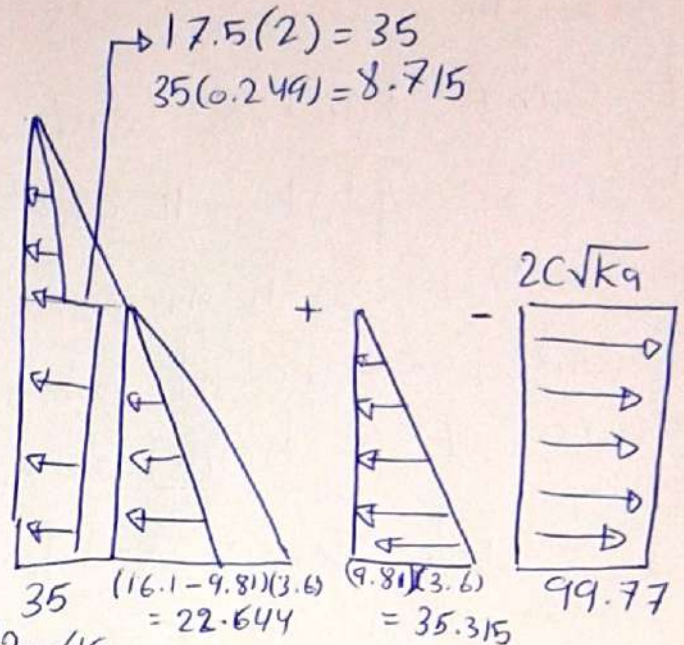
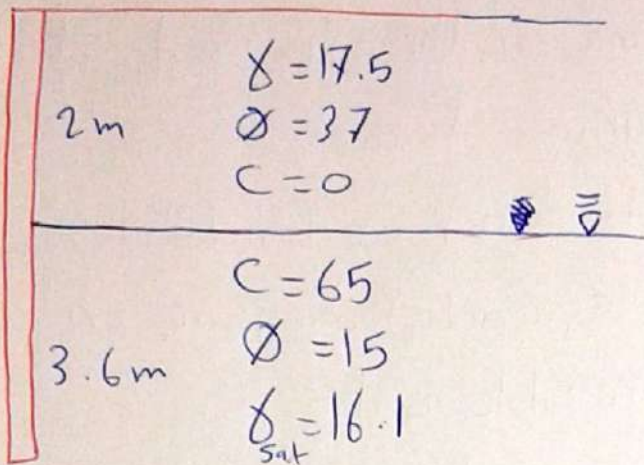
$\beta$  = angular distortion

$\epsilon$  = tilt angle (Rad)

$$= \left[ \frac{\Delta S_{Tij} \text{ (Rad)}}{L_{ij}} \right] \Rightarrow \frac{\Delta S_{TAB}}{L_{AB}}$$



✶✶ فكرة سنوات Tensile crack

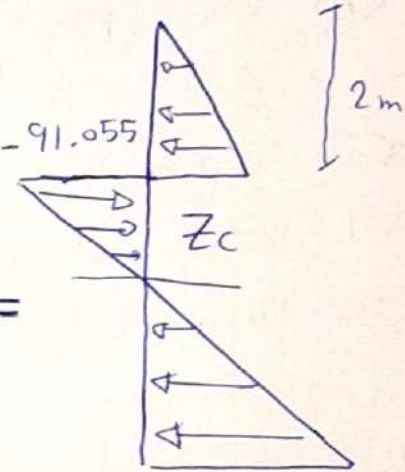


$K_{a1} = 0.249$

$K_{a2} = 0.589$

~~$35(20 - 615)$~~   
 ~~$35(0.589)$~~   
 $22.644(0.589) = 13.34$

$8.715 - 99.77 = -91.055$



✶ لبيحار  $Z_c$

Tensile Crack

$0 = (13.34 H + 35.315 H) - 91.055$

$\Rightarrow 48.655 H = 91.055$

$Z_c = 1.871m$

تأكد من الحل

